



$$MN = dx\bar{i} + dy\bar{j} + dz\bar{k}$$

d - scalar

$$\bar{\lambda} = \frac{MN}{MN} = \frac{MN}{d} = \frac{1}{d} MN =$$

$$= \frac{1}{d} (dx\bar{i} + dy\bar{j} + dz\bar{k})$$

$$F = F \cdot \bar{\lambda} = \frac{F}{d} (dx\bar{i} + dy\bar{j} + dz\bar{k})$$

$$F_x = \frac{F dx}{d}; F_y = \frac{F dy}{d}; F_z = \frac{F dz}{d}$$

Also "d" can be replaced w/ "F" (F<sub>x</sub>, F<sub>y</sub>, F<sub>z</sub>)

$$\cos \theta_x = \frac{dx}{d} \quad \cos \theta_y = \frac{dy}{d}$$

$$\cos \theta_z = \frac{dz}{d}$$

### Concurrent Forces (addition)

$$\bar{R} = \sum \bar{F} \Rightarrow R_x\bar{i} + R_y\bar{j} + R_z\bar{k} = \sum (F_x\bar{i} + F_y\bar{j} + F_z\bar{k})$$

$$R = \sqrt{R_x^2 + R_y^2 + R_z^2} \quad \cos \theta_x = \frac{R_x}{R} = \frac{\sum (F_x\bar{i})}{\sum (F_x\bar{i}) + \sum (F_y\bar{j}) + \sum (F_z\bar{k})}$$

Equilibrium of particle  
in space

$$\cos \theta_y = \frac{R_y}{R} \quad \cos \theta_z = \frac{R_z}{R}$$

$$\therefore R_x = \sum F_x\bar{i} \quad R_y = \sum F_y\bar{j} \quad R_z = \sum F_z\bar{k}$$

$$R_x = \sum F_x = 0; R_y = \sum F_y = 0; R_z = \sum F_z = 0$$

Problem:

AB - 2100N

AC - ?N

AD - ?N

Solution:

$$AB = \sqrt{(4)^2 + (20)^2 + (-5)^2} = 21\text{m}$$

$$\bar{F} = F \bar{\lambda}_{AB} = F \frac{\bar{BA}}{BA} \Rightarrow \frac{F}{BA} = \bar{BA} = \frac{2100}{21} [(4)\bar{i} + (20)\bar{j} + (-5)\bar{k}]$$

$$\therefore F = (400)\bar{i} + (2000)\bar{j} + (-500)\bar{k}$$

$$F_x = 400\text{N}; F_y = 2000\text{N}; F_z = -500\text{N}$$

### Rigid bodies

Equivalent force systems:

- Moment about a force.

External forces

$$\vec{r} \times \vec{F}$$