



**CHG 2314**

**HEAT TRANSFER OPERATIONS**

**MIDTERM EXAM**

**DATE:** Wednesday February 28, 2018, 13:00 – 14:20

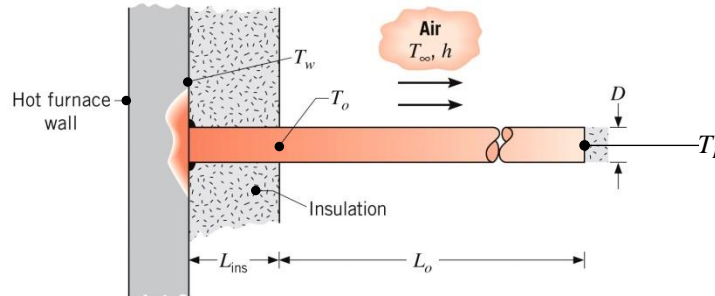
**DURATION:** 80 minutes

**PROFESSOR:** Dr. B. Kruczek

- 1) Closed book examination
- 2) One double-sided reference page with your own notes/information is allowed. Your reference page is to be submitted with the exam booklet; it will be returned to you with the marked exam
- 3) Additional useful information is provided in the Appendix.
- 4) Do 2 out of 3 problems; each problem is worth 25 marks.
- 5) Please indicate which problems should be evaluated; if no indication is provided, the first two problems appearing in the exam booklet will be evaluated.
- 6) Calculator allowed: TI-30X or equivalent
- 7) Cell phones and all other electronic devices must be turned off and stored away from the desk
- 8) If you finish the exam before 14:10, you may leave the room. Otherwise, please wait till the end of the exam

***Good luck!!!***

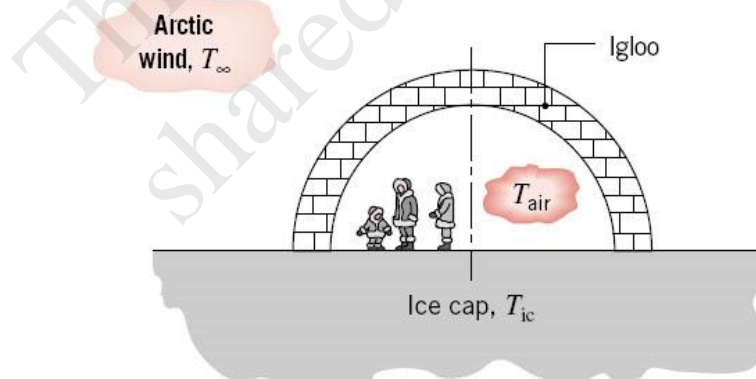
1. A rod of diameter  $D = 30 \text{ mm}$  and thermal conductivity  $k = 80 \text{ W/m K}$  protrudes normally from a furnace wall that is at  $T_w = 200^\circ\text{C}$  and is covered by insulation of thickness  $L_{\text{ins}} = 250 \text{ mm}$ . The rod is welded to the furnace wall and is used as a hanger for supplying instrumentation cables. The exposed length of the rod  $L_o = 400 \text{ mm}$ , and its tip is well insulated. The ambient air temperature is  $T_\infty = 25^\circ\text{C}$ , and the convection coefficient is  $h = 15 \text{ W/m}^2 \text{ K}$ .



- Sketch the thermal circuit of the system assuming that there is no contact resistance between the rod and the furnace wall, and the temperature of the rod at the point of contact with the wall is  $T_w$ . **(5 points)**
- Derive an expression for  $T_o$  (the temperature of the rod at the point it emerges from the insulation) as a function of the prescribed thermal and geometrical parameters. **(5 points)**
- Calculate  $T_o$  from the expression derived in part b). **(7.5 points)**
- Using the value of  $T_o$  calculated in part c), determine  $T_L$ , i.e., the temperature of the rod at the insulated tip. **(7.5 points)**

*Hint:* Assuming perfect insulation, there is a linear temperature profile in the insulated part of the rod of length  $L_{\text{ins}}$ .

2. An igloo is built in a shape of a hemisphere with an inner radius  $r_i = 2.0 \text{ m}$  and walls of compacted snow that are  $t = 0.5 \text{ m}$  thick. On the inside of the igloo the surface heat transfer coefficient is  $h_i = 5 \text{ W/m}^2 \text{ K}$ ; on the outside under normal wind conditions, it is  $h_o = 20 \text{ W/m}^2 \text{ K}$ . The thermal conductivity of the igloo walls and the ice cap on which the igloo sits is the same and equal to  $k = 0.15 \text{ W/m K}$ . The temperature of the ice cap is  $T_{\text{ic}} = -20^\circ\text{C}$  while the temperature of the arctic air outside the igloo is  $T_\infty = -30^\circ\text{C}$ . The occupants of the igloo provide a continuous heat source  $q = 320 \text{ W}$  within the igloo as a result of which the temperature of air in the igloo  $T_{\text{air}}$  is greater than  $T_{\text{ic}}$  and  $T_\infty$ .

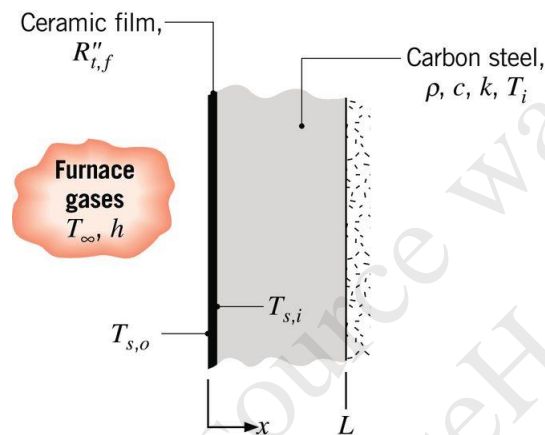


- Please draw the thermal circuit for the above problem. *Hint:* keep in mind that although the temperature of air inside the igloo is uniform and the heat transfer coefficient between the air

- and the igloo's floor is the same as that between air and inside wall of igloo, the floor temperature ( $T_{ic,f}$ ) and the inside wall temperature ( $T_{s,i}$ ) are not necessarily the same. **(10 points)**
- b) Calculate the inside air temperature in the igloo ( $T_{air}$ ) **(15 points)**

*Hint:* Be sure to include heat losses through the floor of the igloo.

3. A plane wall of a furnace is fabricated from plain carbon steel ( $k = 60 \text{ W/m K}$ ,  $\rho = 7850 \text{ kg/m}^3$ ,  $c = 430 \text{ J/kg K}$ ) and thickness  $L = 8 \text{ mm}$ . To protect it from the corrosive effects of the furnace combustion gasses, one surface of the wall is coated with a thin ceramic film that, for a unit surface area, has a thermal resistance of  $R''_{t,f} = 0.01 \text{ m}^2 \text{ K/W}$ . The opposite surface is well insulated from the surroundings.



At furnace start-up the wall is at an initial temperature of  $T_i = 300 \text{ K}$ . and combustion gases at  $T_\infty = 1300 \text{ K}$  enter the furnace, providing a convection coefficient of  $h = 25 \text{ W/m}^2 \text{ K}$  at the ceramic film. You may assume the film to have negligible thermal capacitance (*Hint:* the film can be treated as a contact resistance).

- a) Show that applicability of the LTCM approach is suitable to predict changes of the wall's temperature with time. **(10 points)**
- b) How long would it take for the inner surface of the steel to achieve a temperature of  $T_{s,i} = 1100 \text{ K}$ ? **(10 points)**
- c) What is the temperature  $T_{s,o}$  of the exposed surface of the ceramic film at this time? **(5 points)**

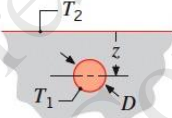
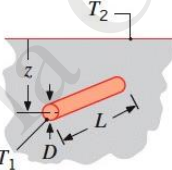
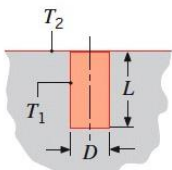
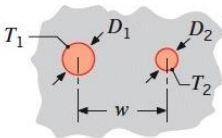
## Appendix

**TABLE 3.4** Temperature distribution and heat loss for fins of uniform cross section

Case	Tip Condition ( $x = L$ )	Temperature Distribution $\theta/\theta_b$	Fin Heat Transfer Rate $q_f$
A	Convection heat transfer: $h\theta(L) = -k d\theta/dx _{x=L}$	$\frac{\cosh m(L-x) + (h/mk) \sinh m(L-x)}{\cosh mL + (h/mk) \sinh mL}$ (3.75)	$M \frac{\sinh mL + (h/mk) \cosh mL}{\cosh mL + (h/mk) \sinh mL}$ (3.77)
B	Adiabatic: $d\theta/dx _{x=L} = 0$	$\frac{\cosh m(L-x)}{\cosh mL}$ (3.80)	$M \tanh mL$ (3.81)
C	Prescribed temperature: $\theta(L) = \theta_L$	$\frac{(\theta_L/\theta_b) \sinh mx + \sinh m(L-x)}{\sinh mL}$ (3.82)	$M \frac{(\cosh mL - \theta_L/\theta_b)}{\sinh mL}$ (3.83)
D	Infinite fin ( $L \rightarrow \infty$ ): $\theta(L) = 0$	$e^{-mx}$ (3.84)	$M$ (3.85)

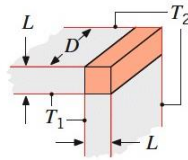
**TABLE 4.1** Conduction shape factors and dimensionless conduction heat rates for selected systems.

(a) Shape factors [ $q = Sk(T_1 - T_2)$ ]

System	Schematic	Restrictions	Shape Factor
<b>Case 1</b> Isothermal sphere buried in a semi-infinite medium		$z > D/2$	$\frac{2\pi D}{1 - D/4z}$
<b>Case 2</b> Horizontal isothermal cylinder of length $L$ buried in a semi-infinite medium		$L \gg D$ $L \gg D$ $z > 3D/2$	$\frac{2\pi L}{\cosh^{-1}(2z/D)}$ $\frac{2\pi L}{\ln(4z/D)}$
<b>Case 3</b> Vertical cylinder in a semi-infinite medium		$L \gg D$	$\frac{2\pi L}{\ln(4L/D)}$
<b>Case 4</b> Conduction between two cylinders of length $L$ in infinite medium		$L \gg D_1, D_2$ $L \gg w$	$\frac{2\pi L}{\cosh^{-1}\left(\frac{4w^2 - D_1^2 - D_2^2}{2D_1 D_2}\right)}$

**Case 8**

Conduction through the edge of adjoining walls

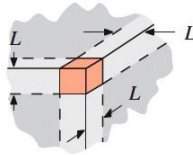


$$D > 5L$$

$$0.54D$$

**Case 9**

Conduction through corner of three walls with a temperature difference  $\Delta T_{1-2}$  across the walls

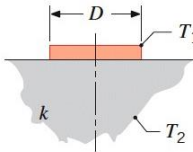


$$L \ll \text{length and width of wall}$$

$$0.15L$$

**Case 10**

Disk of diameter  $D$  and temperature  $T_1$  on a semi-infinite medium of thermal conductivity  $k$  and temperature  $T_2$

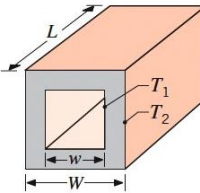


None

$$2D$$

**Case 11**

Square channel of length  $L$



$$\frac{W}{w} < 1.4$$

$$\frac{2\pi L}{0.785 \ln(W/w)}$$

$$\frac{W}{w} > 1.4$$

$$\frac{2\pi L}{0.930 \ln(W/w) - 0.050}$$

$$L \gg W$$