

# GEOMETRIC DESIGN (Ch. 2)

## Rectilinear Motion

$$v = at + v_0$$

$$\frac{1}{2}(v^2 - v_0^2) = a(x - x_0)$$

$$x = \frac{1}{2}at^2 + v_0t + x_0$$

## Breaking Distance

$$\left(\frac{W}{g}\right)a + Wf \cos \alpha + W \sin \alpha = 0$$

$$a = (v^2 - v_0^2) \frac{\cos \alpha}{2D_b} \quad G = \tan \alpha$$

$$D_b = x \cos \alpha \quad D_b = \frac{v_0^2 - v^2}{2g(f + G)}$$

$f = 0.6$  DRY  
 $f = 0.3$  WET

## Curvilinear Motion

$$a_n = \frac{v^2}{\rho} \quad \sum F_n = \frac{mv^2}{\rho}$$

$$e + f_s = \frac{v^2}{gR} (1 - f_s e)$$

$$e = \tan \beta \rightarrow \text{minimum angle}$$

$$e f_s = 0 \text{ for typical highway}$$

## Lateral Displacement

$$l = a \cot \theta \quad \frac{dl}{dt} = -v$$

$$\frac{dl}{dt} = -a \csc^2 \theta \frac{d\theta}{dt}$$

$$\csc^2 \theta = \frac{a^2 + l^2}{a^2} \quad a \text{ is lateral separation}$$

$$\frac{d\theta}{dt} = \frac{va}{a^2 + l^2}$$

## Dilemma Zone

distance to clear intersection

$$T_{min} = \delta_2 + \frac{v_0}{2a_2} + \frac{w+l}{v_0}$$

min amber for  $x_0 = x_c$

For successful stopping

$$x - v_0 \delta_2 \geq \frac{v_0^2}{2a_2}$$

$x_c = v_0 \delta_2 + \frac{v_0^2}{2a_2}$

$D_b @ a_2$   $\uparrow$  min dist. to stop comfortably

$$a_1 = \frac{2x}{(\tau - \delta_1)^2} + \frac{2(w+l - v_0 \tau)}{(\tau - \delta_1)^2}$$

$\uparrow a$  to clear intersection

$$x_0 = v_0 \tau - (w+l)$$

$\uparrow \text{max } x$  to clear w/o accel.

### Design Radius

$$e + f_s = \frac{v^2}{gR} \quad R_{min} = \frac{v^2}{g(e_{max} + f_{smax})}$$

$\frac{m}{hr}$  & ft; imperial:  $g=15$   
 $\frac{km}{hr}$  & m; metric:  $g=127$

$$e_{des} = \frac{v^2}{gR} - f_s \quad R > R_{min}$$

## Horizontal Alignment

$$D = \frac{180A}{\pi R} \quad \sin\left(\frac{D}{2}\right) = \frac{A}{2R}$$

highway railway

- 1-degree of curve  $L = 2\pi R \left(\frac{\Delta}{360}\right)$
- 2-intersecting angle  $L = \frac{A\Delta}{D}$
- 3-external distance  $T = R \tan\left(\frac{\Delta}{2}\right)$
- 1-middle ordinate  $E = R \left(\sec\left(\frac{\Delta}{2}\right) - 1\right)$
- 7-tangent length  $M = R \left(1 - \cos\left(\frac{\Delta}{2}\right)\right)$
- L-curve length  $LC = 2R \sin\left(\frac{\Delta}{2}\right)$
- LC-long chord  $PC = PI - T$   
 $PT = PC + L$

## Vertical Alignment

$$A = G_2 - G_1 (\%)$$

$$K = \frac{L}{|A|}$$

$$E = \frac{AL}{800}$$

$$x = \frac{LG_1}{G_1 - G_2} (x \geq 0)$$

$$y = 4E \left(\frac{x}{L}\right)^2 \begin{matrix} (+) \text{- sag} \\ (-) \text{- crest} \end{matrix}$$

$$P_{elev} = \left[ VPC_{elev} + \left(\frac{G_1}{100}\right)x \right] + y$$

## Stopping Sight Distance

horiz:  $\theta = \frac{90SSD}{\pi R}$   $C = R(1 - \cos \theta)$   $SSD = v_0 \delta + D_b$   
 $h_1 = 1.05m (35ft)$   
 $h_2 = 0.6m (2ft)$

crest:  $L = \frac{|A|SSD^2}{200(\sqrt{h_1} + \sqrt{h_2})^2} (SSD \leq L)$   
 $L = 2SSD - \frac{200(\sqrt{h_1} + \sqrt{h_2})^2}{|A|} (SSD \geq L)$

sag:  $L = \frac{|A|SSD^2}{200(h + S \tan \beta)} (SSD \leq L)$   $h = 0.6m (2ft)$   $\beta = 1^\circ$   
 $L = 2SSD - \frac{200(h + S \tan \beta)}{|A|} (SSD \geq L)$

$S > L$  impractical

## Passing Sight Distance

$$d_1 = 1.47t_1 \left[ v_{avg} m + \frac{at_1}{2} \right]$$

$$d_2 = 1.47vt_2 \quad \uparrow \Delta v \text{ vehicles}$$

$$d_3 = 100 \approx 300 \text{ ft}$$

$$d_4 = \frac{2}{3} d_2$$

super-elevation runoff is from when adverse crown is removed to full super-elevation

agent runoff is from the normal crown to when adverse crown is removed

$$L_m = 1.60934 \text{ km}$$

$$L_m = 3.28084 \text{ ft}$$

$$1 \frac{m}{s} = 3.6 \frac{km}{hr}$$

$$1 \frac{m}{hr} = 0.44704 \frac{m}{s}$$

$$L_m = 5280 \text{ ft}$$

## Vertical Curves

- 1) Find  $L_{min}$
- 2) Find  $VPI_{sta}$  &  $VPI_{elev}$
- 3) Find  $VPC_{sta}$  &  $VPT_{sta}$
- 4) Compute offsets (y) [1<sup>st</sup> whole sta then +1 sta]
- 5) Compute elevations
- 6) Location & elev of high/low point

# TRAFFIC STREAM FLOW MODELS (Ch. 3)

Spacing

$$x_L = \frac{v^2}{2d_L}$$

$$x_f = v\delta + \frac{v^2}{2d_f}$$

$$x_f = S + x_L - NL - x_0$$

$$S = v\delta + \frac{v^2}{2d_f} - \frac{v^2}{2d_L} + NL + x_0$$

d - deceleration

$x_0$  - safety margin

L - car length

N - # vehicles in train

$$s = \frac{1}{k}$$

$$h = \frac{\text{constant} + S}{\text{constant } v}$$

↑ time headway

$$h = \frac{1}{q}$$

$$u_t = \frac{1}{N} \sum_{i=1}^N v_i \rightarrow \text{time mean speed (spot speeds)}$$

$$t_i = \frac{D}{v_i} \quad u_s = \frac{D}{t_{ave}} = \frac{1}{\frac{1}{N} \sum_{i=1}^N \frac{1}{v_i}}$$

↑ space mean speed (avg time)

when  $\frac{dq}{dk} = 0$ , it's  $q_{max}$  when  $u=0$ , it's  $K_j$

Fundamental Eqn

$$h = \frac{S}{u} = t \quad h = \frac{1}{q}$$

$$S = \frac{1}{k} = hu \quad \frac{1}{q} u = \frac{1}{k}$$

$$q = uk$$

$q$  = flow (veh/h)

$u$  = speed (dist./s)

$k$  = concentration (veh/dist.)

Shockwave

$$u_{sw} = \frac{q_b - q_a}{k_b - k_a}$$

(+) - direction of flow  
(-) - opposite of flow  
 $\phi$  - stationary

rate of growth of platoon =  $u_{sw_1} - u_{sw_2}$

- platoon = (rate)(time)

Moving Observer

$$q = \frac{N_o}{T}$$

Stationary obs. moving vehicle

$$N_p = kVT$$

(stationary traffic) (moving observer)  
↑ observer speed

$$M = M_o - M_p = qT - kVT$$

moving observer in traffic

From two tests (w-with; a-against)

$$\frac{M_w}{T_w} = q - kV_w \quad \frac{M_a}{T_a} = q + kV_a \quad V_w T_w = V_a T_a = L$$

$$q = \frac{M_w + M_a}{T_w + T_a} \quad u = \frac{L}{T_w - \frac{M_w}{q}}$$

space mean speed

$$T_{ave} = T_w - \frac{M_w}{q} = \frac{L}{u}$$

$$k = \frac{q}{u}$$

-  $M_w$ :  $T_{ave} > T_w$   
+  $M_w$ :  $T_{ave} < T_w$   
 $\phi M_w$ :  $T_{ave} = T_w$

Fundamental Graphs (y-x)

$u-k$ : inversely proportional

$u-q$ : sideways parabola

$q-k$ : parabola?

$K_j$  is when  $u = \phi$

$q_{max}$  is at  $u_{max}$  &  $\frac{dq}{dk} = \phi$

# CAPACITY & LEVEL OF SERVICE (Ch. 7)

Freeway is N=2  
Two-lane is N=1  
highway

## Capacity & LOS Analysis

- 1) FFS, S, D, LOS
- 2)  $v_p$ , S, D, LOS

### Determining FFS

\*not adjusted if field\*

$$FFS = BFFS - f_{LW} - f_{LC} - f_N - f_{ID}$$

110 (urban) lane ↑ lat. ↑ # ↑ Interchange density  
120 (rural) width clear. lanes density (∅ rural)

$$\text{Interchange density} = \frac{1}{\text{interchange spacing}}$$

- $f_{LW}$  TABLE 2
- $f_{LC}$  TABLE 3
- $f_N$  TABLE 4
- $f_{ID}$  TABLE 5

### Determining Flow Rate

$$v_p = \frac{V \leftarrow \text{volume}}{\text{Peak hour factor}}$$

PHF N fHV fP  
↑ heavy driver ↑ change driver  
veh. pop.

$$PHF = \frac{V}{V_{15(4)}} \text{ Turban } \downarrow \text{ rural}$$

$$f_{HV} = \frac{1}{1 + P_T(ET-1) + P_R(ER-1)}$$

\*RVs treated as if level\*  
\*on downgrade\*

### Determining LOS

1) Given  $v_p$  & FFS; Find S FIGURE 1

↳ For  $90 < FFS \leq 120$  &  $(3100 - 15FFS) < v_p \leq (1800 + 5FFS)$

$$S = FFS - \left[ \frac{1}{28} (23FFS - 1800) \left( \frac{v_p + 15FFS - 3100}{20FFS - 1300} \right)^2 \right]^0.6$$

↳ For  $90 < FFS \leq 120$  &  $v_p \leq (3100 - 15FFS)$

$$S = FFS$$

- ext. seg. fHV TABLE 6
- upgrade fHV TABLE 7
- upgrade fHV TABLE 8
- downgrade fHV TABLE 9

2) Calculate density

$$D = \frac{v_p \text{ pc/hr/ln}}{S \text{ km/hr}}$$

3) Determine LOS TABLE 1

## TWO-LANE HIGHWAYS

- Class I: long ATS & PTSF  
- Class II: local PTSF

### Capacity

1700 pc/hr/direction  
(3200 for both direct.)

### FFS CLASS I

\*field: only adjust if >200 pc/hr

$$FFS = S_{FM} + 0.0125 \frac{v_f \leftarrow \text{veh/hr}}{f_{HV}}$$

↑ mean traffic speed  
estimating

$$FFS = BFFS - f_{LS} - f_A \rightarrow \text{BOTH SIDES}$$

↑ lane & shoulder  
↑ access pts  
may be posted limit

### Flow rate (I & II)

$$v_p = \frac{v}{PHF f_G f_{HV}}$$

\*iteration required\*

- 1) set  $v_p = \frac{v}{PHF}$
- 2) Calc new  $v_p$  w adj.
- 3) Check if same adj.
- 4) Repeat until same

### ATS CLASS I

$$ATS = FFS - 0.0125 v_p - f_{np}$$

↑ no passing zone

### PTSF (I & II)

$$PTSF = BPTSF + f_{d/np}$$

$$BPTSF = 100 [1 - e^{-0.000879 v_p}] FFS f_{LS}$$

LOS (I) TABLE 1

LOS (II) TABLE 2

FFS  $f_{LS}$  TABLE 3

FFS  $f_A$  TABLE 4

ATS  $f_G$  TABLE 5a

PTSF  $f_G$  TABLE 5b

ATS  $f_{HV}$  TABLE 6a

PTSF  $f_{HV}$  TABLE 6b

ATS  $f_{np}$  TABLE 7a

PTSF  $f_{d/np}$  TABLE 7b

## METHOD FOR LOS

- 1) calculate FFS
- 2) Calculate  $v_p$
- 3) Calculate PTSF
- 4) Calculate ATS (Class I)
- 5) Find LOS

\* if 2-way  $v_p > 3200$  pc/hr - LOS F  
\* if  $v_p$  \* directional split > 1700 pc/hr - LOS F

# PAVEMENT DESIGN (Ch. 5)

$$M_r = \frac{\Delta(\sigma_1 - \sigma_3)}{\epsilon_{1,r}}$$

Standard Axle  
↳ 80 kN (18000 lb)

\* traffic load is determined in terms of # of repeated 80 kN single-axle loads applied to pavement on two sets of dual tires \*

## ESAL

$$\text{Traffic factor} = \frac{\sum \text{ESAL}}{\# \text{ vehicles}}$$

$$\text{ESAL} = (\# \text{ axles}) (\text{load eq. factor})$$

$$\text{ESAL}_i = f_d G_{jt} \text{AADT}_i (365) N_i F_{E_i}$$

$$\text{ESAL} = \sum \text{ESAL}_i$$

↳ truck factors

$$\text{ESAL}_i = \text{AADT}_i (365) f_i G_{jt} f_d$$

$f_d$  - design lane factor

$G_{jt}$  - growth factor

$\text{AADT}_i$  - 1<sup>st</sup> year annual avg daily traffic

$N$  - # axles per vehicle

$F_{E_i}$  - load equivalency factor

## FLEXIBLE PAVEMENT DESIGN

Surface - mineral agg. & asphalt - prevents water penetration - distributes load, resists abrasion - varies 3-6 in

Granular base - crushed stone, gravel, sand & slag - distributes stress - foundation to surface - protects surface against volume change

Subbase - granular material - can be excluded if subgrade is good - reduces stress applied in subgrade - water drainage - protects base against vol change

Subgrade - natural materials - foundation of structure

- avoid overloading subgrade
- avoid overloading all layers
- maintain good serviceability along pavement design life
- usually 20 years

$$\text{PSI} = 5.03 \cdot \log(1 + SV) - 1.38 (RD)^2 - 0.01 (C + P)^{1/2}$$

↙ slope variance ↘ rut depth ↙ cracking patching ↘

## AASHTO design method

$$\text{SN} = a_1 D_1 + a_2 D_2 m_2 + a_3 D_3 m_3$$

$m$  - drainage coefficient

$a_1, a_2, a_3$  - layer coefficients (surface, base, subbase)

$D$  - thickness

↳ can be converted to thickness

## HOW TO USE FIGURE 1

- 1) Draw line joining  $R$  &  $S_0$ , extend to first  $T_L$
- 2) Draw line from  $T_L$  to ESAL, extend to second  $T_L$
- 3) Draw line from  $T_{L2}$  to  $M_r$ , extend to graph
- 4) Interpolate SN

$S_0$   
Flexible (0.40 - 0.5)  
Rigid (0.3 - 0.4)

initial serviceability = 4.5  
terminal serviceability = 2.5

- 1) Determine total ESAL for period
- 2) Determine design serviceability loss  $\Delta \text{PSI} = P_i - P_e$
- 3) Determine effective  $M_r$  (subgrade),  $M_r$  (subbase & base) and layer coefficients ( $a_1, a_2, a_3$ )
- 4) Determine drainage coefficients ( $m_2$  &  $m_3$ )
- 5) Select reliability ( $R$ ) & overall standard deviation ( $S_0$ )
- 6) Read SN from FIGURE 1
- 7) Calculate  $D$

At Step (7)

→ use  $M_r$  of base for  $\text{SN}_1$

→ use  $M_r$  of subbase for  $\text{SN}_2$

→ use  $M_r$  of subgrade for  $\text{SN}_3$

At Step (2)

For subgrade

$$\left. \begin{aligned} M_r &= 1500 \text{ CBR } (\text{lb/in}^2) \\ M_r &= 220 \text{ CBR } (\text{kN/m}^2) \end{aligned} \right\} \begin{array}{l} \text{Fine-grained} \\ \text{soils w/} \\ \text{CBR} \leq 10 \end{array}$$

$$\left. \begin{aligned} M_r &= 1000 + 55.5R \frac{\text{lb}}{\text{in}^2} \\ M_r &= 145 + 80.4R \frac{\text{kN}}{\text{m}^2} \end{aligned} \right\} \begin{array}{l} \text{for} \\ R \leq 20 \end{array}$$