



CVG 3109
SOIL MECHANICS - I
MIDTERM EXAMINATION

Length of Examination: 1 hr 15 mins
Course Instructor: Sai Vanapalli

7th Nov, 2017 (08:30 to 09:45)
Page 1 of 9

First Name: _____

Last Name: _____

Student Number: _____

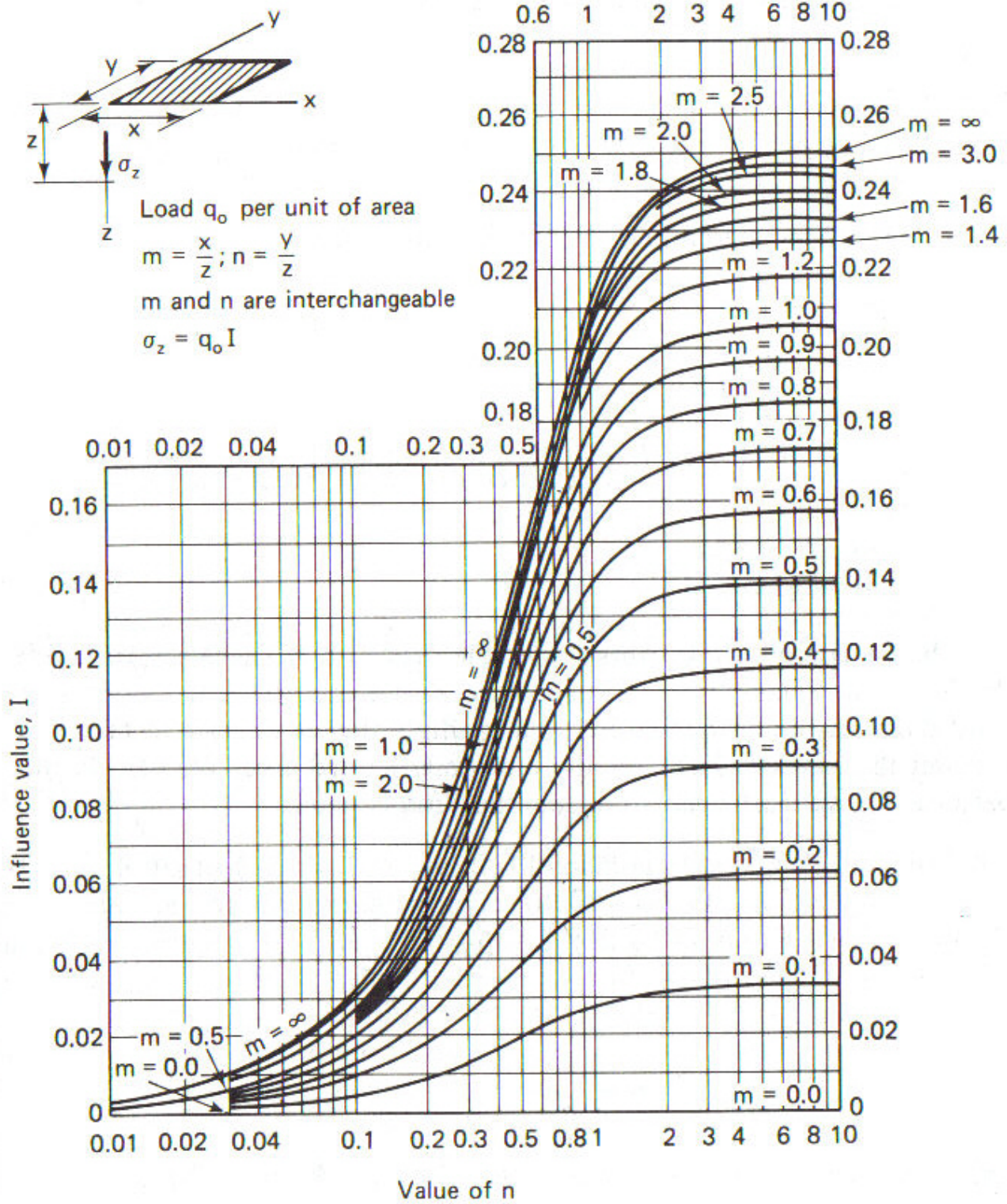
Signature _____

- (i) This is a closed book exam. No textbooks are allowed
- (ii) **Formula sheet** is available on the last page of this question paper
- (iii) **If you do not understand a question, clearly state an assumption and proceed.**
- (iv) Non programmable calculators are permitted
- (v) Questions have the values shown next to the questions.
- (vi) **Marks will be taken out for missing units and labels.**
- (vii) Answers should be succinct.

At the end of the exam, when time is up:

- Stop working and turn your exam upside down.
- Please remain silent.
- Do not move or speak until ALL exams have been picked up, and a TA or the Professor gives the go-ahead to leave.

<u>Question</u>	<u>Max Marks</u>	<u>Marks Awarded</u>
1	Conceptual Questions: 20 %	
2	Chp. 1: Fundamentals/Review: 20 %	
3	Chp. 2: Seepage and Effective Stress: 35 %	
4	Chap. 3: Elastic theory/Stress Distribution : 25 %	
Total	Maximum 100%	



Formulae Sheet

Phase relationships:

Unit weight of soil:

$$\gamma = \frac{W}{V} = \frac{(Se + G_s)}{1 + e} \gamma_w$$

Submerged unit weight: $\gamma_{sub} = \frac{(G_s - 1)}{1 + e} \gamma_w$

Dry unit weight:

$$\gamma_d = \frac{W_s}{V} = \frac{G_s}{1 + e} \gamma_w = \frac{\gamma}{1 + w}$$

$$Se = wG_s$$

Elastic Theory (Stress Distribution theory)

Boussinesq's equation for determining vertical stress due to a point load

$$\sigma_z = \frac{3Q}{2\pi z^2} \left\{ \frac{1}{1 + \left(\frac{r}{z}\right)^2} \right\}^{5/2}$$

Determination of vertical stress due to a rectangular loading: $\sigma_z = q I_c$ (Charts also available)

$$I_c = \frac{1}{4\pi} \left[\frac{2mn\sqrt{m^2 + n^2 + 1} \left(\frac{m^2 + n^2 + 2}{m^2 + n^2 + 1} \right) + \tan^{-1} \frac{2mn\sqrt{m^2 + n^2 + 1}}{m^2 + n^2 + m^2 n^2 + 1}}{m^2 + n^2 + m^2 n^2 + 1} \right]$$

$m = B/z$ and $n = L/z$ (both m and n are interchangeable)

Approximate method to determine vertical stress,

$$\sigma_z = \frac{qBL}{(B+z)(L+z)}$$

Vertical stress determination using Newmarks Chart

$$\sigma_z = q I_c \text{ (No. of sectors)}$$

Permeability & Effective Stress

Total head = Pressure head + Elevation head + Velocity head

$$h = \frac{u}{\gamma_w} + \frac{v^2}{2g} + z$$

Hydraulic gradient: $i = \frac{\Delta h}{L}$

$$v = ki$$

Darcy's law: $q = vA$

$$Q = kiAt = k \cdot \frac{\Delta h}{L} \cdot At$$

Equivalent hydraulic conductivity:

$$k_{H(eq)} = \frac{k_{H_1} H_1 + \dots + k_{H_n} H_n}{H_1 + \dots + H_n}$$

$$k_{V(eq)} = \frac{H_1 + \dots + H_n}{\left(\frac{H_1}{k_{V_1}}\right) + \dots + \left(\frac{H_n}{k_{V_n}}\right)}$$

Seepage in a flow net:

$$q = k \cdot h_w \cdot \frac{N_f}{N_d}$$

Pore-water pressure (kPa):

$$u_p = \gamma_w [h_p - (-z_p)] = \gamma_w (h_p + z_p)$$

Total seepage force = $i\gamma_w V$

Seepage per unit volume = $i\gamma_w$

Effective stress: $\sigma' = \sigma - u_w$

Effective stress on downward seepage:

$$\sigma' = \gamma_{sub} z + jz = \gamma_{sub} z + iz\gamma_w$$

Effective stress on upwards seepage:

$$\sigma' = \gamma_{sub} z - jz = \gamma_{sub} z - iz\gamma_w$$

Critical hydraulic gradient:

$$\sigma' = 0 = \gamma_{sub} z - iz\gamma_w \Leftrightarrow i_c = \frac{\gamma_{sub}}{\gamma_w}$$

$$i_c = \frac{(G_s - 1)\gamma_w}{1 + e} \cdot \frac{1}{\gamma_w} = \frac{(G_s - 1)}{1 + e}$$