

* Example 2 → There are two bags of balls. Tom randomly picks one ball from each bag. What is the probability that he does not get a white ball?

Bag A → 1 white ball and 2 black balls (w_1, B_1, B_2)

Bag B → 1 white ball and 1 black ball (w_2, B_3)

- Random experiment: Pick one ball from each of the two bags.
- Sample Space: $S = \{w_1w_2, w_1B_3, B_1w_2, B_1B_3, B_2w_2, B_2B_3\}$
Note $n(S) = 6$
- Event: $A = \{\text{get no white ball}\} = \{B_1B_3, B_2B_3\}$
Note $n(A) = 2$

$$\therefore P(A) = \frac{n(A)}{n(S)} = \frac{2}{6} = \frac{1}{3}$$

* Example 3 → Jasmine forget her 4-digit number (e.g. 1234). The system allows her to try only once. What is the probability for her to log into the system?

- Random experiment: Guess an unknown PIN with 1 attempt
- Sample space: $S = \{0000, 0001, \dots, 9998, 9999\}$
- Event: $A = \{\text{get the correct PIN}\} = \{1234\}$

$$P(A) = \frac{n(A)}{n(S)} = \frac{1}{10^4} = 0.0001 = 0.1\%$$

Example 3 → The system allows her to try twice. What is the probability for her to log into the system?

- Random experiment: Guess an unknown PIN with 2 attempts.
- Sample space: $S = \{(xxxx, xxxxx)\}$
- Event: $A = \{(1234, xxxxx)\}, \{(xxxx, 1234)\}$

$$P(A) = \frac{n(A)}{n(S)} = ?$$