

MAT 1341A Test 1- Diagnostic test 2015

21-September - 2015. Duration: 80 minutes.

Instructor: Barry Jessup

θ	$\sin \theta$	$\cos \theta$
0	0	1
$\frac{\pi}{6}$	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$
$\frac{\pi}{4}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{2}}{2}$
$\frac{\pi}{3}$	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$
$\frac{\pi}{2}$	1	0

1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	
12	
Total	

Family Name: _____

First Name: _____

Student number: _____

PLEASE READ THESE INSTRUCTIONS CAREFULLY.

1. You have 80 minutes to complete this exam.
2. This is a closed book exam, and no notes of any kind are permitted. The use of calculators, cell phones, or similar devices is not permitted. All implanted cyber devices not necessary for life-support must be disabled at the beginning of the exam.
3. Read each question carefully – you will save yourself time and unnecessary grief later on.
4. All questions are multiple choice, are worth 1 point each and no part marks will be given. Please record your answers in the spaces on this page provided next to the question numbers above.
5. Where it is possible to check your work, do so.
6. Good luck! Bonne chance!

1. An equation for the plane which contains the two lines with parametric equations $x = -1 + t$, $y = -1 - t$, $z = 1 + 3t$ and $x = -3 - s$, $y = 3 + 2s$, $z = 7 + 3s$, is:

A. $7x - 11y + 2z = 6$

B. $11x - 2y + 9z = 0$

C. $6x - 2y + z = -3$

D. $3x - 6y + z = 4$

E. $9x + 6y - z = -16$

F. $9x + 6y + z = -14$

2. An equation for the plane passing through the points $(0, -3, 0)$ and $(-1, 1, 2)$, and which is parallel to the x -axis is:

A. $3x + 2y + 7z = -6$

B. $2x - y = 3$

C. $x - y + z = 3$

D. $x - z = 0$

E. $y - 2z = -3$

F. $x + y + z = -3$

3. Find an equation of the plane which passes through the point $(1, 1, 1)$ and which is perpendicular to the line whose scalar parametric equations are:

$$x = -6 + 2t, y = 1 - 4t, z = -3 + 3t; t \in \mathbf{R}.$$

- A. $2x - 4y + 3z = 1$
- B. $2x + 4y + 3z = 9$
- C. $6x + y - 3z = 2$
- D. $2x - 4y + 3z = -25$
- E. $2x - 4y + 3z = -10$
- F. $2x - 4y + 3z = 10$

4. Parametric equations for the line containing $(2, -2, 3)$ and $(-2, 4, 0)$ are:

- A. Such a line does not exist.
- B. $x = 2 - 2t, y = -2 + 4t, z = 3; t \in \mathbf{R}.$
- C. $x = 1 - t, y = -1 - 6t, z = 4 + 3t; t \in \mathbf{R}.$
- D. $x = 3 + 4t, y = -1 - 6t, z = 6 + t; t \in \mathbf{R}.$
- E. $x = 2 + 4t, y = -2 - 6t, z = 3 + 3t; t \in \mathbf{R}.$
- F. $x = -2 + 4t, y = 4 + 6t, z = 1 + 3t; t \in \mathbf{R}.$

5. Find a Cartesian (scalar) equation for the plane with vector parametric equation

$$v = (0, 2, -2) + s(1, -1, 2) + t(2, -4, -1); s, t \in \mathbf{R}.$$

A. $4x - 9y + 6z = -30$

B. $9x + 5y - 2z = 14$

C. $9x - 5y + 2z = -14$

D. $9x + 5y + 2z = 6$

E. $9x + 2y + 5z = -6$

F. $9x - 2y + 5z = -14$

6. Find all vectors in \mathbf{R}^3 which are perpendicular to both $(-1, 1, 5)$ and $(2, 1, 2)$.

A. $\{(2, -8, 2)\}$

B. $\{(t+1, -8, t+1) \mid t \in \mathbf{R}\}$

C. $\{(t, -4t, t) \mid t \in \mathbf{R}\}$

D. $\{(-t, 0, t) \mid t \in \mathbf{R}\}$

E. $\{(0, 0, 0)\}$

F. $\{(3, -12, 3)\}$

7. A triangle has vertices $A = (1, 1, 1)$, $B = (2, 3, 1)$ and $C = (1, 2, 3)$. Find the cosine of the interior angle at A .

- A. 0
- B. $1/5$
- C. $2/5$
- D. $3/5$
- E. $4/5$
- F. 1

8. The point of intersection of the line through the point $(2, 1, 0)$ parallel to the vector $u = (1, -1, 2)$ with the plane with equation $x + y + 2z = 23$ is:

- A. $(11, 4, 4)$
- B. $(2, 1, 10)$
- C. $(7, -4, 10)$
- D. $(7, 4, 6)$
- E. $(11, 1, 4)$
- F. $(10, -4, 7)$

9. If $u = (3, 3, 6)$ and $v = (2, -1, 1)$ then the length of the projection of u along v is:

A. $\frac{3\sqrt{6}}{2}$

B. $\frac{3\sqrt{2}}{2}$

C. 0

D. $\frac{\sqrt{6}}{2}$

E. $\frac{2\sqrt{6}}{3}$

F. $\frac{2\sqrt{2}}{3}$

10. Find the area of the triangle whose vertices are the points $P = (3, -1, 2)$, $Q = (1, 1, 0)$ and $R = (1, 2, -1)$.

A. 4

B. $2\sqrt{2}$

C. $\sqrt{2}$

D. 0

E. $4\sqrt{2}$

F. 2

11. Write the complex number

$$\frac{(1 + 3i)(5 + 10i)}{4 + 3i}$$

in Cartesian form: $a + bi$, with $a, b \in \mathbf{R}$.

- A. $-1 + 7i$
- B. -1
- C. $1 + 7i$
- D. $7i$
- E. $-5 + 35i$
- F. $-\frac{1}{5} + \frac{7}{5}i$

12. What is the polar form of $\frac{-\sqrt{2} + \sqrt{2}i}{3 + 3\sqrt{3}i}$?

- A. $\frac{1}{3}(\cos(5\pi/12) + i \sin(5\pi/12))$
- B. $\frac{1}{3}(\cos(5\pi/12) - i \sin(5\pi/12))$
- C. $3(\cos(5\pi/12) - i \sin(5\pi/12))$
- D. $3(\cos(5\pi/12) + i \sin(5\pi/12))$
- E. $\cos(11\pi/12) + i \sin(11\pi/12)$
- F. $\cos(5\pi/12) + i \sin(5\pi/12)$

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