

Job	Processing Time (Hours)	Due Hour	Slack	Critical Ratio
a	$(.14 \times 45) + .7 = 7$	4	$4 - 7 = -3$	$4 / 7 = .57$
b	$(.25 \times 14) + .5 = 4$	10	$10 - 4 = 6$	$10 / 4 = 2.5$
c	$(.10 \times 18) + .2 = 2$	12	$12 - 2 = 10$	$12 / 2 = 6$
d	$(.25 \times 40) + 1 = 11$	20	$20 - 11 = 9$	$20 / 11 = 1.82$
e	$(.10 \times 75) + .5 = 8$	15	$15 - 8 = 7$	$15 / 8 = 1.875$

MST: a-b-e-d-c

SPT: c-b-a-e-d

EDD: a-b-c-e-d

CR: a-d-e-b-c

MST:

Job	Operation time (hr.)	Completion time (hr.)	Due hour	Hours Late
a	7	7	4	3
b	4	11	10	1
e	8	19	15	4
d	11	30	20	10
c	2	<u>32</u>	12	<u>20</u>
		99		38

SPT:

Job	Operation time (hr.)	Completion time (hr.)	Due hour	Hours Late
c	2	2	12	0
b	4	6	10	0
a	7	13	4	9
e	8	21	15	6
d	11	<u>32</u>	20	<u>12</u>
		74		27

EDD:

Job	Operation time (hr.)	Completion time (hr.)	Due hour	Hours Late
a	7	7	4	3
b	4	11	10	1
c	2	13	12	1
e	8	21	15	6
d	11	<u>32</u>	20	<u>12</u>
		84		23

CR:

Job	Operation time (hr)	Completion time (hr)	Due Hour	Hours late
a	7	7	4	3
d	11	18	20	0
e	8	26	15	11
b	4	30	10	20
c	2	<u>32</u>	12	<u>20</u>
		113		54

	<u>MST</u>	<u>SPT</u>	<u>EDD</u>	<u>CR</u>
<i>Average flow time</i> = $\frac{\text{Flow time}}{\text{Number of jobs}}$	$\frac{99}{5} = 19.80$	$\frac{74}{5} = 14.80$	$\frac{84}{5} = 16.80$	$\frac{113}{5} = 22.6$
<i>Average hours late</i> = $\frac{\text{Hours late}}{\text{Number of jobs}}$	$\frac{38}{5} = 7.60$	$\frac{27}{5} = 5.40$	$\frac{23}{5} = 4.60$	$\frac{54}{5} = 10.8$
<i>Average no. of jobs at the center</i> = $\frac{\text{Flow time}}{\sum \text{job times}}$	$\frac{99}{32} = 3.09$	$\frac{74}{32} = 2.31$	$\frac{84}{32} = 2.625$	$\frac{113}{32} = 3.53$

For this data, there is no one superior priority rule. SPT has the lowest avg. flow time and avg. WIP, but EDD has the lowest avg. hours late.

3. a.

<u>Job</u>	<u>Time (days)</u>	<u>Due Date</u>	<u>Slack</u>	<u>Critical Ratio</u>
A	8	20	12	2.5
B	10	18	8	1.8
C	5	25	20	5.0
D	11	17	6	1.55
E	9	35	26	3.89

Sequences:

- (1) CR: D-B-A-E-C
- (2) MST: D-B-A-C-E
- (3) SPT: C-A-E-B-D
- (4) EDD: D-B-A-C-E

b. CR:

<u>Job</u>	<u>Time (days)</u>	<u>Completion time (days)</u>	<u>Due Date</u>	<u>Days Late</u>
D	11	11	17	0
B	10	21	18	3
A	8	29	20	9
E	9	38	35	3
C	5	<u>43</u>	25	<u>18</u>
		142		33

SPT:

Job	Time (days)	Completion time (days)	Due Date	Days Late
C	5	5	25	0
A	8	13	20	0
E	9	22	35	0
B	10	32	18	14
D	11	<u>43</u>	17	<u>26</u>
		115		40

EDD & MST

Job	Time (days)	Completion time (days)	Due Date	Days Late
D	11	11	17	0
B	10	21	18	3
A	8	29	20	9
C	5	34	25	9
E	9	<u>43</u>	35	<u>8</u>
		138		29

$$\begin{array}{l}
 \text{Average flow time} = \frac{\text{completion time:}}{\text{number of jobs}} \\
 \text{Average days late} = \frac{\text{total days late:}}{\text{number of jobs}}
 \end{array}
 \begin{array}{l}
 \text{CR} \\
 \frac{142}{5} = 28.4
 \end{array}
 \begin{array}{l}
 \text{SPT} \\
 \frac{115}{5} = 23
 \end{array}
 \begin{array}{l}
 \text{EDD \& MST} \\
 \frac{138}{5} = 27.6 \\
 \frac{40}{5} = 8 \\
 \frac{29}{5} = 5.8
 \end{array}$$

- c. No, SPT has the smallest average flow time, but EDD & MST have the smallest average days late.

4. Using Johnson's rule:

Order	Time (hr.)		Sequence of assignment:
	Step 1	Step 2	
A	1.20 ③	1.40	.80 [C] last (i.e., 7th)
B	0.90 ②	1.30	.90 [B] first
C	2.00	0.80 ①	1.20 [A] 2nd
D	1.70	1.50 ⑤	1.30 [G] 3rd
E	1.60 ⑥	1.80	1.50 [D] 6th
F	2.20	1.75 ⑦	1.60 [E] 4 th
G	1.30 ④	1.40	1.75 [F] 5th

Thus, processing sequence is B-A-G-E-F-D-C.

Note: Order of assignment is given in circles.

19. Each period's increase in WIP is equal to (actual input - actual output). That amount is added to (or subtracted from) the previous WIP to obtain the current (shown) WIP for the period.

1.	Number of recalibrations	Probability of occurrence	Number of expected problems
	0	.15	0
	1	.25	.25
	2	.30	.60
	3	.20	.60
	4	<u>.10</u>	<u>.40</u>
		1.00	1.85

Period

		1	2	3	4	5
Input	Planned	24	24	24	24	20
	Actual	25	27	20	22	24

Output	Planned	24	24	24	24	23
	Actual	24	22	23	24	24

WIP	12	13	18	15	13	13
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