



CHG 2314

January 14, 2019

Quiz 1 - Solution

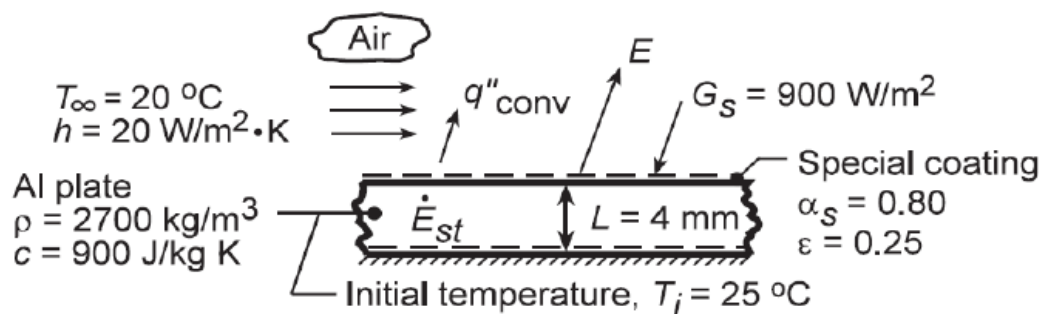
An aluminum plate 4 mm thick is mounted in a horizontal position, and its bottom surface is well insulated. A special, thin coating is applied to the top surface such that it absorbs 80% of any incident solar radiation, while having an emissivity of 0.25. The density  $\rho$  and specific heat  $c$  of aluminum are known to be 2700 kg/m<sup>3</sup> and 900 J/kg · K, respectively.

Consider conditions for which the plate is at a temperature of 25°C and its top surface is suddenly exposed to ambient air at  $T_\infty = 20^\circ\text{C}$  and to solar radiation that provides an incident flux of 900 W/m<sup>2</sup>. The convection heat transfer coefficient between the surface and the air is  $h = 20 \text{ W/m}^2 \cdot \text{K}$ . What is the initial rate of change of the plate temperature?

**Hint 1:** In your analysis, use a unit surface area of the plate of 1 m<sup>2</sup>.

**Hint 2:** Since  $T_{sur}$  is not given, assume  $T_{sur} = 0 \text{ K}$ .

**SCHEMATIC:**



**ASSUMPTIONS:** (1) Negligible end effects, (2) Uniform plate temperature at any instant, (3) Constant properties, (4) Adiabatic bottom surface, (5) Negligible radiation from surroundings, (6) No internal heat generation.

**ANALYSIS:** (a) Applying an energy balance, Eq. 1.12c, at an instant of time to a control volume about the plate,  $\dot{E}_{in} - \dot{E}_{out} = \dot{E}_{st}$ , it follows for a unit surface area.

$$\alpha_S G_S (1 \text{ m}^2) - E (1 \text{ m}^2) - q''_{conv} (1 \text{ m}^2) = (d/dt)(McT) = \rho (1 \text{ m}^2 \times L) c (dT/dt).$$

Rearranging and substituting from Eqs. 1.3 and 1.7, we obtain

$$dT/dt = (1/\rho Lc) [\alpha_S G_S - \epsilon \sigma T_1^4 - h(T_1 - T_\infty)].$$

$$dT/dt = (2700 \text{ kg/m}^3 \times 0.004 \text{ m} \times 900 \text{ J/kg} \cdot \text{K})^{-1} \times$$

$$[0.8 \times 900 \text{ W/m}^2 - 0.25 \times 5.67 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4 (298 \text{ K})^4 - 20 \text{ W/m}^2 \cdot \text{K} (25 - 20)^\circ \text{C}]$$

$$dT/dt = 0.052^\circ \text{C/s}.$$

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