

• For  $n(S)$ : There are 10000 possible outcomes for her 1<sup>st</sup> guess, and then 9999 possible outcomes for her 2<sup>nd</sup> guess. So,  
 $n(S) = 10000 \times 9999 = 99\,990\,000$

\* Here we treat (1111, 2222) and (2222, 1111) as two different outcomes.

• For  $n(A)$ : To have  $A$  occur, Jasmine needs to get the correct PIN in either her 1<sup>st</sup> or 2<sup>nd</sup> guess. In either case, there are 9999 possible outcomes in the guess which does not get the correct PIN. So,  
 $n(A) = 9999 \times 2 = 19\,998$ .

$$\therefore P(A) = \frac{n(A)}{n(S)} = \frac{19\,998}{99\,990\,000} = 0.0002 = 0.02\%$$

\* Example 5  $\rightarrow$  There are 7 girls and 3 boys in a classroom. A teacher needs 2 volunteers to help with the lab setup. She randomly selects 2 students from the class. What is the probability that she gets 1 girl and 1 boy?

- Random experiment: Select 2 students from the class.
- Sample space:  $S = \{\text{any 2 students of the class}\}$
- Event:  $A = \{\text{get 1 girl and 1 boy}\}$

• For  $n(S)$ : There are 10 possible choices for picking one student, and then 9 possible choices for picking another.

$\rightarrow$  One may claim that  $n(S) = 10 \times 9 = 90$ , but this way one treats (Stud A, Stud B) and (Stud B, Stud A) as two different outcomes.

$\therefore$  if order does not matter, we have

$$n(S) = \frac{10 \times 9}{2} = 45$$

• For  $n(A)$ : To have  $A$  occur, the teacher needs to select 1 out of 3 boys and 1 out of 7 girls. So,

$$n(A) = 7 \times 3 = 21$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{21}{45} = \frac{7}{15} \approx 46.67\%$$