

# MATH2004DE-Assignment 1

- This Assignment MAY NOT be distributed in any way without written permission of your professor.
- You may either write your answers on this, or on your own paper or on your electronic devices (do not need to copy questions).
- Show all of your work in getting your solution. A correct final answer with no justification risks getting zero points! **Keep exact answer.**
- Due date: **Friday, Jan 29 at 10pm. Total points: 30 points.**
  - No e-mail submission will be accepted.
  - Technical issues are not an excuse. Don't wait until the deadline to submit.
- Submission Requirements:
  - Only a **single PDF** file is allowed. Other file types will NOT be accepted. Combine all pages into **single** .pdf file (using any app or software you like, such as CamScanner). Submit this .pdf file on CuLearn.
  - If you have some changes after submission, you can resubmit before deadline.
  - Once you submit your assignment, **you certified that this is your own work.** The penalty for plagiarism is going to be very substantial.
  - Page size: A4 or Letter.
  - Orientation: The PDF document should be in proper orientation so as not to require rotation.
  - Resolution: The PDF document must be of sufficient resolution and writing must be legible. Pictures of your work are NOT an acceptable substitute for a scan.
  - File name format: **LastName-StudentNumber-Ass1.pdf**
  - Failure to follow these instructions will result in a grade of zero.

Surname \_\_\_\_\_ First Name \_\_\_\_\_ Student # \_\_\_\_\_

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1. (4 points) Given the two lines:

$$L_1 : \vec{r}(t) = (1, 1, 2) + t(1, 1, -2), \quad t \in \mathbb{R};$$

$$L_2 : \vec{r}(t) = (1, 7, -2) + s(1, -5, 2), \quad s \in \mathbb{R}.$$

- (a) Classify the relation of the two lines, i.e., parallel, or intersected (if so, find the intersection), or skewed.
- (b) Find the equation of the plane containing the two lines.

2. (2 points) Given the two planes:

$$\Pi_1 : 2x - y + 3z = 5; \quad \Pi_2 : x + 2y + kz = 3.$$

Find the value of  $k$  such that the angle between the two planes is  $\frac{\pi}{4}$ .

3. (2 points) Given that the image of the point  $(x, y)$  under the change of the origin  $\mathbf{O}=(1,5)$ , then followed by a counterclockwise rotation of the new axes with the angle  $\theta = \frac{\pi}{2}$  is  $(2, -1)$ . Find the point  $(x, y)$ .

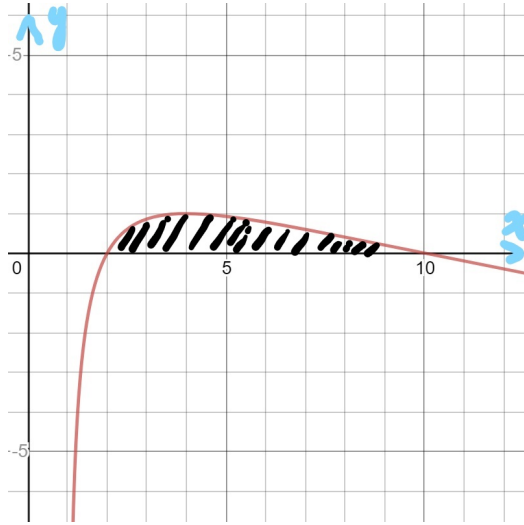
4. (4 points) The parametric curve  $C$  is given by

$$x = t^2 + \ln(2e^{t-1} - t), y = t^6 - \cos(t^2\pi).$$

Find the tangent line to the curve at the point  $t = 1$ .

5. (4 points) Find the length of the curve  $C$ :  $x = e^{3t} \cos(4t)$ ,  $y = e^{3t} \sin(4t)$ ,  $0 \leq t \leq 1$ .

6. (5 points) The region  $D$  is enclosed by the curve  $x = 1 + e^{t \ln 3}$ ,  $y = 2t - t^2$  and the  $x$ -axis. Find the area of the region  $D$ .



7. (5 points) Find the tangent line of the polar curve  $r = 2 + \sin \theta$  at  $\theta = 0$ .

8. (4 points) Find the area of the region outside  $r = 3 + 4 \sin \theta$  and inside  $r = 5 + 2 \sin \theta$ , from  $\theta = 0$  to  $\theta = \frac{\pi}{2}$ .