

1.

$$\Delta H + \Delta E_k + \Delta E_p \overset{\rightarrow 0}{=} Q - W_s \overset{\rightarrow 0}{}$$

$$\Delta H + \Delta E_k = Q$$

from steam tables

$$\hat{H}(\text{H}_2\text{O}(l), 24^\circ\text{C}, 10\text{bar}) = 100.6 \text{ kJ/kg}$$

$$\hat{H}(10\text{bar, saturated steam}) = 2776.2 \text{ kJ/kg}$$

$$\Delta \hat{H} = 2776.2 \frac{\text{kJ}}{\text{kg}} - 100.6 \frac{\text{kJ}}{\text{kg}}$$

$$\Delta \hat{H} = 2675.6 \frac{\text{kJ}}{\text{kg}}$$

$$u_f = \frac{\dot{V}}{A} = \frac{15000 \text{ m}^3/\text{h} \left(\frac{1\text{h}}{3600\text{s}}\right)}{0.25 \pi (15 \times 10^{-2} \text{ cm})^2} = 235.8 \text{ m/s}$$

from steam tables,  $\hat{V}(10\text{bar, saturated steam}) = 0.1943 \text{ m}^3$ 

$$\dot{m} = (15000 \text{ m}^3/\text{h}) \left(\frac{1\text{kg}}{0.1943 \text{ m}^3}\right) \left(\frac{1\text{h}}{3600\text{s}}\right) = 21.44 \text{ kg/s}$$

$$\Delta E_k = \frac{1}{2} \dot{m} u_f^2 - 0$$

$$= \frac{1}{2} (21.44) (235.8)^2$$

$$= 5.96 \times 10^5 \text{ J/s}$$

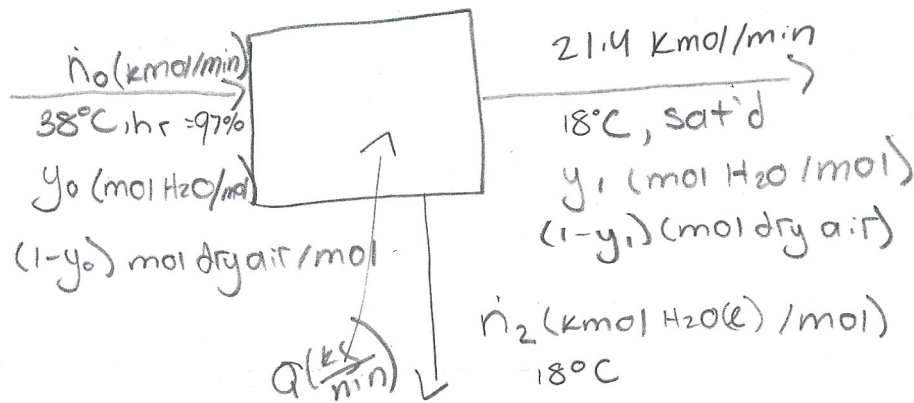
$$Q = \Delta H + \Delta E_k$$

$$= \dot{m} \Delta \hat{H} + \Delta \dot{E}_k$$

$$= (21.44 \frac{\text{kg}}{\text{s}}) (2675.6 \frac{\text{kJ}}{\text{kg}}) \times \frac{1000 \text{ J}}{1 \text{ kJ}} + 5.96 \times 10^5 \text{ J/s}$$

$$Q = 5.80 \times 10^7 \text{ W}$$

2a)



$$\text{basis: } 510 \frac{\text{m}^3}{\text{min}} \times \frac{273 \text{ K}}{291 \text{ K}} \times \frac{10^3 \text{ L}}{\text{m}^3} \times \frac{1 \text{ mol}}{22.4 \text{ L (STP)}} \times \frac{1 \text{ kmol}}{10^3 \text{ mol}}$$

$$= 21.4 \text{ kmol/min}$$

$$\text{Inlet condition: } y_0 = \frac{h_r p_{\text{H}_2\text{O}}^*(38^\circ\text{C})}{P} = \frac{0.97 (49.692 \text{ mmHg})}{760 \text{ mmHg}}$$

$$= 0.0634 \text{ mol H}_2\text{O/mol}$$

$$\text{outlet condition: } y_1 = \frac{p_{\text{H}_2\text{O}}^*(18^\circ\text{C})}{P} = \frac{15.477 \text{ mmHg}}{760 \text{ mmHg}}$$

$$= 0.0204 \text{ mol H}_2\text{O/mol}$$

Dry air balance:  $(1 - 0.0634) \dot{n}_0 = (1 - 0.0204) 21.4$

P3

$$\dot{n}_0 = 22.4 \text{ kmol/min}$$

Water balance:  $(0.0634)(22.4) = \dot{n}_2 + (0.0204) 21.4$

$$\dot{n}_2 = 0.98 \text{ kmol/min}$$

$$0.98 \text{ kmol/min} \times 18.02 \frac{\text{kg}}{\text{kmol}}$$

$$= 17.66 \frac{\text{kg}}{\text{min}} \text{ H}_2\text{O condenses}$$

b)

Enthalpies:  $\hat{H}_{\text{air}}(38^\circ\text{C}) = 0.0291(38 - 25) = 0.3783 \frac{\text{kJ}}{\text{mol}}$

$$\hat{H}_{\text{air}}(18^\circ\text{C}) = 0.0291(18 - 25) = -0.204 \frac{\text{kJ}}{\text{mol}}$$

$$\hat{H}_{\text{H}_2\text{O}}(\text{V}, 38^\circ\text{C}) = 2570.8 \frac{\text{kJ}}{\text{kg}} \times \frac{1 \text{ kg}}{10^3 \text{ g}} \times 18.02 \frac{\text{g}}{\text{mol}}$$

$$= 46.33 \frac{\text{kJ}}{\text{mol}}$$

$$\hat{H}_{\text{H}_2\text{O}}(\text{V}, 18^\circ\text{C}) = 2534.5 \frac{\text{kJ}}{\text{kg}} \times \frac{1 \text{ kg}}{10^3 \text{ g}} \times 18.02 \frac{\text{g}}{\text{mol}}$$

$$= 45.67 \frac{\text{kJ}}{\text{mol}}$$

$$\hat{H}_{\text{H}_2\text{O}}(\text{P}, 18^\circ\text{C}) = 75.5 \frac{\text{kJ}}{\text{kg}} \times \frac{1 \text{ kg}}{10^3 \text{ g}} \times 18.02 \frac{\text{g}}{\text{mol}}$$

$$= 1.36 \frac{\text{kJ}}{\text{mol}}$$

Energy balance:  $\Delta \hat{E}_P, W_s = 0 \quad \Delta E_K = 0$

P4

$$Q = \Delta H = \sum_{out} n_i \hat{H}_i - \sum_{in} n_i \hat{H}_i$$

$$= (1 - 0.0204)(21.4 \times 10^3)(-0.20) + (0.0204)(21.4 \times 10^3)(-0.20) + (0.98 \times 10^3)(1.36) - (1 - 0.0634)(22.4 \times 10^3)(0.3783) - (0.0634)(22.4 \times 10^3)(46.33)$$

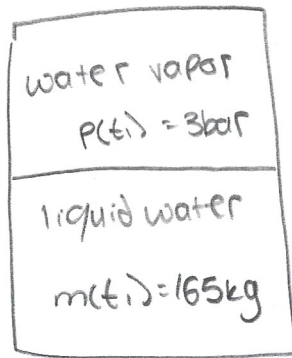
$$= -5.67 \times 10^4 \text{ kJ/min}$$

$$5.67 \times 10^4 \frac{\text{kJ}}{\text{min}} \times \frac{60 \text{ min}}{\text{h}} \times 0.9486 \frac{\text{Btu}}{\text{kJ}} \times \frac{1 \text{ ton cooling}}{12000 \text{ Btu}}$$

$$= 270 \text{ tons of cooling}$$

3.

P5



$$V = 200 \text{ L}$$

$$P_{\text{max}} = 20 \text{ bar}$$

a) From steam tables

$$T_s(3 \text{ bar, sat'd}) = \boxed{133.5^\circ\text{C}}$$

$$\hat{v}_l(3 \text{ bar, sat'd}) = 0.001074 \text{ m}^3/\text{kg}$$

$$\hat{v}_v(3 \text{ bar, sat'd}) = 0.606 \text{ m}^3/\text{kg}$$

The total volume is equal to the volume occupied by the liquid plus the head space

$$V_{\text{liquid}} = 165 \text{ kg} \left( \frac{0.001074 \text{ m}^3}{1 \text{ kg}} \right) \left( \frac{1000 \text{ L}}{1 \text{ m}^3} \right) = \boxed{177.2 \text{ L}}$$

$$V_{\text{space}} + V_{\text{liquid}} = 200 \text{ L}$$

$$V_{\text{space}} = 200 - 177.2$$

$$= \boxed{22.8 \text{ L}}$$

$$m_v = 22.8 \text{ L} \left( \frac{1 \text{ m}^3}{1000 \text{ L}} \right) \left( \frac{1 \text{ kg}}{0.606 \text{ m}^3} \right)$$

$$= \boxed{0.0376 \text{ kg}}$$

b) At  $t_2$ ,  $P = 20.0 \text{ bar}$

P6

$$T_2(20 \text{ bar, sat'd}) = 212.4^\circ\text{C}$$

$$\hat{v}_l(20 \text{ bar, sat'd}) = 0.001177 \text{ m}^3/\text{kg}$$

$$\hat{v}_v(20 \text{ bar, sat'd}) = 0.0995 \text{ m}^3/\text{kg}$$

if the liquid water is completely evaporated, volume would be:

$$V = 165 \text{ kg} \left( \frac{0.0995 \text{ m}^3}{1 \text{ kg}} \right) \left( \frac{1000 \text{ L}}{1 \text{ m}^3} \right) \\ = 16417.5 \text{ L}$$

this volume is much larger than total  $V$  (200 L) so some liquid water remains and the system is saturated.

$$T(t_2) = T(20 \text{ bar, sat'd}) \\ = 212.4^\circ\text{C}$$

$$m_{\text{total}} = 165 + 0.0376 \\ = 165.0376 \text{ kg}$$

$$V_l + V_v = 200 \text{ L}$$

$$m_l \hat{v}_l + (m_{\text{total}} - m_l) \hat{v}_v = 200 \text{ L}$$

$$m_l \left( 0.001177 \frac{\text{m}^3}{\text{kg}} \right) + (165.04 - m_l) \left( 0.0995 \frac{\text{m}^3}{\text{kg}} \right) = 200 \text{ L} \times \frac{1}{1000}$$

$$m_l = 164.98 \text{ kg}$$

$$m_v = 0.06 \text{ kg}$$

$$V_e = 164.98 (0.001177)$$

P7

$$V_L = 194.2 \text{ L}$$

$$V_{\text{space}} = 200 - 194.2$$

$$V_{\text{space}} = 5.8 \text{ L}$$

$$m_{\text{evap}} = m_v(t_2) - m_v(t_1)$$

$$= 0.06 - 0.0376$$

$$m_{\text{evap}} = 0.0224 \text{ kg}$$

e)  $\Delta E_p, \Delta E_k, W = 0$  because closed system

$$U_{\text{final}} = 164.98 \text{ kg} (906.2 \frac{\text{kJ}}{\text{kg}}) + 0.06 \text{ kg} (2598.2 \frac{\text{kJ}}{\text{kg}})$$

$$U_{\text{final}} = 149660 \text{ kJ}$$

$$U_{\text{initial}} = 165 \text{ kg} (561.1 \frac{\text{kJ}}{\text{kg}}) + 0.0376 \text{ kg} (2543 \frac{\text{kJ}}{\text{kg}})$$

$$U_{\text{initial}} = 92677.1 \text{ kJ}$$

$$\Delta U = 149660 - 92677.1$$

$$= 5.7 \times 10^4 \text{ kJ}$$

$$Q = \Delta U = 5.7 \times 10^4 \text{ kJ}$$