

# CH: Measurements.

1. Initial observation:
2. Research study
3. Measure behaviour
4. Evaluate findings.

- Temporal precedence:  $Y \rightarrow X$ .
- Experimental Control:  $Z \rightarrow X$ .
- Statistics: not-Random.

## Population vs Sample:

- Population: all members of well-defined Group.  
→ Parameter: characteristic of population.
- Sample: subset of population.  
→ Statistic: characteristic of Sample.

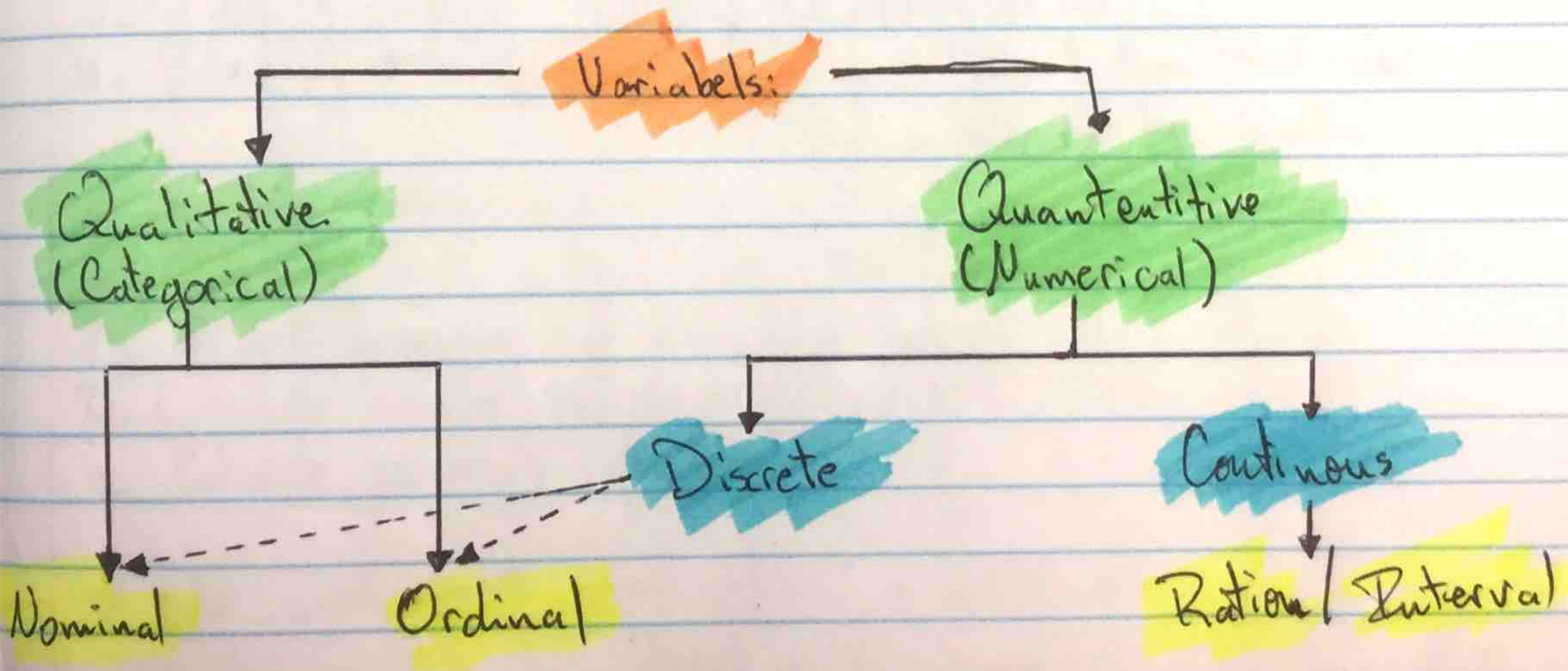
## Sampling:

- Random: equal chance of all members of population of being selected.
- Bias: not all members have equal chance.
- Sampling Error: difference between sample stats and population parameter.

## Variables:

Characteristics observed to take different values.

Constants: take only a single value.



Dichotomous: one of two values.

properties of measurements:

Order larger better?	} Difference Subtract Meaningful?	} Ratio: divide Meaningful?
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Nominal

Ordinal

Interval

Ratio

- equal along Category  
- mutually exclusive.

- Rank  
- differences between  
Ranks are meaningless

- Rank & difference  
- No absolute zero  
- No Ratios.

- Rank & difference  
- Absolute zero  
- Ratios

Reliable: Same measurement under Same Conditions.

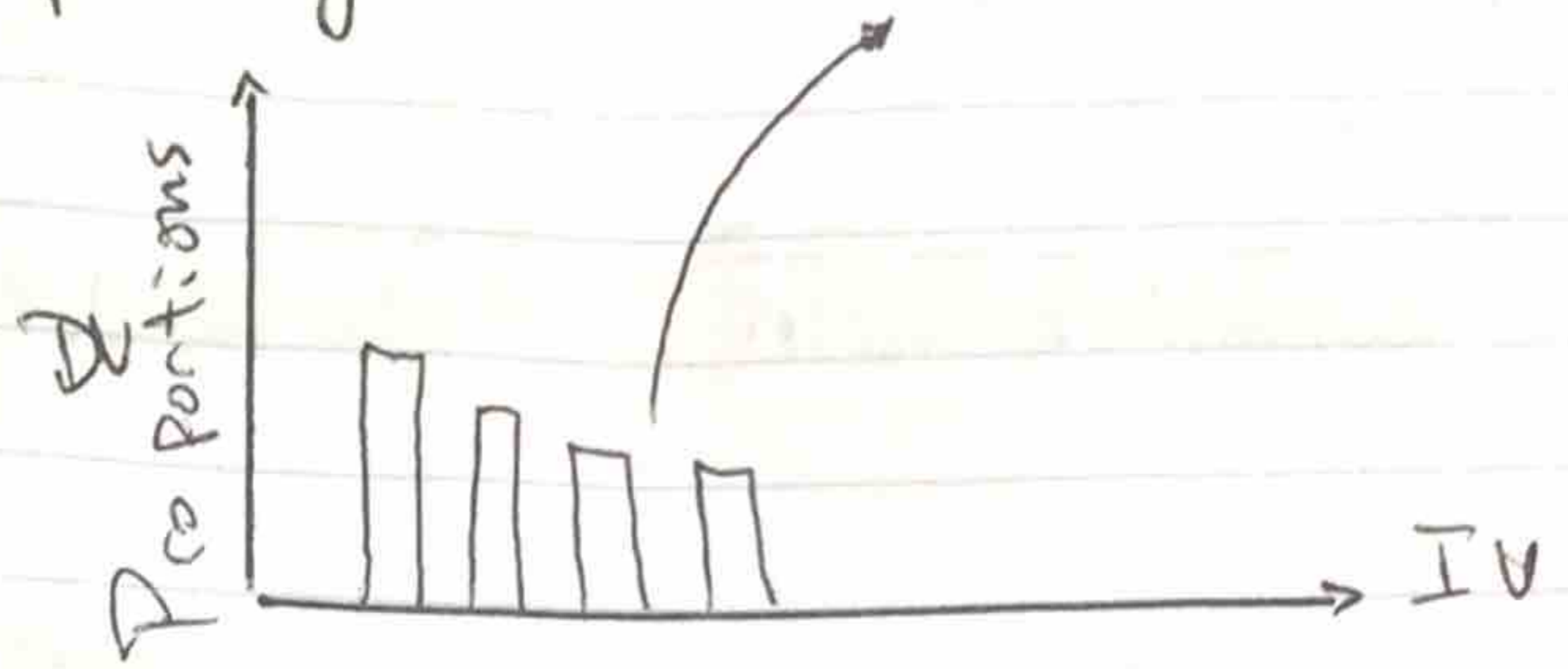
Valid: Measuring what it says it measures.

## Ch2: Frequency and Probability:

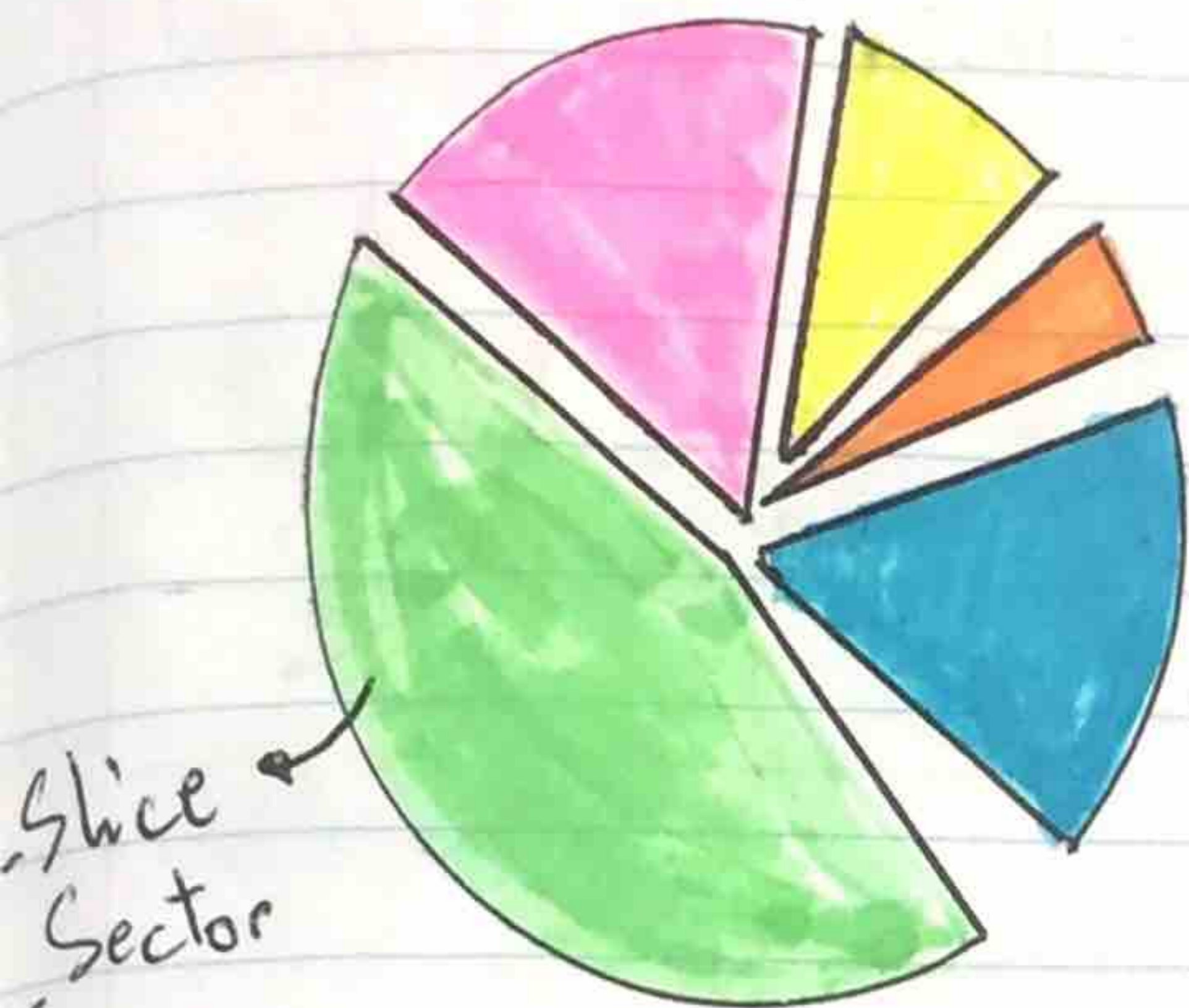
Constant width

Proportion:

$$P = f/N$$



Categories



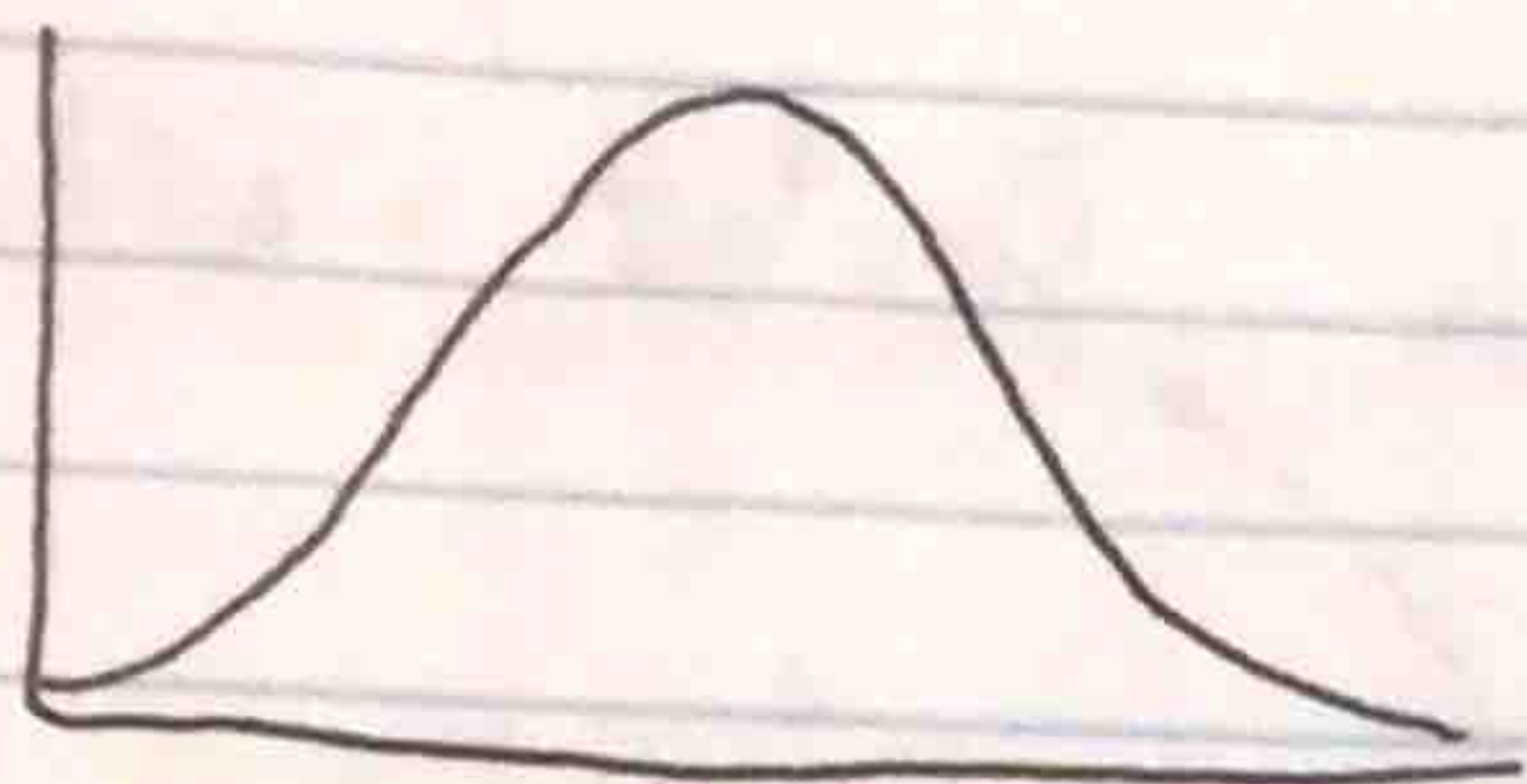
- all Slices add up to (100%)
- best for nominal & ordinal.

Cumulative proportion

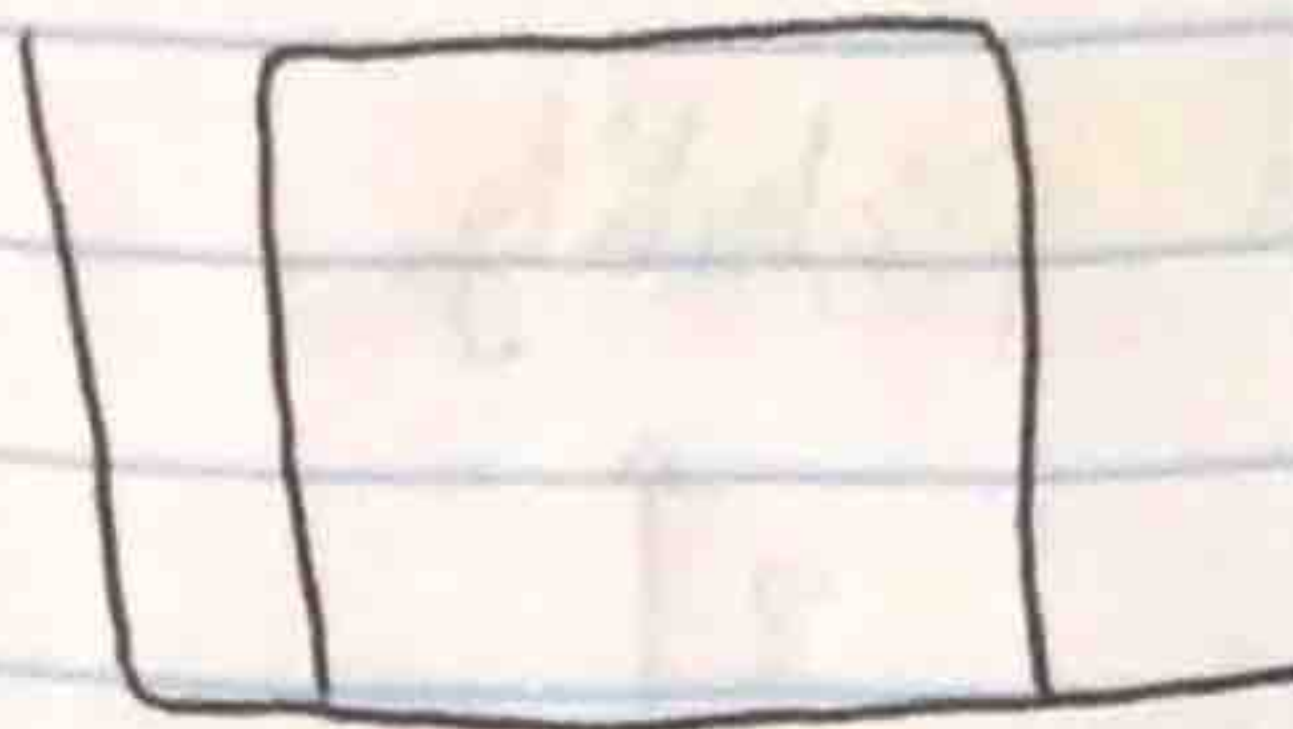
$$P = \frac{\text{Cumulative } f}{n}$$

1. Determine lowest & highest
2. Identify Range = (Highest - lowest) + 1
3. Identify width = Range / # of Interval desired
4. Identify lowest Interval value.   
 → lowest than lowest value.   
 → divisible by width.
5. Identify class label
6. Identify real limits (-0.01, +0.99)
7. Count frequencies of every Interval.
8. Calculate relative frequency (proportion)
9. Calculate percentage (p. %)

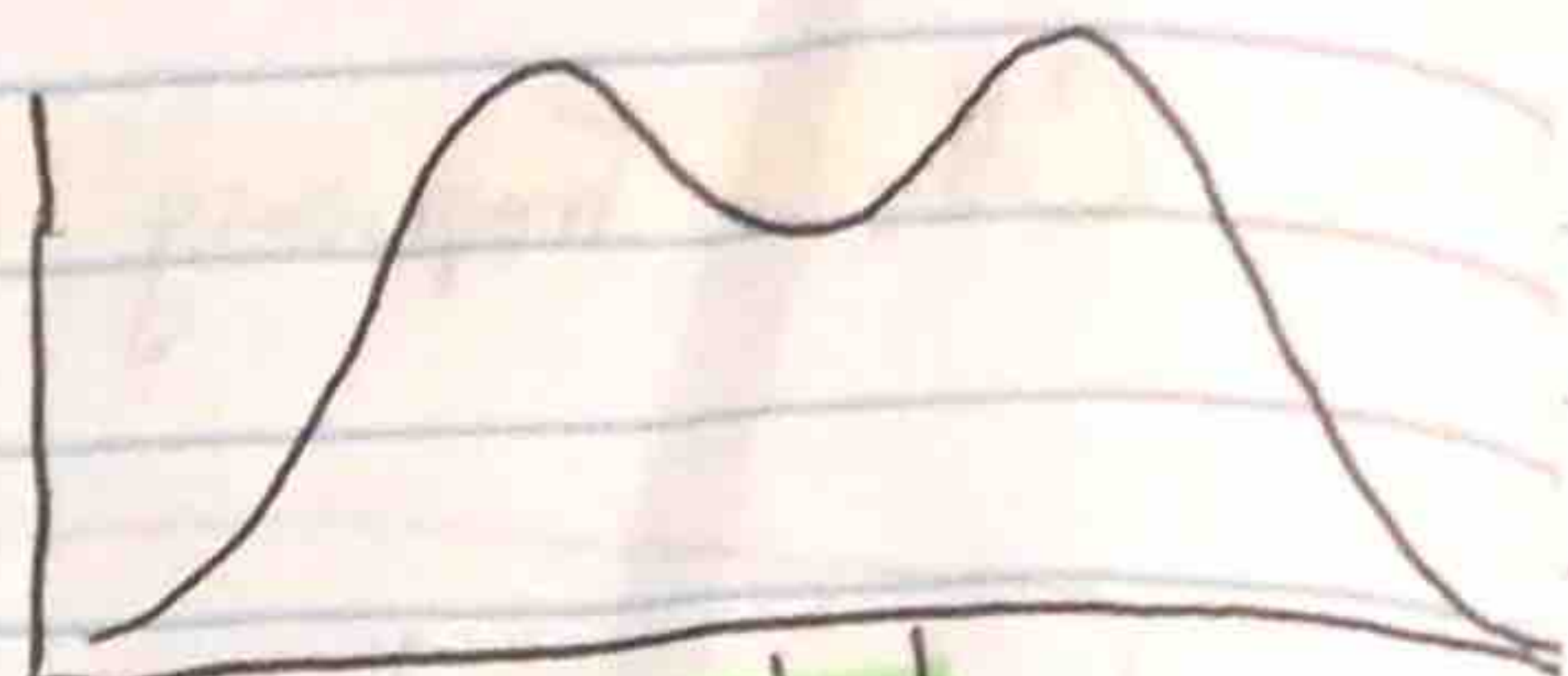
\* add limit point up or down (be consistent).



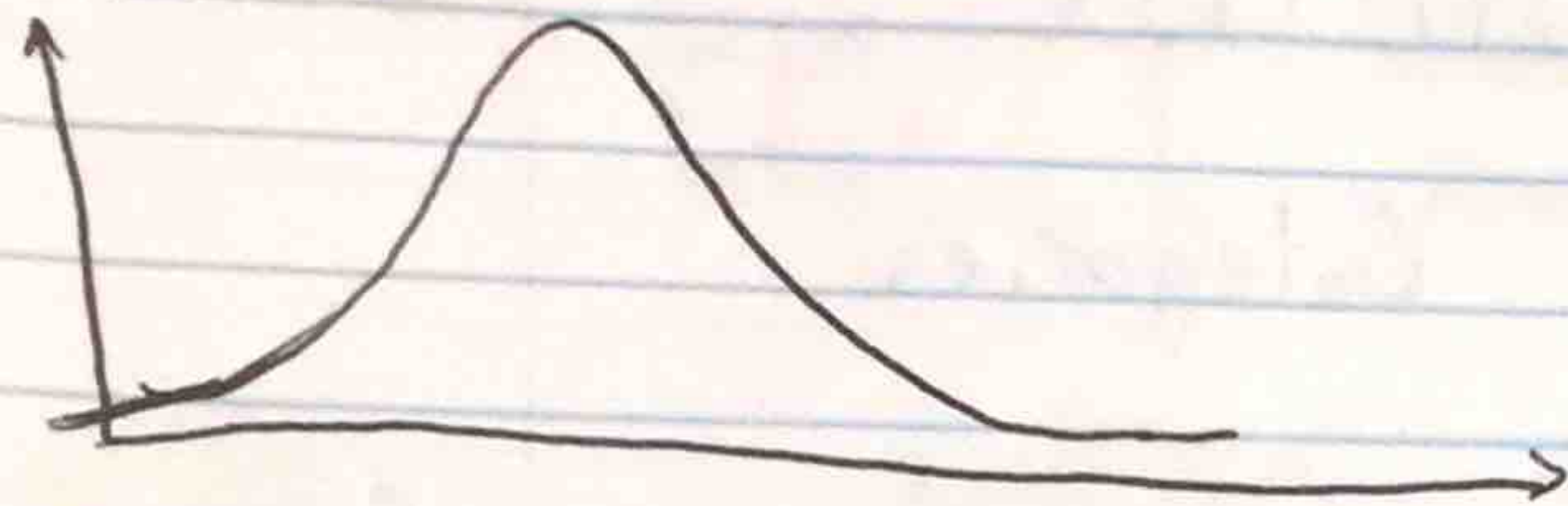
normal / unimodal



Rectangular

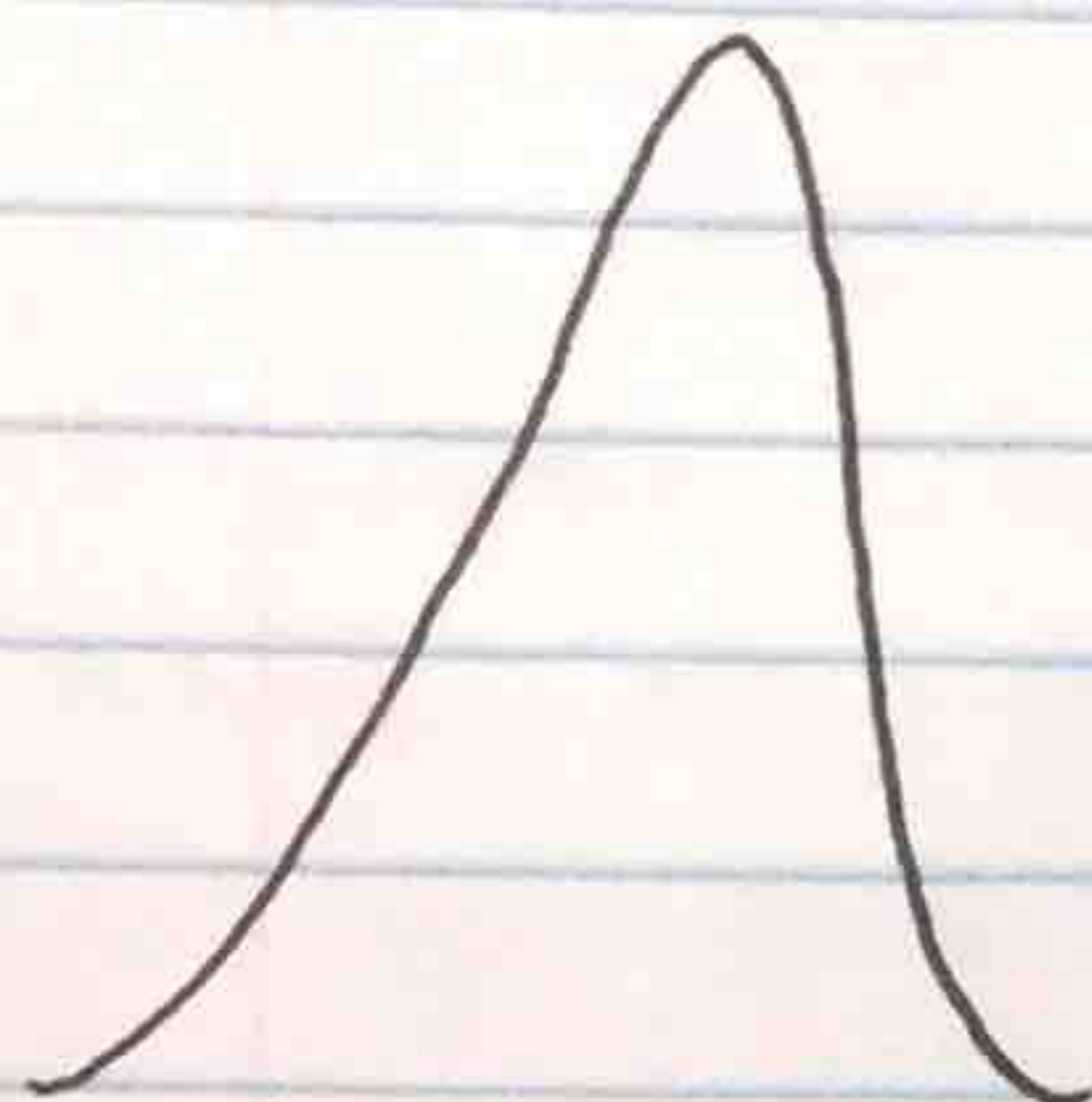
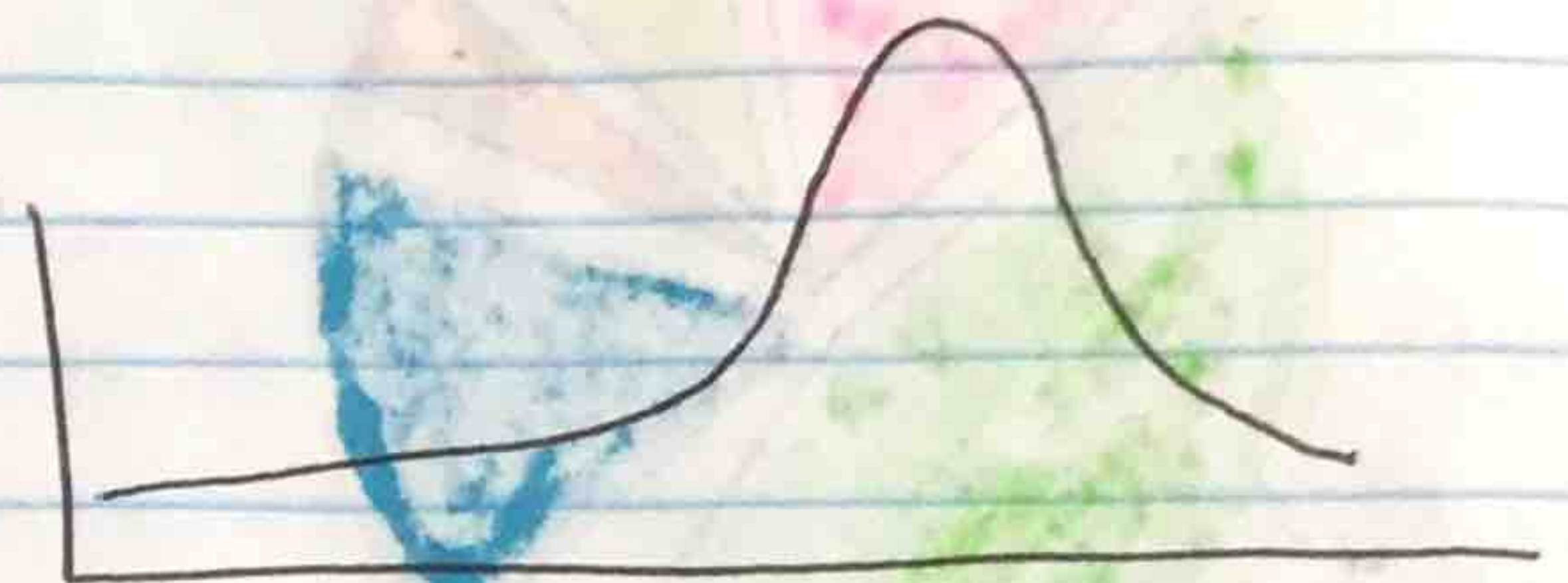


bimodal



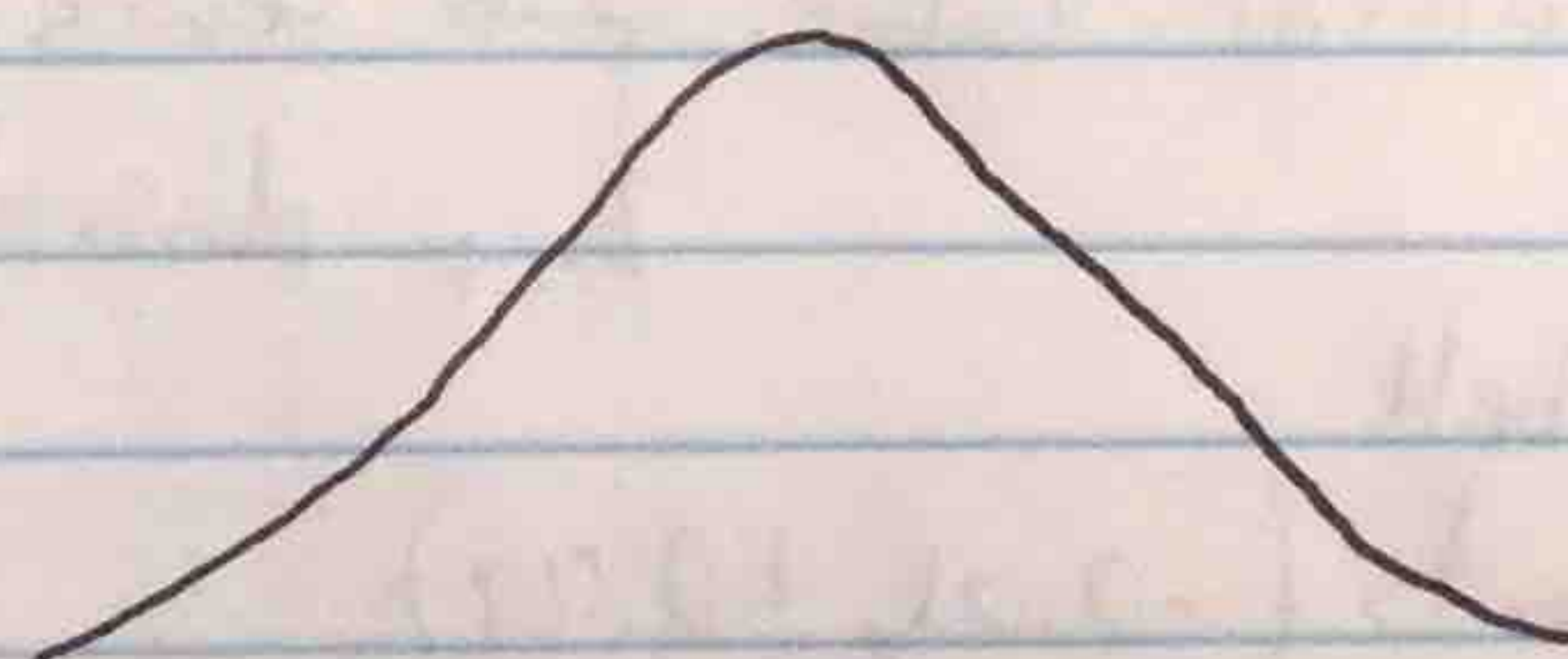
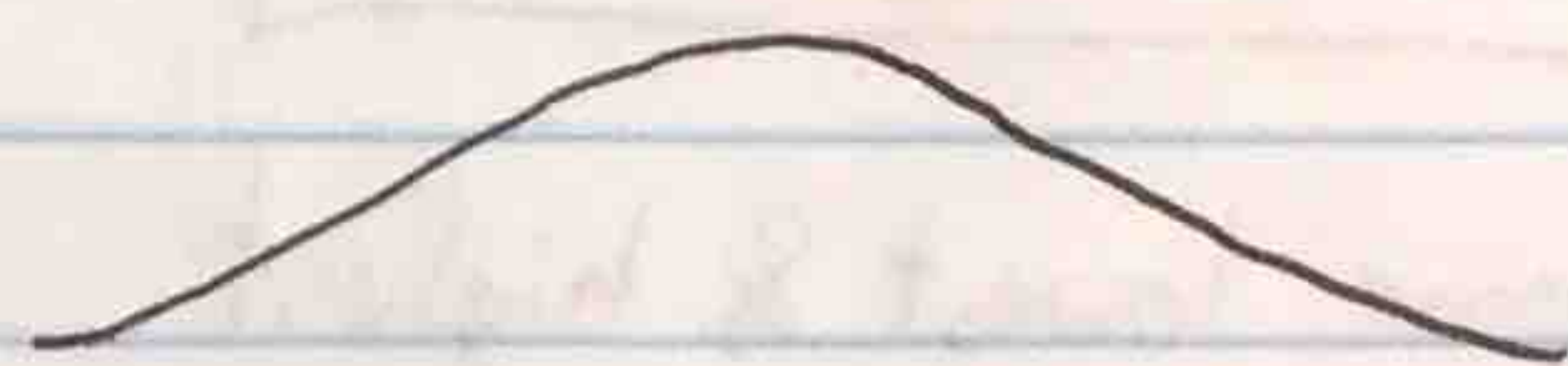
• Positive skew  
- floor effect

• Negative skew  
- Ceiling effect



• leptokurtic (Positive kurtosis)  
- pile up narrowly

• platykurtic (Negative)  
- relatively flat



Mesokurtic (No kurtosis)

# CH3: Central Tendency.

## Mean:

$$\mu = \frac{\sum X}{N}$$

population

$$M(\bar{x}) = \frac{\sum x}{n}$$

Sample.

Weighted Mean:  $M_w = \frac{\sum (M \cdot n)}{\sum n}$

Weighted Sum

Combined n

- Function for every score / Unique Value / stable /
- Influence by extreme scores (Interval & Ratio only /

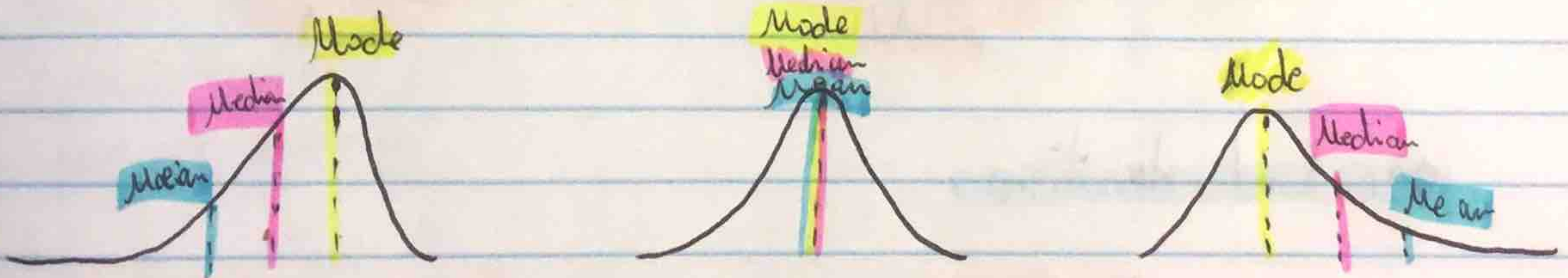
## Median:

- Not influence by extreme / Unique Value /
- Not function of all scores / Not stable / every thing except nominal.

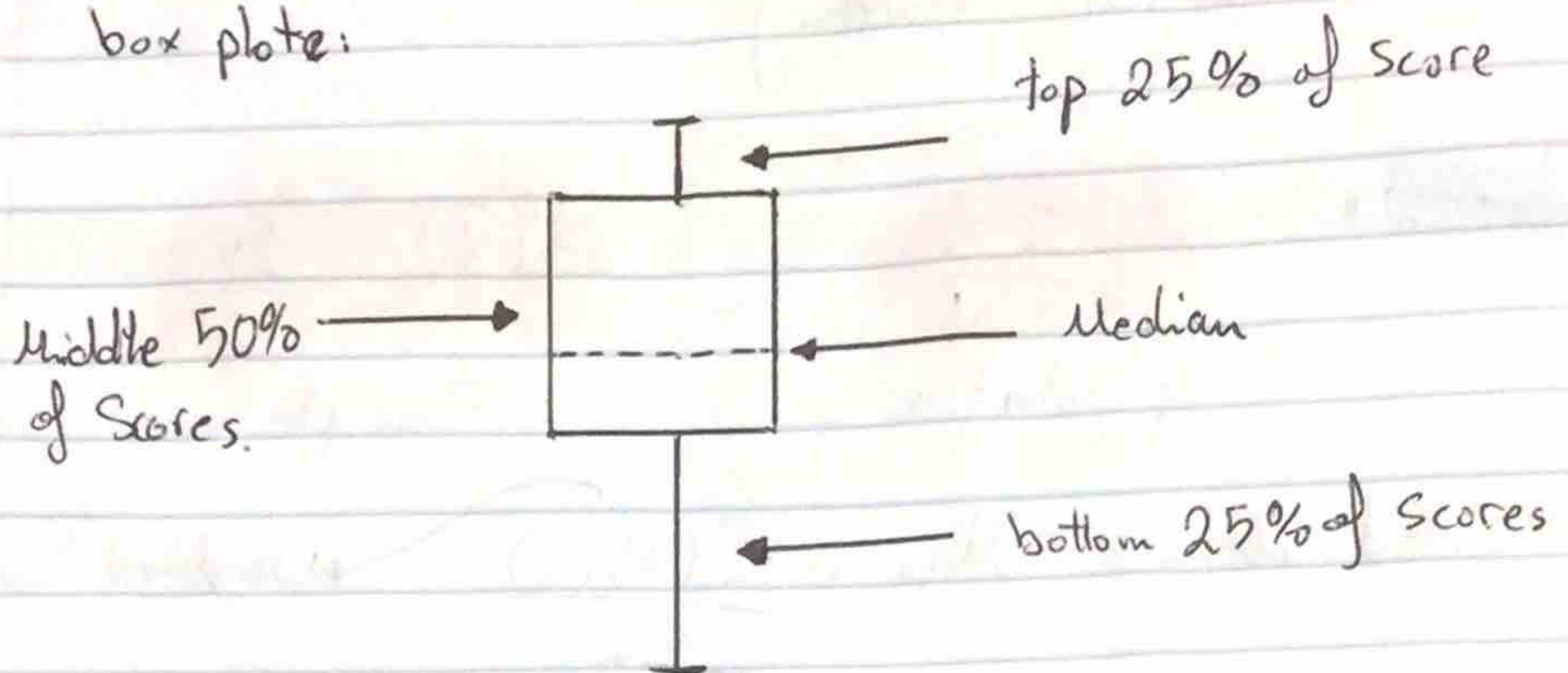
## Mode:

- Simple to obtain (all scales /
- Not Unique / not function of scores / not stable.

on graphs:  $\Rightarrow$  Mode  $\rightarrow$  Median  $\rightarrow$  Mean.      negative  
Mean  $\rightarrow$  Median  $\rightarrow$  Mode      positive  
Median, Mode, Mean      normal



box plots:



Variability:

Range = highest - lowest.

- Simple / Alternative / ordinal, Interval, and Ratio
- Influenced by extreme scores / function of 2 scores / Not stable

Deviation Score:

$$\frac{X - M}{\sum (X - M) = 0}$$

Sum of squares:

$$SS = \sum (X - M)^2$$

Variance:

$$\sigma^2 = \frac{\sum (X - M)^2}{N}$$

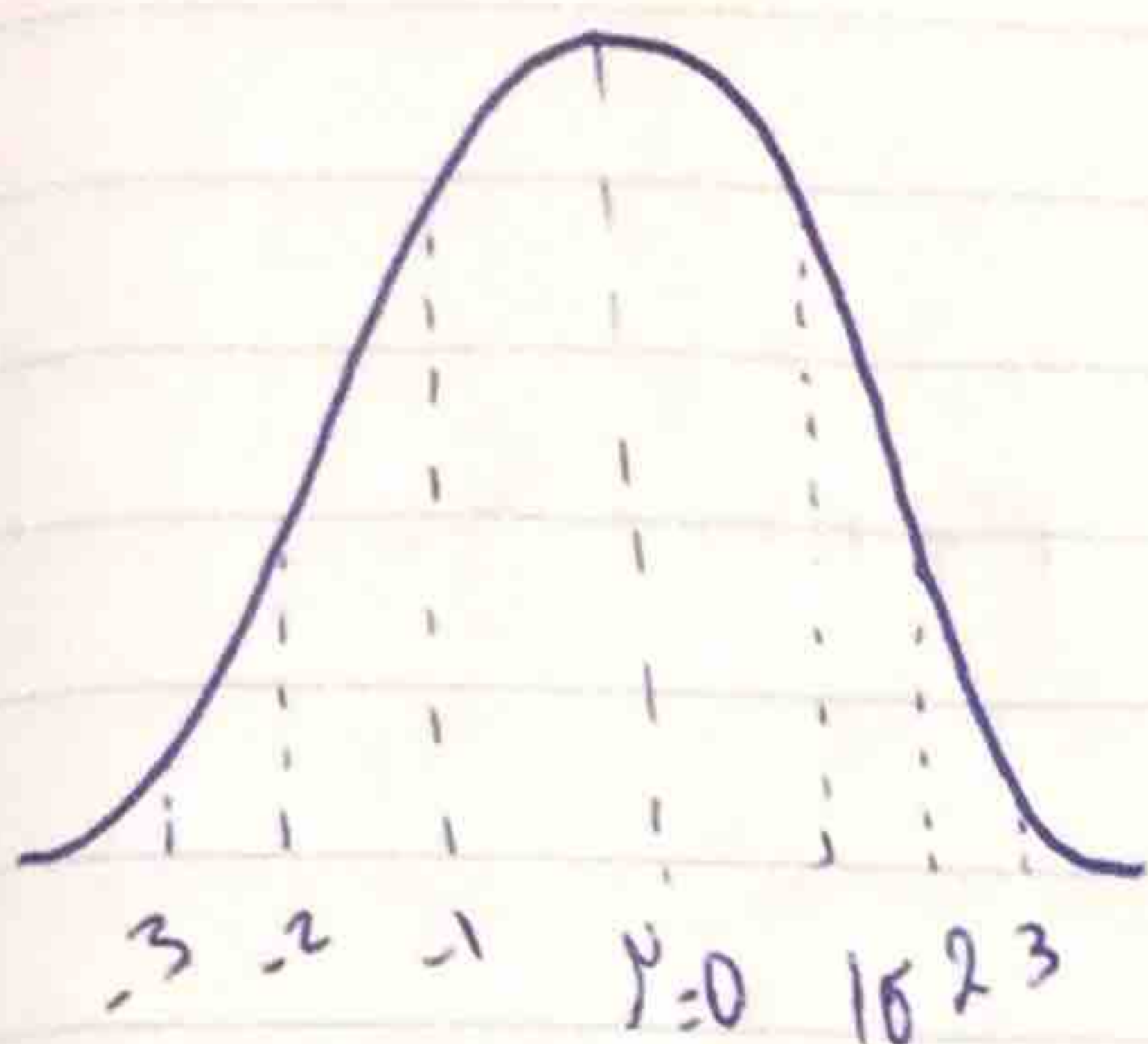
$$S^2 = \frac{\sum (X - M)^2}{n - 1}$$

standard deviation:

$$\sigma = \sqrt{\frac{\sum (X - M)^2}{N}}$$

$$S = \sqrt{\frac{\sum (X - M)^2}{n - 1}}$$

## CH4: Normal Distribution:



0	→	1/-1	⇒	0.3413
-1/1	→	-2/2	⇒	0.1359
-2/2	→	-3/3	⇒	0.0215
-3/3	→	-∞/∞	⇒	0.0013

Z-Score: when normal distribution = Convert to Z-scores and Compare.

$$Z = \left( \frac{x - \mu}{\sigma} \right)$$

$$X = Z \cdot \sigma + \mu$$

### Rules:

1.  $P(z)$  = the probability that a randomly chosen score will be less than  $z$ .
2.  $1 - P(z)$  = the probability that a randomly chosen score will be greater than  $z$ .
3.  $P(z_2) - P(z_1) =$  " " " " " " between  $z_1$  &  $z_2$  ( $z_2 > z_1$ )
4.  $1 - [P(z_2) - P(z_1)] =$  " " " " " " outside  $z_1$  &  $z_2$  ( $z_2 > z_1$ )

to find  $Z_{\alpha/2}$  given  $\alpha$ :

$$(1 - \alpha) 100\%$$

- Find  $\alpha/2$

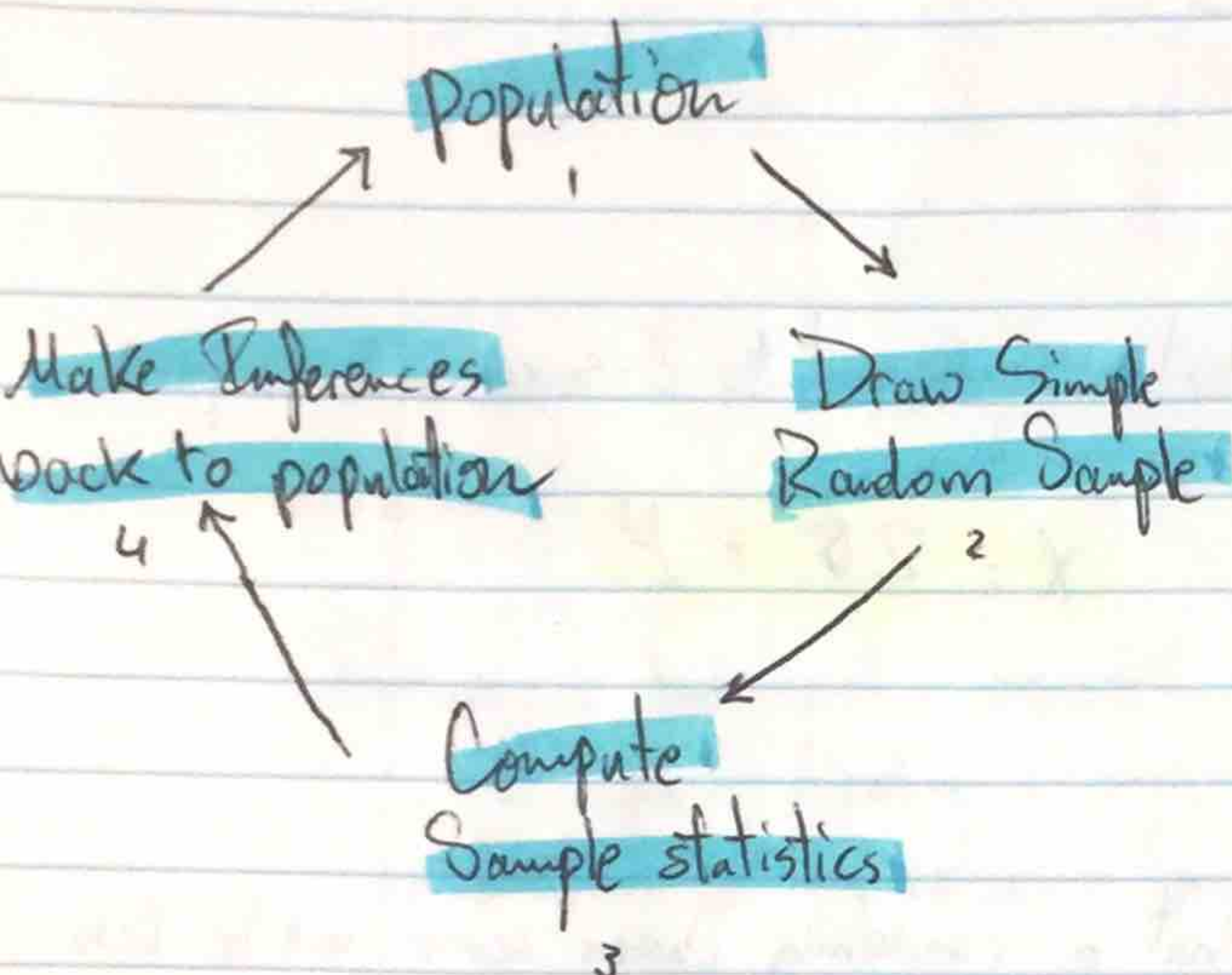
- Find Z-score of  $\alpha/2$

- Absolute Value

## CHs: Sampling Distributions:

Random Sampling:

- Ideal / widely used / difficult.  
Equal & Independent probability.



Convenience Sampling:

- Not Ideal (Biased) / limits generalizability (Dangers of volunteer samples (Self-Selection) / worse if Sample Size is small.

→ Replication as a Solution.

~~the~~ Duplication of results in a different context or with different characteristics.

~~the~~ Sampling with Replacement  
put back into  
sample population

Sampling without Replacement  
not put back into  
population.

# of Sample means =  $N^n$

# of Sample means  $< N^n$

## Distribution of means:

- plot of means of samples obtained from a population
- will follow a normal distribution (unimodal).
- Constant Sample Size

→ Population Mean ( $\mu$ ) = Sampling Distribution Mean ( $\mu'$ )

→ standard ~~deviation~~ error → standard deviation

$$SEM(\sigma_m) = \frac{s}{\sqrt{n}} \rightarrow \text{Sample Size}$$

\* larger Sample Size will lead to less variability. ( $\approx 30$ )

$$SEM(\sigma_m) = \frac{\sigma}{\sqrt{n}} \rightarrow \text{Standard deviation of population}$$