University of Ottawa
MAT 1332 Practice Midterm Exam
Duration: 80 Minutes.

Family Name:_____

First Name:_____

Do **not** write your student ID number on this front page. Please write your student ID number in the space provided on the second page.

Take your time to read the entire paper before you begin to write, and read each question carefully. Remember that certain questions are worth more points than others. Make a note of the questions that you feel confident you can do, and then do those first: you do not have to proceed through the paper in the order given.

- You have 80 minutes to complete this exam.
- This is a closed book exam, and no notes of any kind are allowed.
- Cellular phones, unauthorized electronic devices or course notes are not allowed during this exam. Phones and devices must be turned off and put away in your bag. Do not keep them in your possession, such as in your pockets. If caught with such a device or document, the following may occur: you will be asked to immediately leave the exam and academic fraud allegations will be filed, which may result in you obtaining a 0 (zero) for the exam. By signing below, you acknowledge that you have ensured that you are complying with the above statement:

  Signature:_____
- Only the Faculty approved calculators (TI-30X, TI-34X, Casio FX-260X and Casio FX-300X) are allowed. All others will be confiscated.
- The correct answer requires justification written legibly and logically: you must convince me that you know why your solution is correct. Answer these questions in the space provided. Use the backs of pages if necessary.
- If you tear off any blank pages, they have to be handed in.
- Where it is possible to check your work, do so.
- Good luck!

Student number:_____, Total marks: _____ out of 30

Problem	1	2	3	4	5	6	7
Marks							

Question 1. [4 points] Calculate

a) $\displaystyle\int_{-2}^{2} \frac{1}{y^2-9}\,dy$ **b)** $\displaystyle\int_{-\pi/2}^{\pi/2} \frac{\sin(x)}{1+\cos^2(x)}\,dx$

Question 2. [3 points] Evaluate the integral

$$\int \frac{2x+1}{x^2-2x+5}dx$$

Question 3. [4 points] Evaluate the integral

$$\int \frac{x^3 + 2x^2 - 18x + 2}{x^2 + x - 12}\, dx.$$

Question 4. [6 points] For each of the following improper integrals, determine whether it converges, and determine its value if it does.

a) $\displaystyle\int_1^3 \frac{1}{t\,\ln t}\,dt$ **b**) $\displaystyle\int_0^\infty \frac{3}{18+2t^2}\,dt$ **c**) $\displaystyle\int_5^\infty \frac{\ln x}{x^2}\,dx$

BLANK PAGE FOR EXTRA WORK

Question 5. [4 points] Define functions f and g by

$$f(x) = 3x^2 \qquad\qquad g = -3x + 6$$

a) Show that f and g intersect at points $x = -2$ and $x = 1$.
b) Calculate the area between f and g in the interval $-4 \leq x \leq 2$.
c) If this region is rotated around the x-axis, find the volume.

Question 6. [4 points] **a**) A very skinny 2m-long snake has density $\rho(x)$ kg/m at a distance x from the head of the snake, where

$$\rho(x) = 2x - x^2.$$

What is the total mass of the snake?
b) A less skinny 2m-long snake's body is given by rotating the function

$$y = \frac{e^{-x/2}}{10}, \qquad 0 \leq x \leq 2$$

about the x-axis (the units of y is also m). What is the volume of this snake?

Question 7. [5 points] Determine the average value of $f(x) = x\ln(x)$ over the range $0 \leq x \leq 2$. (Hint: to calculate an indeterminate limit, rearrange and use L'Hôpital's rule.)

BLANK PAGE FOR EXTRA WORK