

## Outline (Chapter 3)

- **Atomic Packing:**
  - ✓ Linear density
  - ✓ Planer density
- **Single-crystal & Polycrystalline Materials**
- **Crystal Structure Analysis: X-ray Diffraction**

## Atomic Packing

➤ Arrangement of atoms on different **directions** and in different **planes** are called **linear** and **planar densities**, respectively.

✓ **Importance:**

- Deformation in metals (**Slip**) depends on linear & planar density (**WHY?**):
- Because slip occurs on planes that have the greatest density of atoms in direction with highest density (*along closest packed directions on the closest packed planes*)

## Atomic Packing

• **Linear Density**

Number of atoms/length whose centers lie on the direction vector for a specific crystallographic direction. (**# of atoms/unit length**)

$$\text{Linear Density of Atoms} \equiv \text{LD} = \frac{\text{Number of atoms}}{\text{Unit length of direction vector}}$$

• **Planar Density**

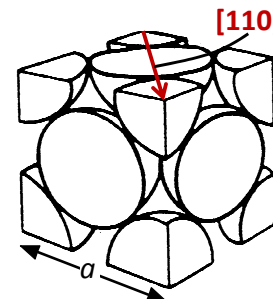
Number of atoms/unit area that are centered on a particular crystallographic plane. (**# of atoms/unit area**)

$$\text{Planar Density of Atoms} \equiv \text{PD} = \frac{\text{Number of atoms}}{\text{Area of the plane}}$$

## Linear Density

• **Example:**

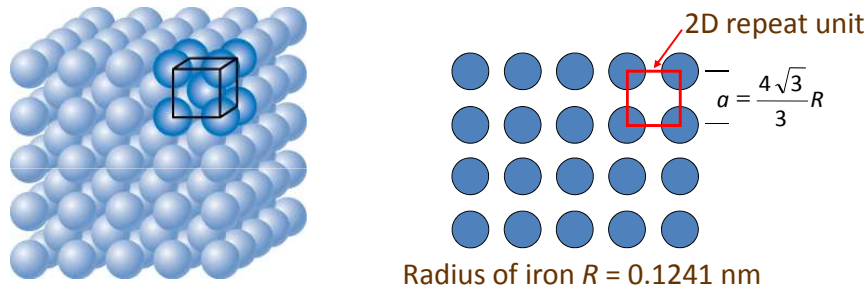
linear density of Al in [110] direction,  $a = 0.405 \text{ nm}$



$$\text{LD} = \frac{\text{\# atoms}}{\text{length}} = \frac{2}{\sqrt{2}a} = 3.5 \text{ atoms/nm}$$

# Planar Density

- **Example:** Planar density of iron (at  $T < 912^\circ\text{C}$ ) in  $\{100\}$  plane.  
At  $T < 912^\circ\text{C}$  Iron has **BCC crystal structure**



$$\text{Planar Density} = \frac{\text{atoms}}{\text{area}} = \frac{1}{a^2} = \frac{1}{\left(\frac{4\sqrt{3}}{3}R\right)^2} = 12.1 \frac{\text{atoms}}{\text{nm}^2} = 1.2 \times 10^{19} \frac{\text{atoms}}{\text{m}^2}$$

Lecture 6 - MECH 221

5

# Planar Density

- **FCC** and **HCP** are both **CLOSE-PACKED** structures.  
**APF = 0.74:** This is the maximum if all atoms are same size.

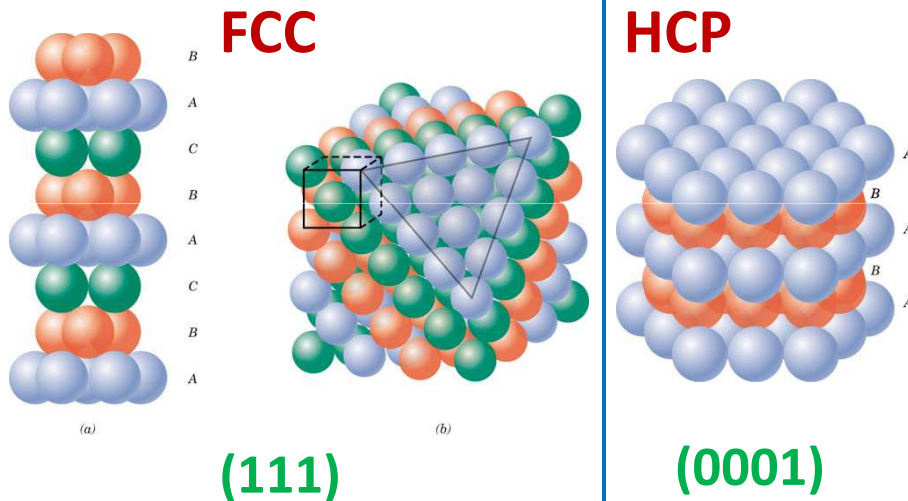
- Atoms are packed in **CLOSE-PACKED** planes:  
(*but different stacking sequence*)
  - ✓ In **FCC**,  $\{111\}$  are close packed planes (stack as **ABC-ABC-ABC**)
  - ✓ In **HCP**,  $\{0001\}$  is close packed plane (stack as **AB-AB-AB**)

➤ **Note:** *BCC is not close packed (APF = 0.68), the most densely packed plane is  $\{110\}$*

Lecture 6 - MECH 221

6

# Planar Density



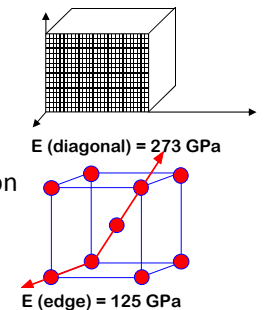
Lecture 6 - MECH 221

7

# Single-Crystal vs. Polycrystalline

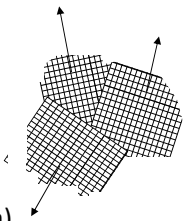
## SINGLE CRYSTALS

- ✓ This is when a piece of material is made up of one crystal;
  - ✓ All the unit cells are aligned up in the same orientation
  - ✓ Properties vary with direction (**anisotropic**).
- e.g. Stiffness (rigidity) electrical conductivity, refraction.



## POLYCRYSTAL

- ✓ Many small **crystals (grains)** with **different orientations** joined together. (each grain is a single crystal)
- ✓ Most engineering materials are POLYCRYSTALLINE.
- ✓ **Grain boundary:** Regions where grains (crystals) meet.
- ✓ If crystals are **randomly** oriented, overall component properties are not directional (**isotropic**). ( $E_{\text{poly iron}} = 210 \text{ GPa}$ )



Lecture 6 - MECH 221

8

# Single-Crystals

- Some engineering applications require single crystals:



-- diamond single crystals for abrasives

--turbine blades



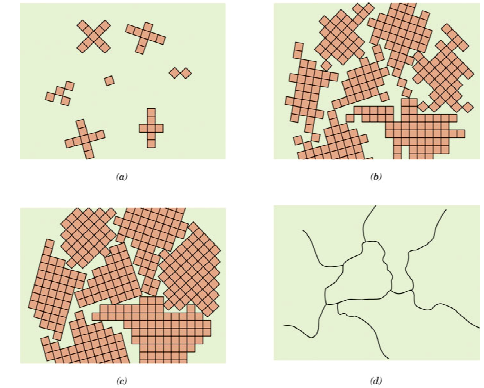
-- Crystal properties reveal features of atomic structure.

--Ex: Certain crystal planes in quartz fracture more easily than others.

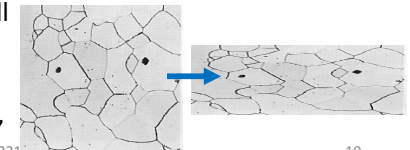


# Polycrystalline Materials

- Solidification of a polycrystalline material

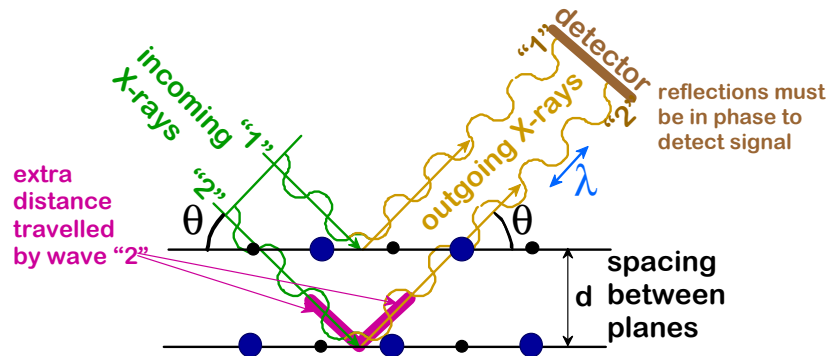


- ✓ If crystals are **randomly** oriented, overall component properties are not directional (**isotropic**).
- ✓ If grains are **textured** (e.g., after rolling), **anisotropic**.



# Crystal Structure Analysis: X-ray Diffraction

- Incoming X-rays **diffract** from crystal planes.



- Measurement of: Critical angles,  $\theta_c$ , for X-rays provide atomic spacing,  $d_{hkl}$ .

# Crystal Structure Analysis: X-ray Diffraction

- Finding out What the Crystal Structure is.

Analysis using X-Rays. X-Ray **Diffraction**.

- Bragg's Law:**

- ✓ Incoming X-rays diffract from crystal planes.
- ✓ X-rays are diffracted off atoms and either constructively interfere (peak) or destructively interfere (low) from layers of atoms depending on **interplanar** spacing ( $d_{hkl}$ ) and **angle**.

$$n\lambda = 2d_{hkl} \sin \theta \quad (\text{Bragg's Law})$$

$n = 1, 2, 3, 4, 5, \dots$

$\lambda =$  wavelength of incident X-rays

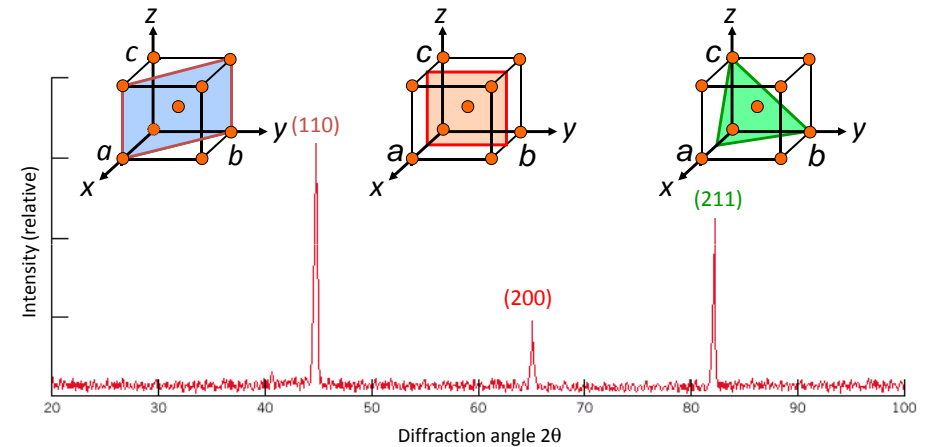
$\theta =$  incident angle

## Crystal Structure Analysis: X-ray Diffraction

- As  $\theta$  is varied, peaks will occur when distance  $d_{hkl}$  is a whole number of wavelengths.
- So can measure peak and use Bragg's law to determine  $d_{hkl}$  and then "a".
- Distance between similar planes in the cubic systems, e.g., (110) planes in adjacent unit cells:

$$d_{hkl} = \frac{a}{\sqrt{h^2 + k^2 + l^2}}$$

## X-ray Diffraction



Diffraction pattern for polycrystalline  $\alpha$ -iron (BCC)

## X-ray Diffraction (review problem)

- For BCC Fe, compute:
  - (a) the interplanar spacing and,
  - (b) the diffraction angle for (220) set of planes.
- The lattice parameter for Fe is 0.2866 nm
- the wavelength used is 0.1790 nm
- First order reflection.

## Summary

- Atoms may assemble into **crystalline** or **amorphous** structures.
- We can predict the **density** of a material, provided we know the **atomic weight**, **atomic radius**, and **crystal geometry** (e.g., FCC, BCC, HCP).
- Material properties generally vary with single crystal orientation (i.e., they are **anisotropic**), but properties are generally non-directional (i.e., they are **isotropic**) in polycrystals with randomly oriented grains.