

**MIDTERM
 EXAMINATION**

Instructions:

- Answer ALL questions on the questionnaire.
- This is a close-book examination.
- Use the provided space to answer the following questions. For your calculations you can use pages 6-8.
- Calculators are not allowed.
- Read all the questions before you start.

Q1. The range of signed integers N expressed in *2's complement representation* that can be stored in a 10-bit register is: 1 point

- (a) $-1024 \leq N \leq +1023$ (b) $-1023 \leq N \leq +1024$ (c) $-512 \leq N \leq +511$ (d) $-511 \leq N \leq +512$
 (e) None of the above

Q2. Identify the decimal number which is represented next in floating point with the IEEE 754 standard: 11000010100010101100000000000000 1.5 points

- (a) $(-133.375)_{10}$ (b) $(-69.375)_{10}$ (c) $(-138.750)_{10}$ (d) $(-34.6875)_{10}$ (e) $(-8.671875)_{10}$

Q3) Give the best binary approximation of $A = (26.6)_{10}$ and $B = -(23.4)_{10}$ employing *signed 2's-complement representation* with 2 bits for the fractional part. 1.5 points

A = _____ B = _____

Q4) 1) Convert to decimal the following two numbers, 01010 & 10101, which are already expressed in 2's complement representation. 1 point

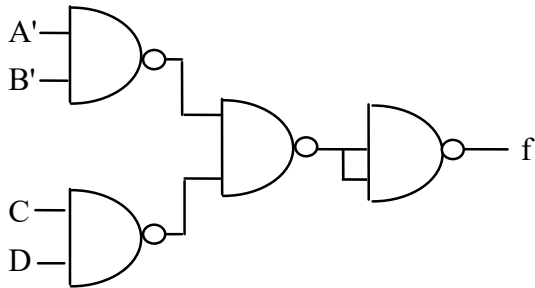
- 2) These numbers are stored in two 6-bit registers X and Y to calculate their sum ($S = X + Y$) and their difference ($D = X - Y$) by using additions and 2's complementation only. Convert to decimal and write each intermediate and final result, to check the correctness of your assertions. 1.5 points

<u>S = X + Y</u>	<u>2's complement</u>	<u>Base 10</u>	<u>D = X - Y</u>	<u>2's complement</u>	<u>Base 10</u>
CY:			CY:		
X +			X +		
<u>Y</u>			<u>-Y</u>		
S		_____	D		_____

3) Since both S and D have to be represented with 6 bits, indicate if overflow occurs, and explain how a circuit can detect these situations. 1 point

Q5. Which of the logic functions is implemented by the following circuit?

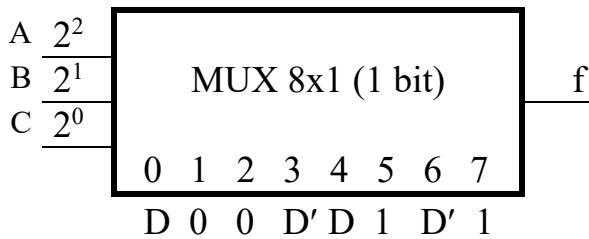
1.5 points



- (a) $f(A,B,C,D) = \Sigma m(4,5,6,7,8,9,10) + X(12,13,14,15)$
- (b) $f(A,B,C,D) = \Sigma m(4,5,6,8,9,10,14)$
- (c) $f(A,B,C,D) = \Sigma m(0,1,2,3,6,7,14,15)$
- (d) $f(A,B,C,D) = \Sigma m(0,1,2,3,7,11,15)$
- (e) $f(A,B,C,D) = \Sigma m(4,5,6,8,9,10,12,13,14) + X(7,11)$

Q6. Which of the following logic functions is implemented by the given circuit?

1.5 points



- (a) $f(A,B,C,D) = \Sigma m(2,5,9,10,11,12,13,15)$
- (b) $f(A,B,C,D) = \Sigma m(0,7,8,10,11,13,14,15)$
- (c) $f(A,B,C,D) = \Sigma m(3,4,9,10,11,12,13,15)$
- (d) $f(A,B,C,D) = \Sigma m(3,5,6,7,8,12,13,15)$
- (e) $f(A,B,C,D) = \Sigma m(1,6,9,10,11,12,14,15)$

Q7. What is the capacity of a ROM, capable to implement three functions of six variables?

1.5 points

- (a) 8 words of 6 bits
- (b) 16 words of 3 bits
- (c) 32 words of 6 bits
- (d) 64 words of 3 bits
- (e) None of the above

Draw a block diagram of your memory with the major components, indicating its inputs and outputs.

Q8.

1) - Draw the state diagram of the sequential circuit whose state table is given below

The State Diagram goes here:

Present State	Next state	JA	KA	JB	KB	JC	KC
0 0 0	1 0 0						
0 0 1	1 1 0						
0 1 0	0 0 1						
1 0 0	0 1 0						
1 1 0	0 0 0						

1.5 points

- Fill out the above table with the appropriate values for the JK flip-flops inputs such that the sequential circuit will observe the required transitions.

1.5 points

- Indicate the correct set of minimized equations of the JK flip-flops inputs from the following:

2 points

- (a) $J_A = A'B'$, $K_A = C'$, $J_B = AB'C' + A'B'C$, $K_B = BC'$, $J_C = A'BC$, $K_C = A'B'C$.
- (b) $J_A = A'B'$, $K_A = 1$, $J_B = A+C$, $K_B = 1$, $J_C = A'B$, $K_C = 1$.
- (c) $J_A = B'$, $K_A = 1$, $J_B = A+C$, $K_B = 1$, $J_C = A'B$, $K_C = 1$.
- (d) $J_A = A'B'$, $K_A = A$, $J_B = AC$, $K_B = C'$, $J_C = A'BC$, $K_C = A'$.
- (e) $J_A = B'$, $K_A = A$, $J_B = AC$, $K_B = C'$, $J_C = A'BC$, $K_C = A'$.

2) - If your circuit reaches by mistake any of the 3 states that are not used, determine their corresponding next state.

1.5 points

Present state	Next State

- Is your circuit auto-corrective? Reply just with YES or NO

Draw the time diagram and give the states of the flip-flops' outputs through the first 6 clock pulses, assuming that their initial state (at $t=0$) is 000 and they are triggered on the rising edge of the clock.

1.5 points

