

Given:  
 $I_s = 3A$   
 $P_i = 6W$

$I_x = gV_1$   
 $g = 2A/V$   
 $V_o = 5V$

Find  $P_o$

Steps:

① Find  $V_1$

$$P_i = I_s V_1 \Rightarrow \frac{P_i}{I_s} = V_1$$

$$V_1 = \frac{6W}{3A} = 2V$$

② Find  $I_x$

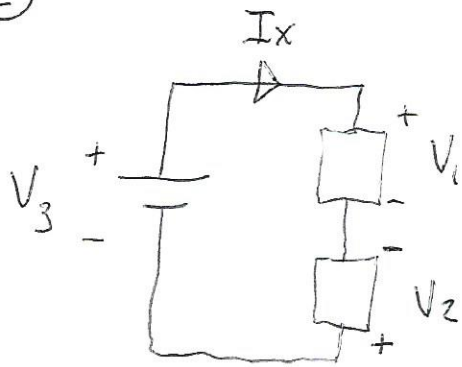
$$I_x = gV_1$$

$$I_x = (2A/V)(2V) \\ = 4A$$

③ Find  $P_o$

$$P_o = I_x V_o \\ = (4A)(5V) \\ = 20W$$

2)



Given:

$$P_3 = -8W \quad I_x = 5mA$$

$$P_1 = 3W$$

Find  $V_1, V_2, V_3$

a) Find  $P_2$

$$P_1 + P_2 + P_3 = 0$$

$$\begin{aligned} P_2 &= -P_1 - P_3 \\ &= 8W - 3W \\ &= 5W \end{aligned}$$

b) Find  $V_1, V_2, V_3$

$$V_1 = \frac{P_1}{I_x} = \frac{3W}{5mA} = \frac{3}{5} kV = 0.6 kV$$

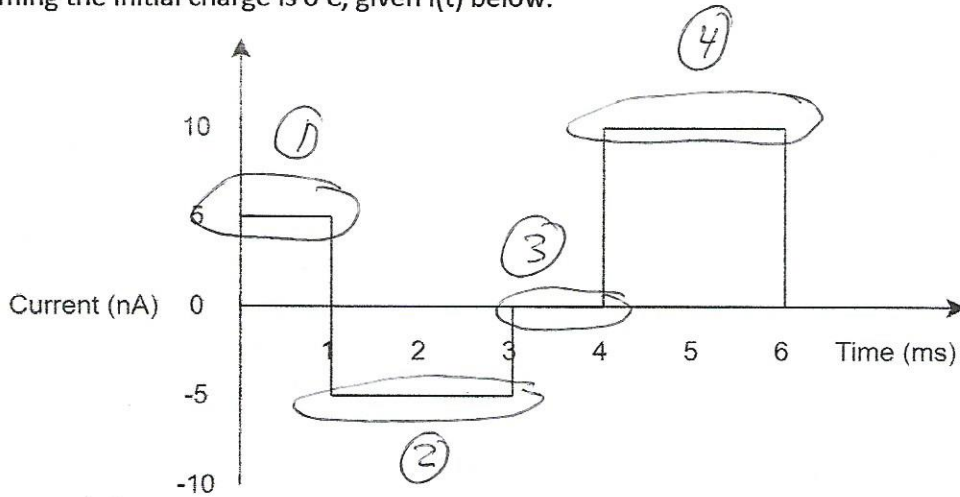
$$V_2 = -\frac{P_2}{I_x} = -\frac{5W}{5mA} = -1 kV$$

$$V_3 = \frac{P_3}{I_x} = -\left(\frac{-8W}{5mA}\right) = 1.6 kV$$

3

$$q_0 = 0 \text{ C}$$

Plot  $q(t)$ , assuming the initial charge is 0 C, given  $i(t)$  below:

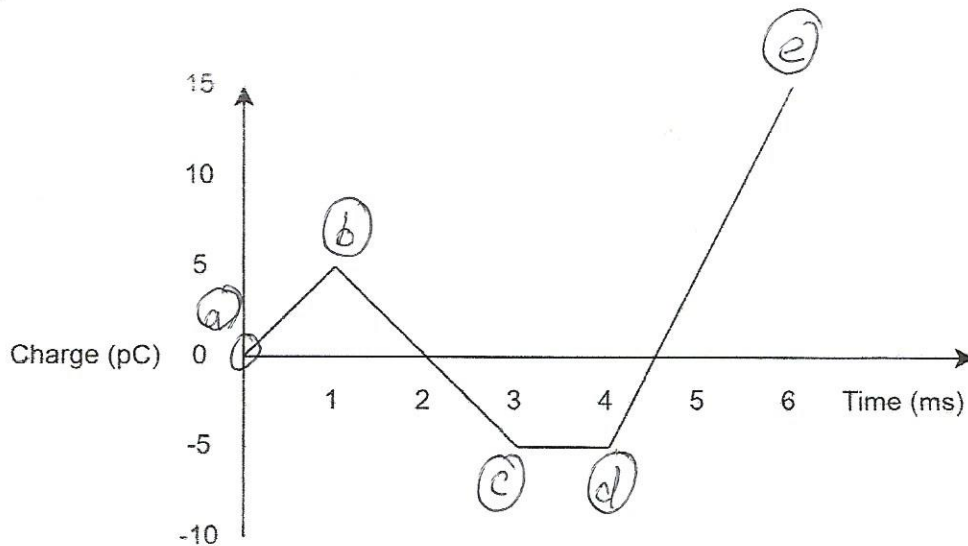


$$\begin{aligned} \textcircled{1} \quad q_b &= q_a + I_1(\Delta t_1) \\ &= 0 + (5 \text{ nA})(1 \text{ ms}) \\ &= 5 \text{ pC} \end{aligned}$$

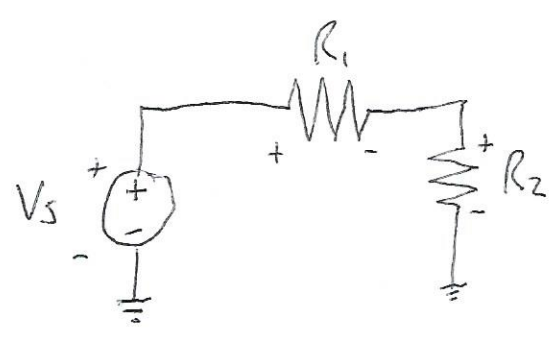
$$\begin{aligned} \textcircled{3} \quad q_d &= q_c + I_3(\Delta t_3) \\ &= -5 \text{ pC} + 0(1 \text{ ms}) \\ &= -5 \text{ pC} \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad q_c &= q_b + I_2(\Delta t_2) \\ &= 5 \text{ pC} + (-5 \text{ nA})(2 \text{ ms}) \\ &= -5 \text{ pC} \end{aligned}$$

$$\begin{aligned} \textcircled{4} \quad q_e &= q_d + I_4(\Delta t_4) \\ &= -5 \text{ pC} + (10 \text{ nA})(2 \text{ ms}) \\ &= 15 \text{ pC} \end{aligned}$$



4)



Given:  
 $V_s = 5V$   
 $P_2 = 5W$   
 $R_1 = R_2 = R$

Find  $I_x$  &

9) Find  $V_1, V_2$

KVL:

$$V_1 + V_2 - V_s = 0$$

We know:  $I_1 = I_2 = I_x$  and  $R_1 = R_2$

$$\therefore V_1 = I_1 R_1 = I_x R_2 = V_2 \quad \text{or} \quad V_1 = V_2$$

sub into KVL:

$$V_1 + V_1 = V_s$$

$$V_1 = \frac{1}{2} V_s = 2.5V$$

$$V_2 = 2.5V$$

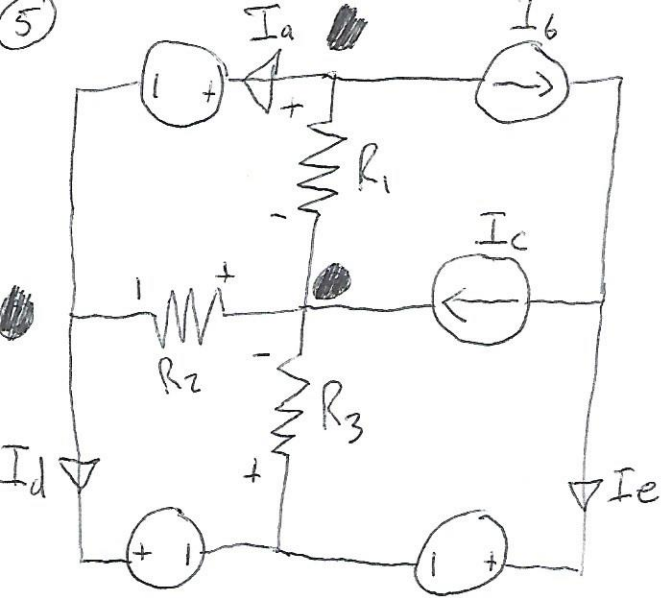
10) Find  $I_x$

$$I_x = \frac{P_2}{V_2} = \frac{5W}{2.5V} = 2A$$

11) Find  $R$

$$V_1 = I_x R$$

$$R = \frac{V_1}{I_x} = \frac{2.5V}{2A} = 1.25 \Omega$$



Given:

$$V_2 = 4V$$

$$I_c = 7A$$

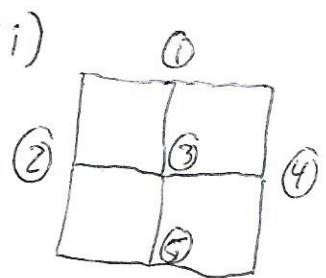
$$I_d = 3A$$

$$I_e = 2A$$

$$R_2 = 2\Omega$$

- Find:
- i) # of branches, nodes, and independent loops.
  - ii) KCL equation for each node
  - iii)  $I_1, I_2, I_3, I_a, I_b$

branches = 8      loops = 4      check:  $6 = 8 + 5 - 1$        $\therefore LHS = RHS \checkmark$   
 nodes = 5       $8 = 4 + 5 - 1 = 8$



①  $0 = -I_a - I_b - I_1$

④  $0 = I_b - I_c - I_e$

②  $0 = I_a + I_2 - I_d$

⑤  $0 = I_d - I_3 + I_e$

③  $0 = I_1 - I_2 + I_c + I_3$

\* Assuming PSC and current entering nodes are +ve

iii) Find  $I_2$

$$I_2 = \frac{V_2}{R_2} = \frac{4V}{2\Omega} = 2A$$

Find  $I_b$

Eq. ④

$$I_b = I_c + I_e = 9A$$

→ Find  $I_3$

Eq. ⑤

$$I_3 = I_d + I_e = 5A$$

Find  $I_a$

Eq. ②

$$I_a = I_d - I_2 = 1A$$

→ Find  $I_1$

Eq. ①

$$I_1 = -I_a - I_b = -10A$$

check:

Eq. ③

$$0 = (-10A) - 2A + 7A + 5A$$

$$0 = 0 \quad \therefore LHS = RHS \checkmark$$