

Statistics

Chapter Eight

- **Nonparametric tests** are used primarily when:
 - **Outcomes (DV)** are not measured on an interval or ratio scale
 - **Assumptions for parametric tests** are severely violated
 - Especially when sample sizes are small

- **Selection of a nonparametric test** depends mostly on:
 - **Number of groups** being compared (two vs three or more)
 - **Type of comparison** being made
 - **Independent groups** (between-subjects design)
 - **Dependent groups** (within-subjects/ repeated measures, correlated groups design)

- **Chi-Square Test of Independence**
 - Tests relationships between two categorical variables in a **contingency table**
 - A test of differences in proportions between groups

- **Chi-Square Test Hypothesis**
 - **Null hypothesis**: The two categorical variables are independent (unrelated)
 - ~~Eq~~ Proportions across groups are equal
 - **Alternative hypothesis**: The two variables are not independent - they are related
 - ~~Eq~~ Proportions across groups are not equal

- **Assumptions for Chi-Squared Test**
 - Random sampling from the population
 - Each observation is independent (eq. no correlated groups)
 - Each cell in the contingency table must have an expected frequency greater than zero

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• General logic for Chi-Squared Test

- If the null hypothesis is true there should be no differences in proportions (relative frequencies) for groups being compared.
- The test contrasts observed frequencies in each cell of a crosstab table with expected frequencies > the frequencies that would be expected if the null hypothesis were true

• Observed vs Expected Frequencies

- Each cell needs an expected frequency
 - $E = \text{Row total} \times \text{Column Total} \div N$
- Observed frequency is just what's in the cell

• Sampling Distribution

- For each cell:
 - $(O - E)^2 \div E$
- Add all the cell components together to obtain X^2
- In X^2 $df = (\text{Rows} - 1) \times (\text{Columns} - 1)$
- If calculated $X^2 \geq$ tabled value reject the null hypothesis

• If expected value for multiple cells is < 5 use Fisher's exact test

- Sometimes for 2×2 tables a correction factor is applied:
Yates Continuity Correction

• Magnitude of Effects

- Index summarizing strength of relationship in $2 \times 2 = \phi$ (Phi)
 - Phi varies from 0-1 & can be interpreted as Pearson's r
- Index summarizing strength of relationship in larger tables:
Cramér's V
 - Varies from 0 to 1

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• Other Tests for Independent groups

- For ordinal level data - or for higher-level data when parametric tests can't be used bc of a violated assumption:
 - Two groups > Mann-Whitney U Test
 - Three or more groups > Kruskal-Wallis Test
- Both are rank tests that examine differences b/w groups in location

• The Mann-Whitney U Test

- Tests the null hypothesis that two population distributions are identical
 - The nonparametric analog of the independent group t-test
- For $N_s > 20$, normal distribution (z values) can be used
- When displaying outcomes in a table, median values of the dependent variable for the two groups are often shown

• Kruskal-Wallis Test

- Tests the null hypothesis that three or more population distributions are identical
 - The nonparametric analog of a one-way ANOVA
- Compares the ranks of the values for the groups
- Test statistic is H which follows chi-squared distribution
- Significant results only indicate that there is a difference among the groups, does not indicate which ones
 - To isolate groups that are significantly different use the Dunn Procedure
 - This involves using the Mann-Whitney U Test for all possible pairs

* In Spss look at the significance level

- .05 or smaller, reject the null hypothesis