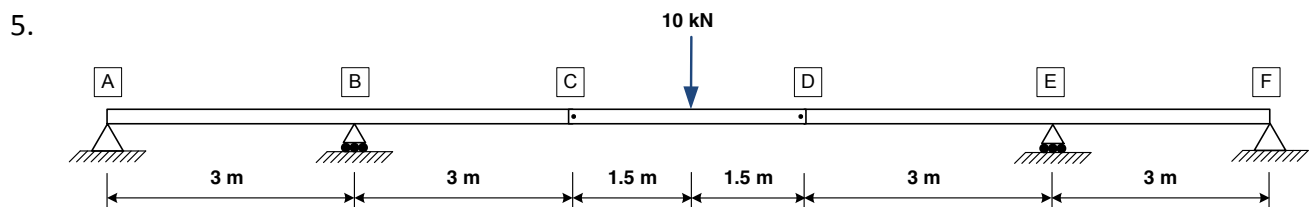
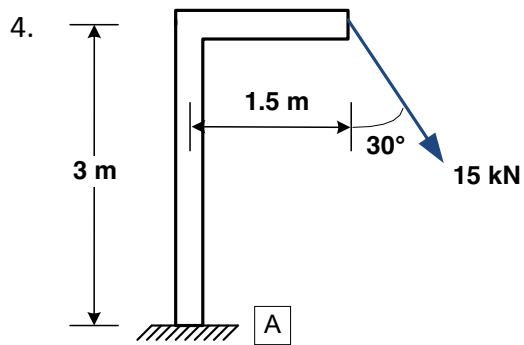
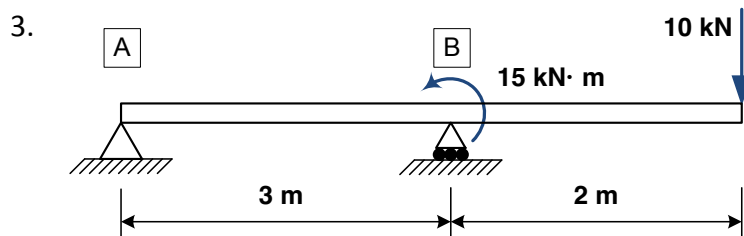
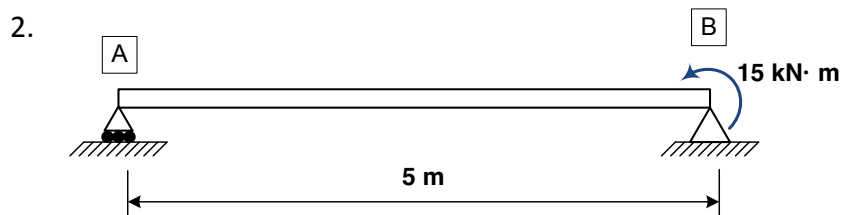
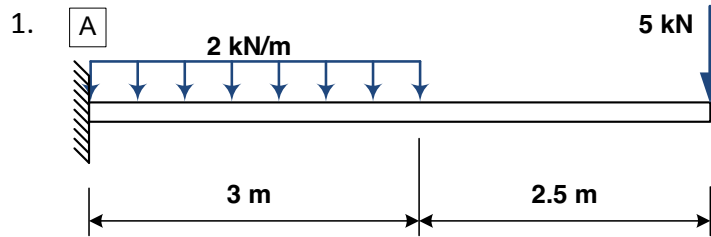


CVG2140 – Assignment No. 1 (External Reactions)

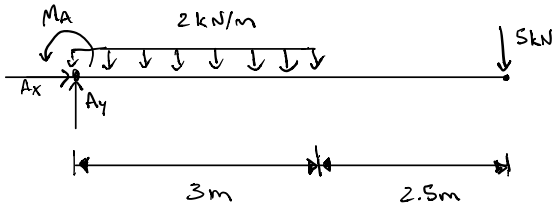
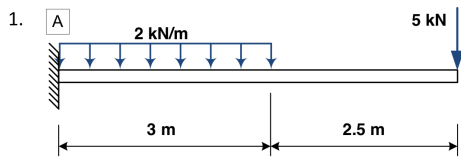
(Due Date: Friday, January 19th, 2018 by 4:59 PM)

Compute the external reactions for the following problems:



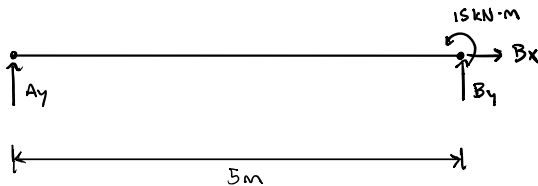
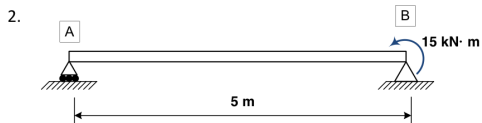
Note: **C** and **D** are internal pins.

CVG 2140 ASSIGNMENT #1



$$\begin{aligned} \rightarrow \sum F_x = 0 & \quad +\uparrow \sum F_y = 0 \\ 0 = A_x & \quad 0 = A_y - 2(3) - 5 \\ \therefore \boxed{A_x = 0 \text{ kN}} & \quad \boxed{A_y = 11 \text{ kN}} \end{aligned}$$

$$\begin{aligned} \curvearrowright \sum M_A = 0 \\ 0 = M_A - 6(1.5) - 5(5.5) \\ \boxed{M_A = 36.5 \text{ kN}\cdot\text{m}} \end{aligned}$$

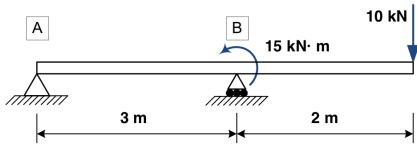


$$\begin{aligned} \rightarrow \sum F_x = 0 & \quad +\uparrow \sum F_y = 0 \\ 0 = B_x & \quad [1] \quad 0 = A_y + B_y \\ \therefore \boxed{B_x = 0 \text{ kN}} \end{aligned}$$

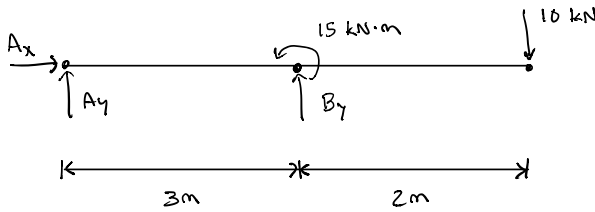
$$\begin{aligned} \curvearrowright \sum M_B = 0 \\ 0 = 15 - A_y(5) \\ \boxed{A_y = 3 \text{ kN}} \end{aligned}$$

$$\begin{aligned} \therefore [1] \quad 0 = 3 + B_y \\ B_y = -3 \text{ kN} \\ \boxed{B_y = 3 \text{ kN} \downarrow} \end{aligned}$$

3.



UKT PA

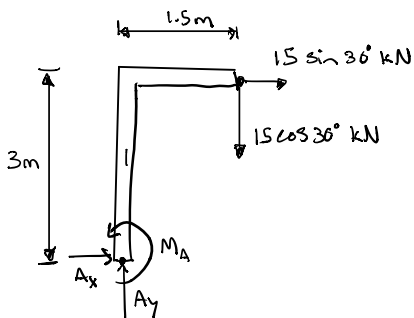
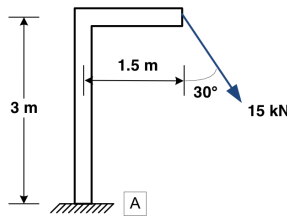


$$\begin{aligned} \rightarrow \sum F_x = 0 & \quad \uparrow \sum F_y = 0 \\ 0 = A_x & \quad [1] \quad 0 = A_y + B_y - 10 \\ \therefore \boxed{A_x = 0 \text{ kN}} & \end{aligned}$$

$$\begin{aligned} \curvearrowright \sum M_B = 0 \\ 0 = 15 - A_y(3) - 10(2) \\ A_y = \frac{-5}{3} \text{ kN} \\ \boxed{A_y = 1.67 \text{ kN} \downarrow} \end{aligned}$$

$$\begin{aligned} \therefore [1] \quad 0 = -\frac{5}{3} + B_y - 10 \\ \boxed{B_y = 11.67 \text{ kN}} \end{aligned}$$

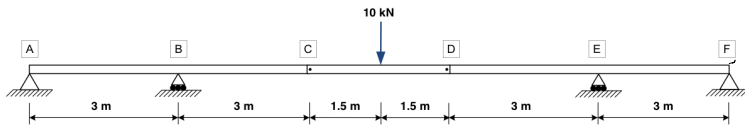
4.



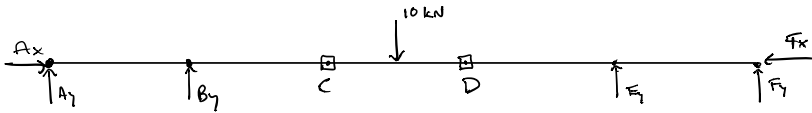
$$\begin{aligned} \rightarrow \sum F_x = 0 & \quad \uparrow \sum F_y = 0 \\ 0 = A_x + 15 \sin 30^\circ & \quad 0 = A_y - 15 \cos 30^\circ \\ A_x = -15 \sin 30^\circ & \quad A_y = 15 \cos 30^\circ \\ \therefore \boxed{A_x = -7.5 \text{ kN}} \quad \therefore A_y \leftarrow & \quad \therefore \boxed{A_y = 13.0 \text{ kN}} \end{aligned}$$

$$\begin{aligned} \curvearrowright \sum M_A = 0 \\ 0 = M_A - (15 \cos 30^\circ)(1.5) - (15 \sin 30^\circ)(3) \\ \therefore \boxed{M_A = 41.99 \text{ kN}\cdot\text{m}} \end{aligned}$$

5.



Note: C and D are internal pins.



$$\sum F_x = 0 \quad \uparrow \sum F_y = 0$$

$$0 = A_x - F_x$$

∴ There are no external forces, the rxn forces

A_x, F_x equal 0

$$\boxed{A_x = F_x = 0 \text{ kN}}$$

$$0 = A_y + B_y - 10 + E_y + F_y$$

∴ Problem is symmetric

$$0 = A_y + B_y - 10 + A_y + B_y$$

$$0 = 2A_y + 2B_y - 10$$

$$0 = A_y + B_y - 5$$

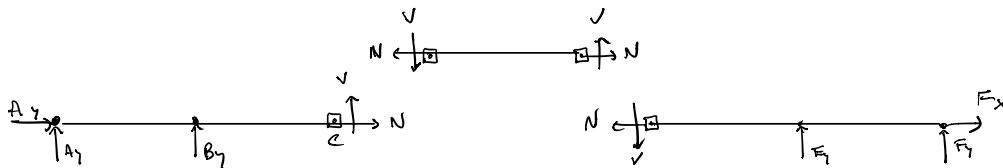
$$\sum M_A = 0$$

$$0 = B_y(3) - 10(7.5) + E_y(12) + A_y(15)$$

checking values:

$$0 = 10(3) - 10(7.5) + 10(12) + (-5)(15)$$

$$0 = 0$$



$$\sum F_x = 0$$

$$0 = B_y + N$$

$$\uparrow \sum F_y = 0$$

$$0 = A_y + B_y + V$$

$$\text{sub into [1]} \rightarrow 0 = -V - 5$$

$$V = -5 \text{ kN}$$

$$\sum M_A = 0$$

$$0 = B_y(3) + V(6)$$

$$V = -\frac{B_y}{2} \rightarrow -5 = -\frac{B_y}{2}$$

$$\boxed{B_y = 10 \text{ kN} = E_y}$$

$$\therefore 0 = A_y + B_y - \frac{B_y}{2} \Rightarrow 0 = A_y + 10 - 10$$

$$\boxed{A_y = -5 \text{ kN} = F_y}$$

Direction assumption was incorrect
∴ $A_y \downarrow$ and $F_y \downarrow$

