

- * Show your work.
- * Show the units and what cancels.

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CHEM - EMR & the Atom (Eng) - 1 -

1. Calculate the energy of the photon emitted when an electron in a H atom falls from the fifth level to the ground state.

Givens

$n_i = 5$
 $n_f = 1$ (ground state)
 $R_H = 2.18 \times 10^{-18} \text{ J}$

Sign = \ominus , because it is releasing energy

① $\therefore E_{\text{gap}} = E_{\text{photon}}$

② $E_{\text{photon}} = R_H \left(\frac{1}{n_i^2} - \frac{1}{n_f^2} \right)$

$E_{\text{photon}} = 2.18 \times 10^{-18} \text{ J} \left(\frac{1}{(5)^2} - \frac{1}{(1)^2} \right)$

$E_{\text{photon}} = 2.18 \times 10^{-18} \text{ J} \left(\frac{1}{25} - 1 \right)$

$E_{\text{photon}} = -2.0928 \times 10^{-18} \text{ J}$ (3 S.F.)

$E_{\text{photon}} = [-2.09 \times 10^{-18} \text{ J}]$

2. Photons of 182 kJ/mol are emitted when e^- 's in H fall to the second energy level. Determine their original level.

Givens

$IE = 182 \text{ kJ/mol}$
 $E_{\text{photon}} = \frac{182 \text{ kJ}}{1 \text{ mol}} \times \frac{1000 \text{ J}}{1 \text{ kJ}} \times \frac{1 \text{ mol}}{6.02 \times 10^{23} \text{ atoms}}$

$n_f = 2$

$n_i = ?$

$R_H = 2.18 \times 10^{-18} \text{ J}$

① Convert kJ/mol \rightarrow J (IE \rightarrow E_{photon})

$E_{\text{photon}} = \frac{3.02325}{3 \text{ S.F.}} \times 10^{-19} \text{ J}$

② Find n_i

$\therefore E_{\text{gap}} = E_{\text{photon}}$

$E_{\text{photon}} = R_H \left(\frac{1}{n_i^2} - \frac{1}{n_f^2} \right)$

$\ominus 3.02325 \times 10^{-19} \text{ J} = 2.18 \times 10^{-18} \text{ J} \left(\frac{1}{n_i^2} - \frac{1}{(2)^2} \right)$

$\frac{-3.02325 \times 10^{-19} \text{ J}}{2.18 \times 10^{-18} \text{ J}} = \frac{1}{n_i^2} - \frac{1}{4}$

$-0.138681 + \frac{1}{4} = \frac{1}{n_i^2}$

$0.111318 n_i^2 = 1$

$n_i = \sqrt{\frac{1}{0.111318}}$

(Note energy levels must be to the closest whole number)

$n_i = 2.997$

$n_i = [3]$

Important:

Sign = \ominus , because e^- 's are falling, \therefore releasing energy

mol = 6.02×10^{23}

Chem Ass'n EMR & atom (ENK) - 2 -

3. Carbon has an ionization energy of 1086 kJ/mol. What wavelength of E.M.R. is just sufficient to ionize it?

① Convert kJ/mol \rightarrow J (IE \rightarrow E_{photon})

$$E_{\text{photon}} = \frac{1086 \text{ kJ}}{1 \text{ mol}} \times \frac{1000 \text{ J}}{1 \text{ kJ}} \times \frac{1 \text{ mol}}{6.02 \times 10^{23} \text{ atoms}}$$

$$E_{\text{photon}} = \frac{1.80398}{3 \text{ s.f.}} \times 10^{-18} \text{ J}$$

②

$$E_{\text{photon}} = \frac{h \cdot c}{\lambda}$$

$$\lambda = \frac{h \cdot c}{E_{\text{photon}}}$$

$$\lambda = \frac{(6.626 \times 10^{-34} \text{ J}\cdot\text{s}) (3.00 \times 10^8 \text{ m/s})}{(1.80398 \times 10^{-18} \text{ J})}$$

(3 s.f.)

$$\lambda = [1.10 \times 10^{-7} \text{ m}]$$

$$\lambda = [110. \text{ nm}]$$

4. You shine EMR with wavelength 189 nm onto the surface of tin (Sn) metal. The emitted electrons have $3.43 \times 10^{-19} \text{ J}$ of kinetic energy. Determine the work function of tin.

① Convert nm \rightarrow m

$$\lambda = 189 \text{ nm} \times \frac{10^{-9} \text{ m}}{1 \text{ nm}}$$

$$\lambda = 189 \times 10^{-9} \text{ m}$$

② Find E_{photon}

$$E_{\text{photon}} = \frac{h \cdot c}{\lambda}$$

$$E_{\text{photon}} = \frac{(6.626 \times 10^{-34} \text{ J}\cdot\text{s}) (3.00 \times 10^8 \text{ m/s})}{189 \times 10^{-9} \text{ m}}$$

$$E_{\text{photon}} = \frac{1.05174}{3 \text{ s.f.}} \times 10^{-18} \text{ J}$$

③

$$E_{\text{photon}} = W + KE$$

$$W = E_{\text{photon}} - KE$$

$$W = \left(\frac{1.05174 \times 10^{-18} \text{ J}}{3 \text{ s.f.}} - \frac{3.43 \times 10^{-19} \text{ J}}{2 \text{ decimal places}} \right)$$

$$W = [7.1 \times 10^{-19} \text{ J}] \quad 2 \text{ s.f.}$$