



First Letter Last Name

Name: Ans Key

Student Number: _____

PHYS 101 Mid-term 2 November 7, 2007

Marks				
Q1 (7)	Q2 (8)	Q3 (8)	Q4 (7)	Total (30)

It is recommended that you use pen – if you use pencil then any requests for regrading may be denied.

Simple scientific calculator

Question 1 a) Circle the correct answer (1 mark)

Standing waves are produced by the superposition of two waves with

- ①
- A) the same amplitude, frequency, and direction of propagation
 - B) the same amplitude and frequency, and opposite propagation directions.
 - C) the same amplitude and direction of propagation, but different frequencies.
 - D) the same amplitude, different frequencies, and opposite directions of propagation.

Question 1b) (6 marks)

Listed below are the equations for traveling waves, where x and y are in metres and, t is in seconds and the numerical values have the appropriate units.

^{3/4} A ^{4/4}
 $y = 6\sin(4x + 4t)$

B ^{8/3}
 $y = 4\sin(-3x + 8t)$

C ^{6/4}
 $y = 3\sin(4x + 6t)$

D ^{3/6}
 $y = -6\sin(-6x + 3t)$

E ^{6/6}
 $y = 4\sin(-6x - 6t)$

F ^{8/2}
 $y = 3\cos(2x - 8t)$

i) Rank the waves from greatest to least in order of wavelength, indicating any equality:

F > B > A = C > D = E Least

ii) Rank the waves from greatest to least in order of wavespeed, indicating any equality:

F > B > C > A = E > D Least

iii) Which waves are traveling in the negative x-direction? Show your reasoning.

- A $4x + 4t = \text{const}$ if $t \uparrow$ $x \downarrow$
- B $-3x + 8t = \text{const}$ if $t \uparrow$ $x \uparrow$
- C $4x + 6t$ as A
- D $-6x + 3t$ as B
- E $-6x - 6t = \text{const}$ if $t \uparrow$ $x \downarrow$
- F $2x - 8t = \text{const}$ if $t \uparrow$ $x \uparrow$

A C E

②

Reasoning 1 mark
miss 1 - 1/2

Question 2a (4 marks)

A student wishes to measure the depth of a well, which can be modeled as a pipe closed at one end. She uses a loud speaker to generate acoustic resonances. She hears a resonance at 170 Hz and the next resonance is at 190 Hz. Assume the speed of sound in air is 343 m/s.

i) What is the lowest resonant frequency for the well?

①

10 Hz

ii) What is the depth of the well?

②

$$L = \frac{\lambda}{4} = \frac{343}{40} = 8.58 \text{ m}$$

iii) Which harmonics did she hear?

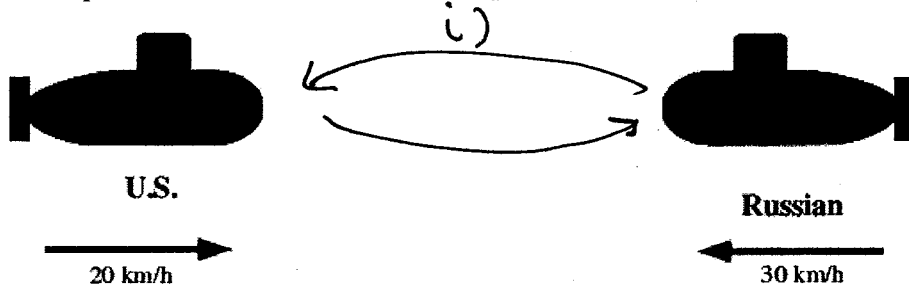
17 Hz & 19 Hz

①

Question 2b (4 marks)

A U.S. submarine and a Russian submarine move toward each other in still water in the North Atlantic. The U.S. submarine moves at 20.0 km/h and the Russian submarine at 30.0 km/h. The Russian submarine sends out sonar (sound in water) waves traveling with a speed of 5,500 km/h and at a frequency of 1500 Hz.

$$f' = f \left(\frac{v \pm v_o}{v \pm v_s} \right)$$



check signs

i) What is the frequency detected by the U.S. submarine?

$v_s = 30 \text{ km/h}$ $v_o = 20 \text{ km/h}$

②

$$f' = 1500 \left(\frac{5500 + 20}{5500 - 30} \right)$$

source & detector towards (mix up)
= 1514 Hz (1513.7)

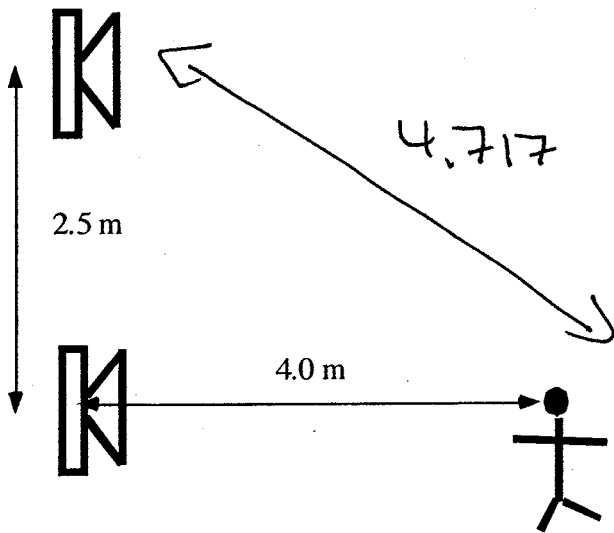
ii) What is the frequency detected by the Russian submarine for the signal reflected back to it by the U.S. submarine?

$v_s = 20 \text{ km/h}$ $v_o = 30 \text{ km/h}$

②

$$f'' = f' \left(\frac{5500 + 30}{5500 - 20} \right) = 1527.5 \text{ Hz}$$

Question 3a (4 marks)



Path difference

$$\Delta x = 0.717 \text{ m} \dots \textcircled{1}$$

Two loud speakers, separated by a distance of 2.50 m, are in phase and produce sound waves of the same frequency. There is a listener 4.00 m in front of one speaker as shown. The frequency of the speakers is slowly increased from 20 Hz.

i) What are the three lowest frequencies at which the listener hears a maximum signal?

Const $\Delta x = m \lambda$ $m=1 \lambda = 0.717 \text{ m}$ $f = \frac{343}{0.717} = 478 \text{ Hz}$
 $m=2 \lambda = 0.358 \text{ m}$ $f_2 = \frac{343}{0.358} = 957 \text{ Hz}$
 $m=3 \lambda =$ 1435 Hz

(method = 1)

ii) What are the three lowest frequencies at which the listener hears a minimum signal?

$\Delta x = (m + \frac{1}{2}) \lambda$ $m=0 \lambda = 1.434 \text{ m}$ $f_1 = 239 \text{ Hz}$
 $m=1 \lambda = 0.478 \text{ m}$ $f_2 = 718 \text{ Hz}$
 $m=2 \lambda = 0.287$ $f_3 = 1196 \text{ Hz}$

Question 3b (3 marks)

Twenty violins are played simultaneously with the same intensity. Together, they produce a sound level of 80.0 dB.

If only one is playing:

$$80 = 10 \log \frac{20 I}{I_0} = 10 \log \frac{I}{I_0} + 10 \log 20$$

i) What is the sound level (dB) of a single violin?

$$80 - 10 \log 20 = 67 \text{ dB}$$

ii) What is the intensity of a single violin?

$$6.7 = \log \frac{I}{I_0} = \log I + 12$$

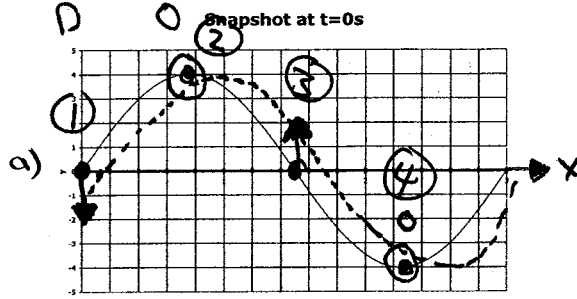
$$\log I = 6.7 - 12 = -5.3$$

$$I = 1 \times 10^{-5.3} = 5.0 \times 10^{-6} \text{ W/m}^2$$

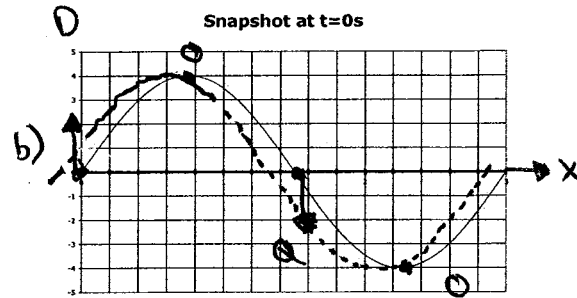
Question 4 (7 marks)

The identical figures at the side show a snapshot of a wave on a wire at $t = 0$. On the figures, sketch what the snapshot would look like at an **instant later** i.e. a time later that is **much** smaller than the period of oscillation for each of the following cases.

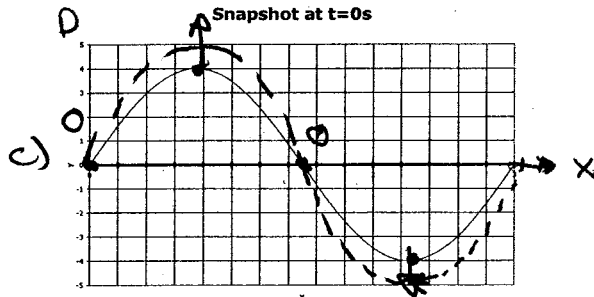
a) A wave traveling in the positive x-direction.



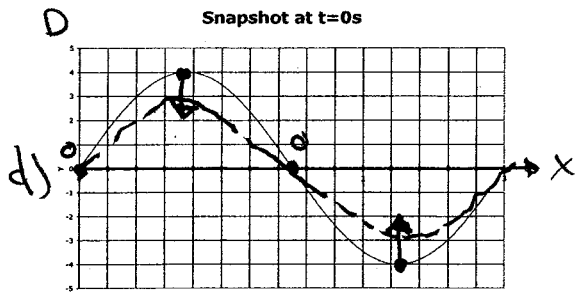
b) A wave traveling in the negative x-direction



c) A standing wave with a displacement that at $t=0$ is increasing.



d) A standing wave with a displacement that at $t=0$ is decreasing.



e) On the above diagram for part a, four points on the wire are indicated. Indicate the velocity of a particle on the wire (use an arrow indicating the relative size and direction) at these points at the instant $t = 0$.

Repeat for parts b, c and d.

2 (a & b) zero or v. small correct dir pts 2 & 4
 pts 1 & 3

1 (c & d) zero at pts 1 & 3 correct dir pts 2 & 4