

EXAMPLES 10.1
(Part 1A: IL for determinate beams)

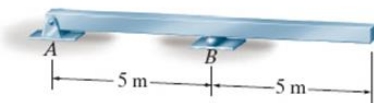
Lecture outline:

1. Examples: Determinate Beams (Tabular method)
2. Examples : Determinate Beams (Muller-Bresslau method)

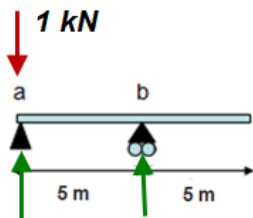
1. Examples - Determinate Beams (Tabular method)

Example#1 - REACTION

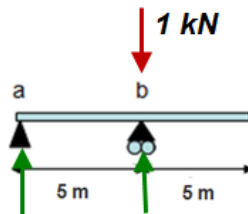
Construct the influence line for the vertical reaction at *B* of the beam in Fig. 6-2a.



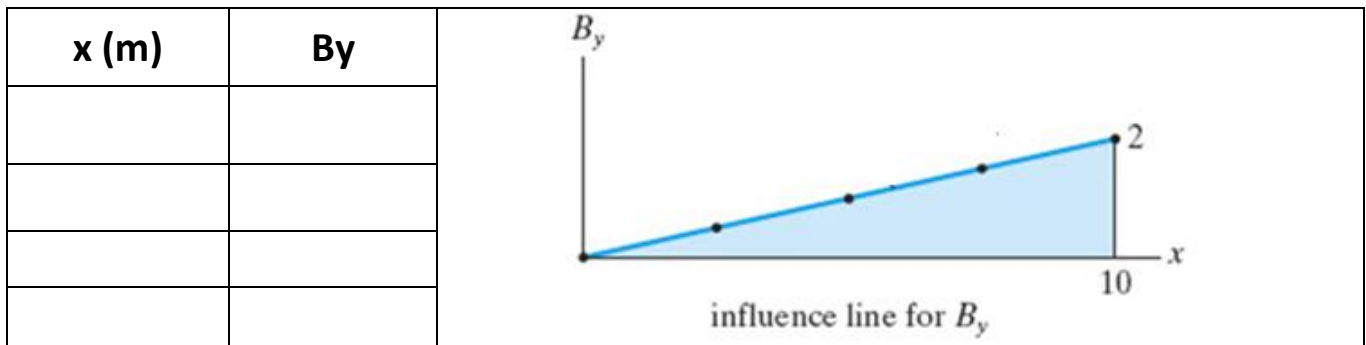
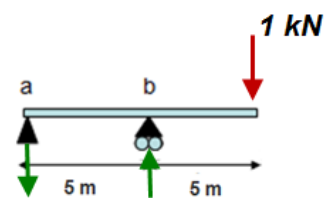
unit load @ x = 0



unit load @ x = 5

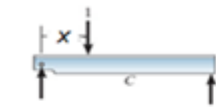
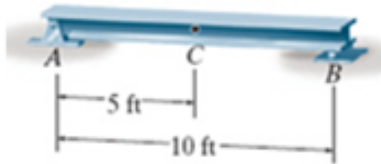


unit load @ x = 10

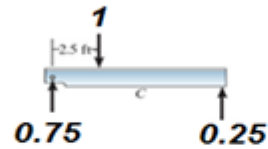
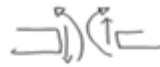


Example #2 – MOMENT

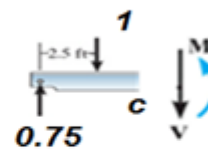
Construct the influence line for the moment @ C for the beam below:



example ... @ $x = 2.5$ ft



cut at C ... get M_C



$$(+\Sigma M_C = 0;$$

$$M_C - (0.75)(5) + (1)(2.5) = 0$$

$$M_C = 1.25 \text{ kN m}$$

Repeat for other positions and setup table then draw IL diagram ...

x	M_C
0	0
2.5	1.25
5	2.5
7.5	1.25
10	0

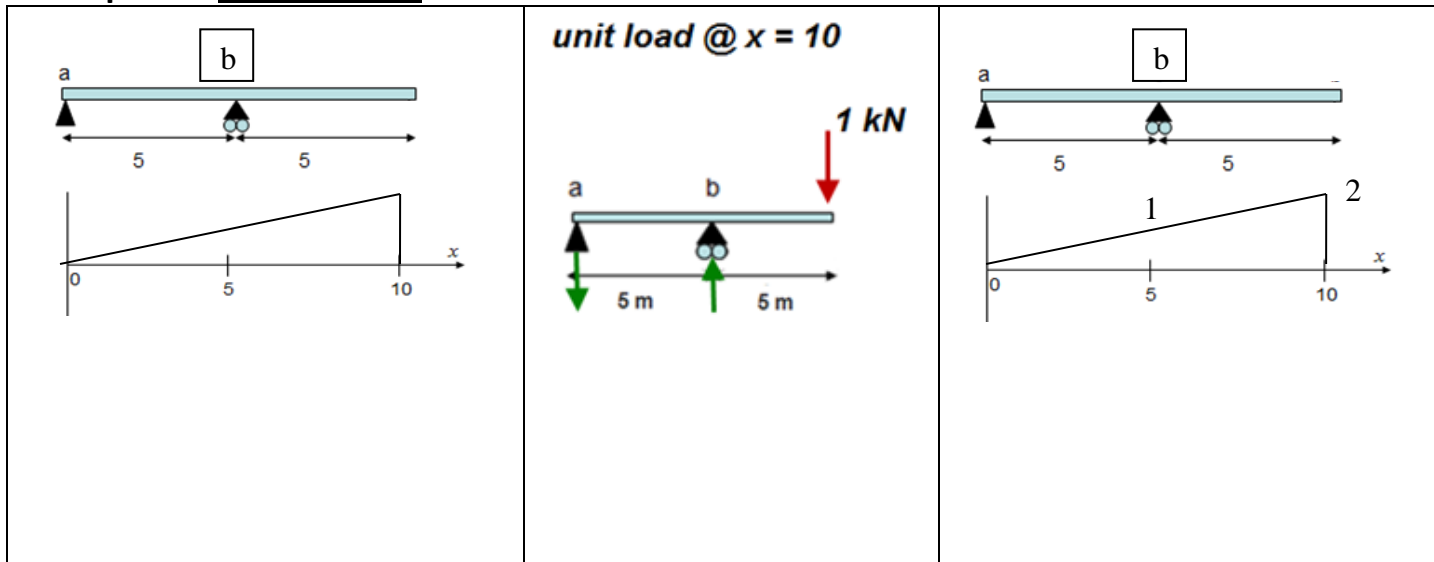


2. Examples - Determinate Beams (Muller-Bresslau method)

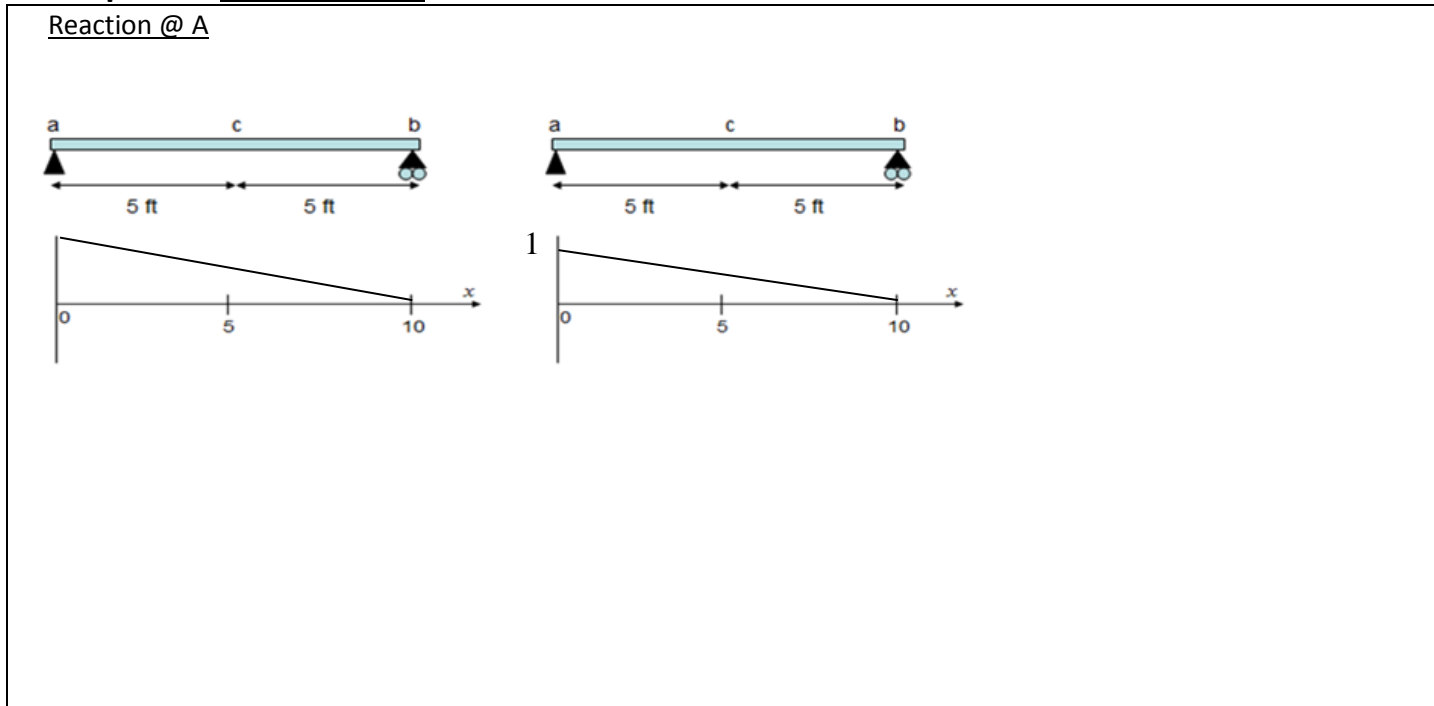
For the beams shown below

- Draw the “qualitative” influence line (i.e. just the shape)
- Then draw the “quantitative” influence line for the reaction that is indicated

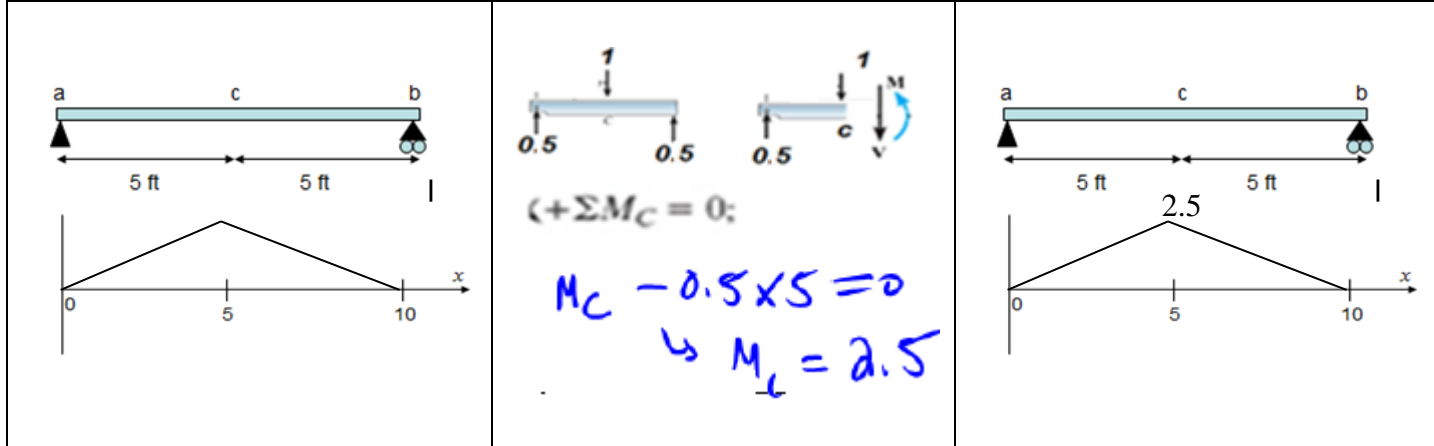
Example 1a: Reaction @ B



Example 1b: Reaction @ A

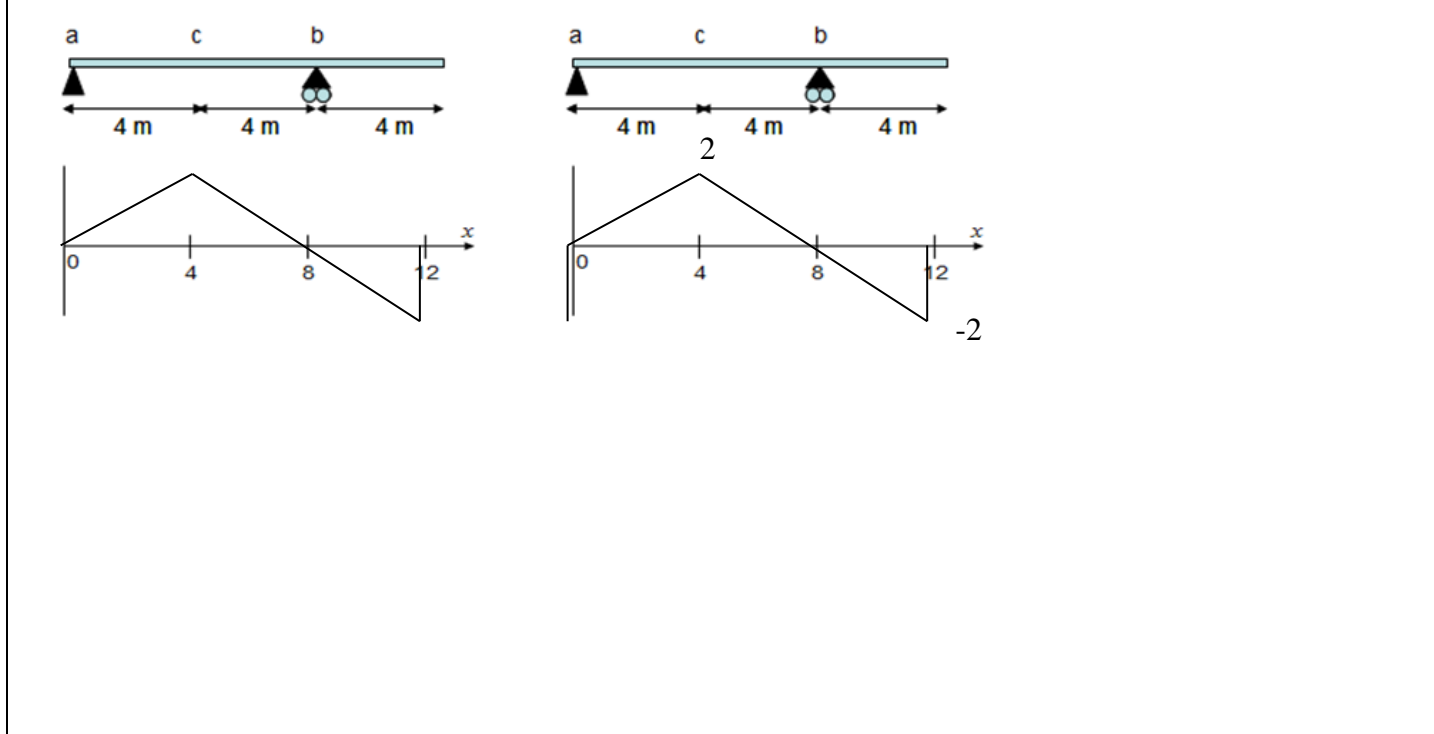


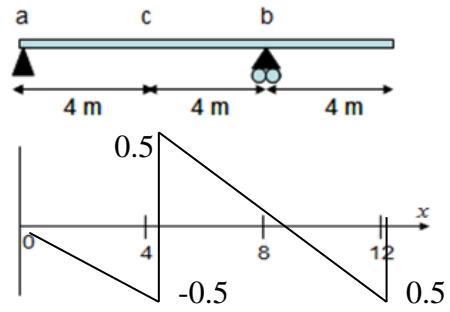
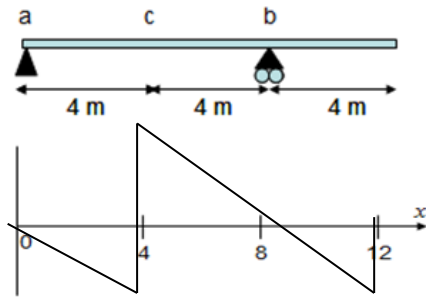
Example 2a: Moment @ C



Example 2b: Moment @ C

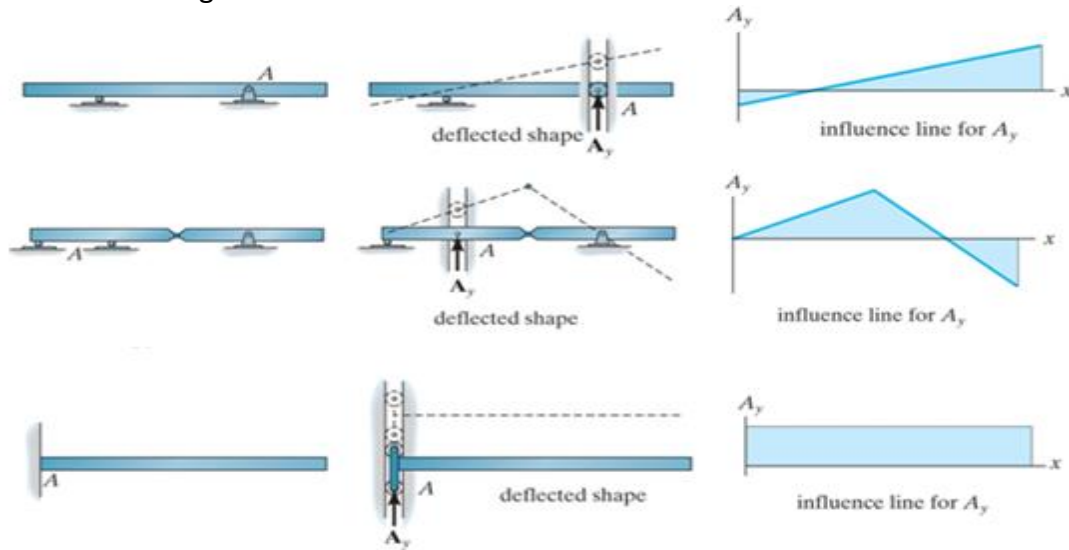
Moment @ C



Example 3: Shear @ CShear @ C

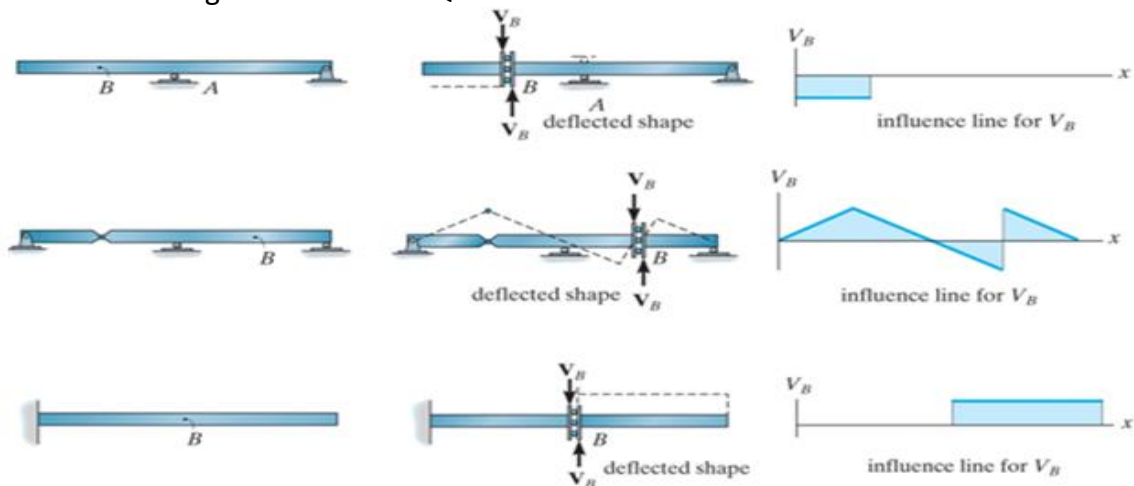
Extra Examples : - More challenging...

For the following beams find the QUALITATIVE influence line for the **vertical reaction at A**



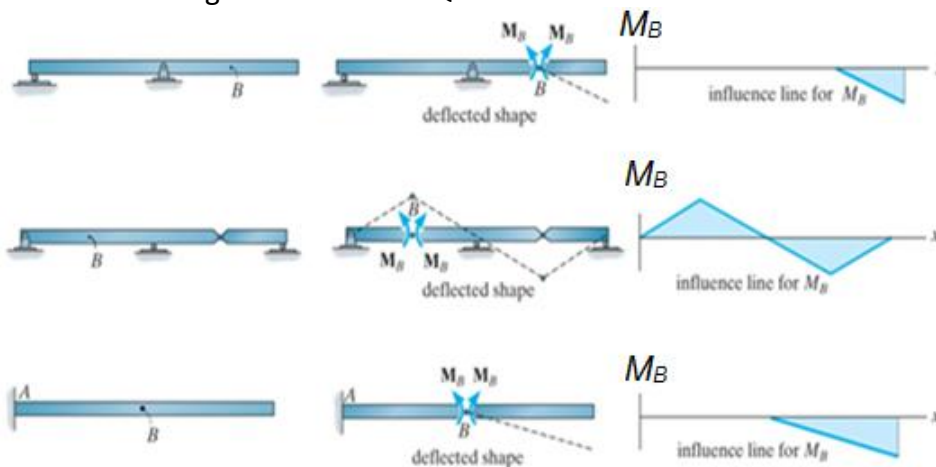
Extra Examples: - More challenging...

For the following beams find the QUALITATIVE influence line for the **shear at B**



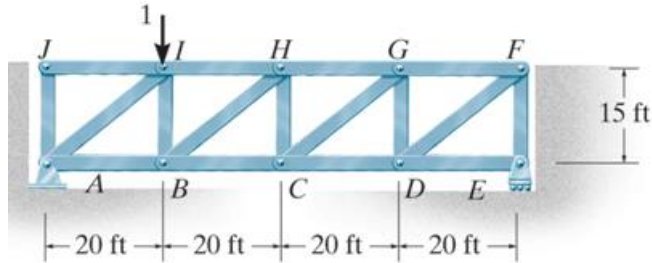
Extra Examples: - More challenging...

For the following beams find the QUALITATIVE influence line for the **moment at B**



3. Examples - Determinate Trusses

Example 1: Draw the influence line for member BC in the truss below. Assume the load moves along the top chord.



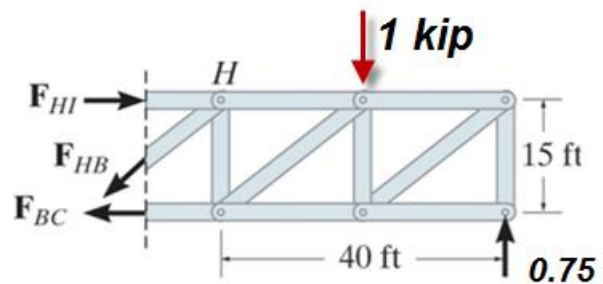
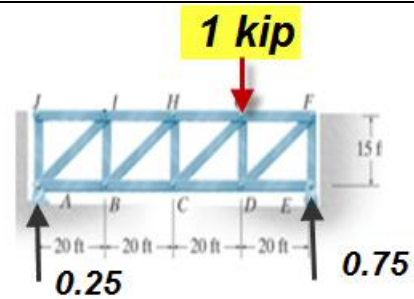
Load @ joint J ($x = 0\text{ft}$): $F_{BC} = \underline{0}$.

Load @ joint I ($x = 20\text{ft}$): $F_{BC} = \underline{0.667}$.

Load @ joint H ($x = 40\text{ft}$): $F_{BC} = \underline{1.33}$.

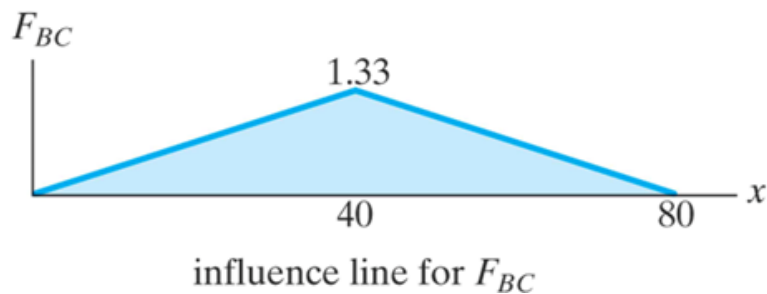
Load @ joint G ($x = 60\text{ft}$): $F_{BC} = \underline{0.667}$.

Load @ joint F ($x = 80\text{ft}$): $F_{BC} = \underline{0}$.

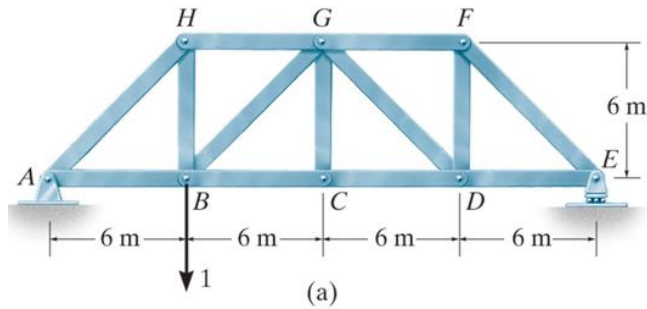


$$\begin{aligned}
 & (+ \sum M_H = 0 ; \\
 & -F_{BC}(15) + (0.25)(40) - (0.75)(40) = 0 \\
 & F_{BC} = 0.667 \text{ (T)}
 \end{aligned}$$

x	F_{BC}
0	0
20	0.667
40	1.33
60	0.667
80	0



Example 2: Draw the influence line for member GB in the truss below. Assume the load moves along the Bottom chord.



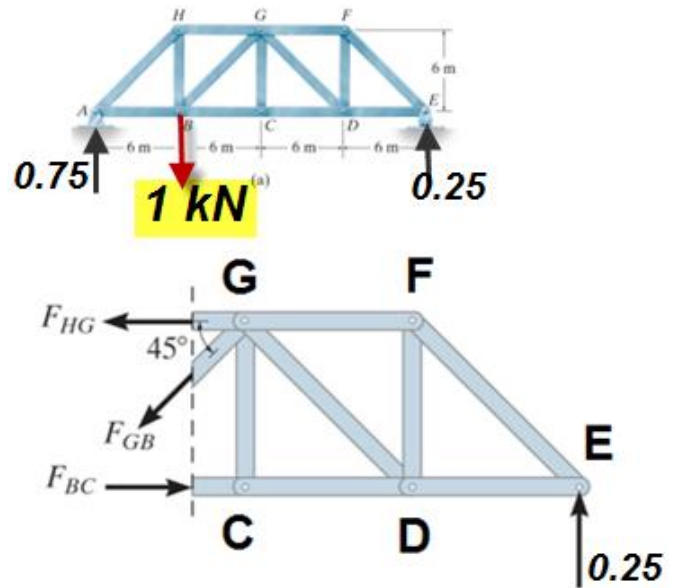
Load @ joint A ($x = 0\text{m}$): $F_{GH} = \underline{0}$.

Load @ joint B ($x = 6\text{m}$): $F_{GH} = \underline{\hspace{2cm}}$

Load @ joint C ($x = 12\text{m}$): $F_{GH} = \underline{-0.707}$.

Load @ joint D ($x = 18\text{m}$): $F_{GH} = \underline{-0.354}$.

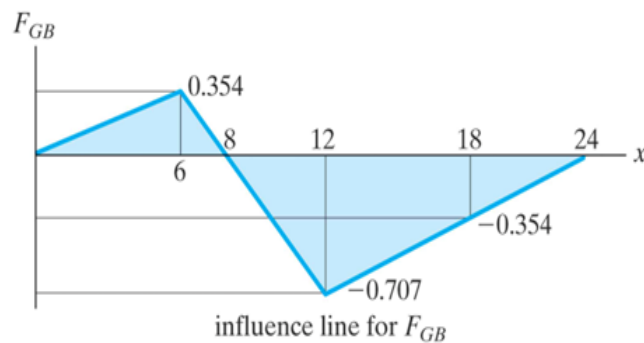
Load @ joint E ($x = 24\text{m}$): $F_{GH} = \underline{0}$.



$$\Sigma F_y = 0; \quad (\quad) - F_{GB} \sin 45^\circ = 0$$

$$F_{GB} = \underline{\hspace{2cm}}$$

x	F_{GB}
0	0
6	0.354
12	-0.707
18	-0.354
24	0



EXAMPLES
10.2: Influence Lines
(Part 2: Application examples)

Examples outline:

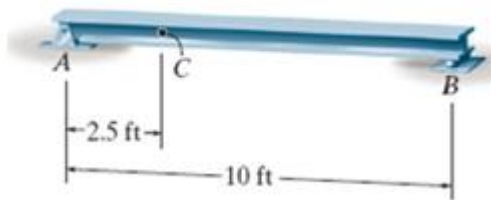
1. Examples: Determinate Beams – Maximum load effects
2. Examples : Trusses – Maximum axial forces
3. Examples: Indeterminate beams – Placing live loads
4. Examples: Truck loads

1. Examples: Determinate Beams - Maximum load effects

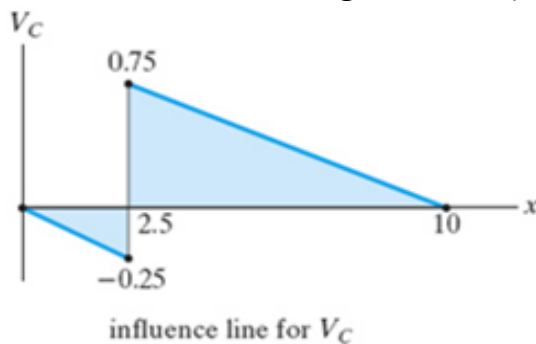
Example #1

Determine the max +ve shear that can be developed @ **C** due to:

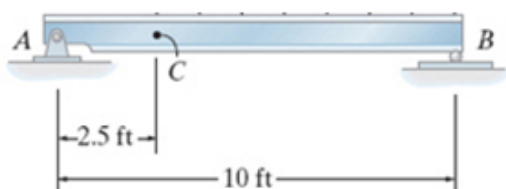
- Concentrated live load of 4000 lb and;
- Distributed live load of 2000 lb/ ft



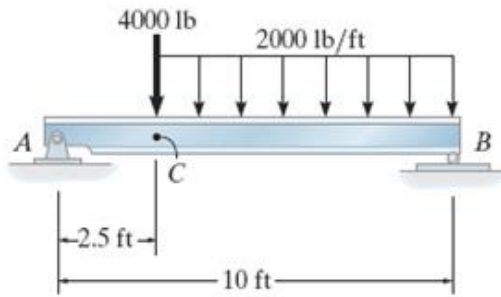
Draw influence line using unit load (Muller-Bresslau + similar triangles)



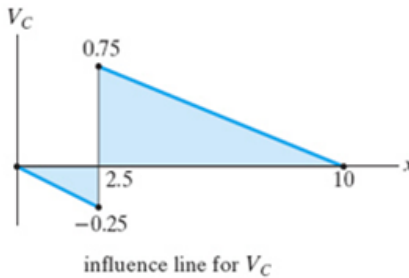
Loading for maximum positive shear @ C V_c^+ ?



Loading for maximum positive shear @ C V_C^+ :

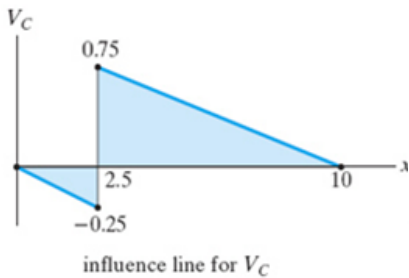


Effect of concentrated live load of 4000 lbs:



$$V_C = 0.75(4000 \text{ lb}) = 3000 \text{ lb}$$

Effect of distributed live load of 2000 lb/ft:

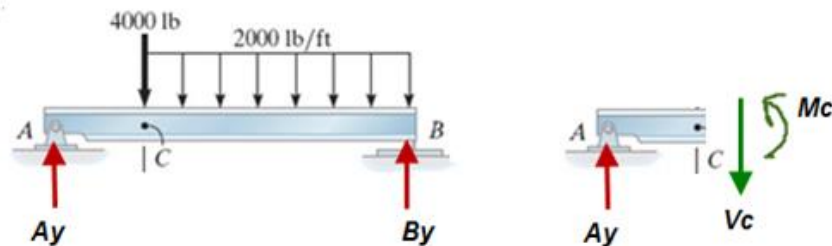


$$V_C = \left[\frac{1}{2}(10 \text{ ft} - 2.5 \text{ ft})(0.75) \right] 2000 \text{ lb/ft} = 5625 \text{ lb}$$

Total Maximum Shear at C

$$(V_C)_{\max} = 3000 \text{ lb} + 5625 \text{ lb} = 8625 \text{ lb} \quad \text{Ans.}$$

Note, we could have also determined this value using statics (try yourself)...

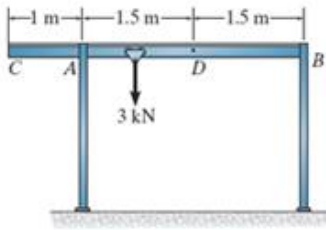


Example #2

The beam shown below is used to support a moving crane.

The loads on the beam are:

- Concentrated live load of 3kN;
- Distributed live load of 2 kN/m
- Distributed dead load due to self-weight (24 kg/m)
- Assume the beam is pinned @ A and has a roller @ B.

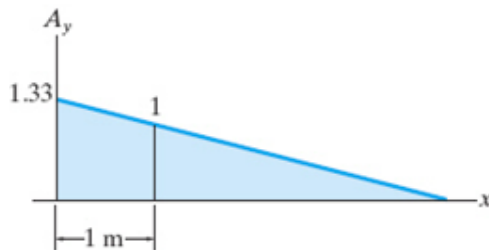


(a) Determine the max vertical reaction that can be developed @ **A**.

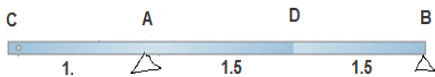
Loads:

- *Concentrated live load =*
- *Distributed live load =*
- *Distributed dead load =*

Influence line for reaction at A:



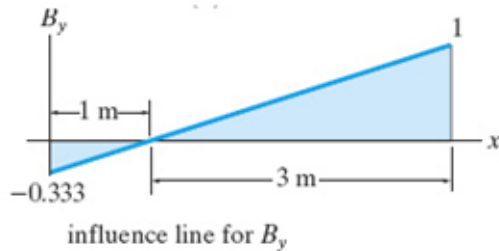
Loading for maximum reaction at A:



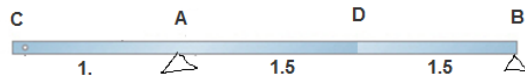
$$A_y \rightarrow: A_{y_{\max}} = (3)(1.33) + 2 \left[\frac{1}{2} \times 4 \times 1.33 \right] + 0.235 \left[\frac{1}{2} \times 4 \times 1.33 \right] =$$

(b) Determine the max +ve vertical reaction that can be developed @ **B**.

Influence line for reaction at B:



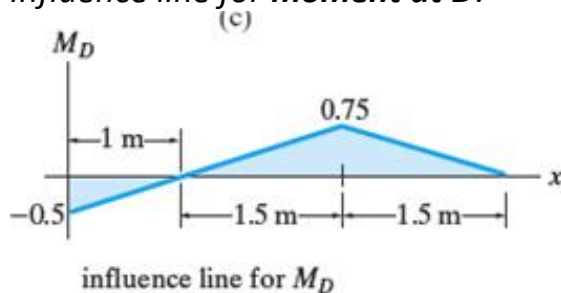
Loading for maximum positive reaction at B:



$$B_y \rightarrow: B_{y_{\max}} = (3)(1) + 2 \left[\frac{1}{2} \times 3 \times 1 \right] + 0.235 \left[\left(\frac{1}{2} \times 3 \times 1 \right) + \left(\frac{1}{2} \times 1 \times -0.333 \right) \right] =$$

(c) Determine the max +ve moment that can be developed @ **D**.

Influence line for moment at D:



Loading for maximum positive moment at D:



$$M_{D+} \rightarrow: M_{D_{\max}} = (3)(0.75) + 2 \left[\frac{1}{2} \times 3 \times 0.75 \right] + 0.235 \left[\left(\frac{1}{2} \times 3 \times 0.75 \right) + \left(\frac{1}{2} \times 1 \times -0.5 \right) \right] =$$

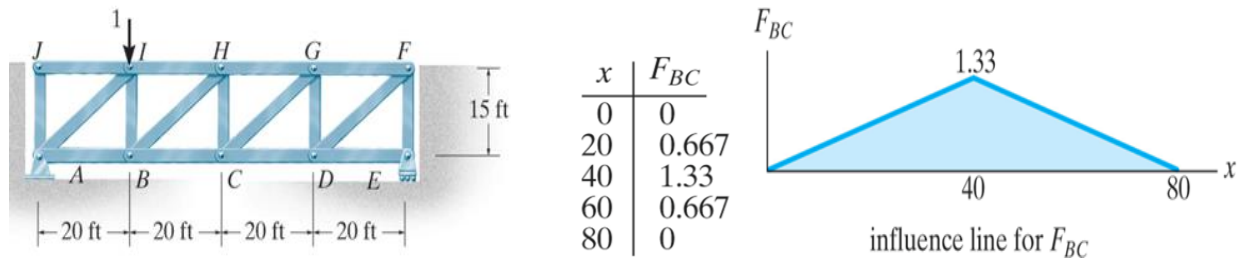
2. Examples: Trusses - Maximum axial force

Example #1

Determine the **maximum tensile axial force** that can be developed in **member BC** of the truss due to:

- a concentrated live load of 20 kips
- The loading is applied at the top chord.

Recall we had found the influence line for member BC (see below) ...



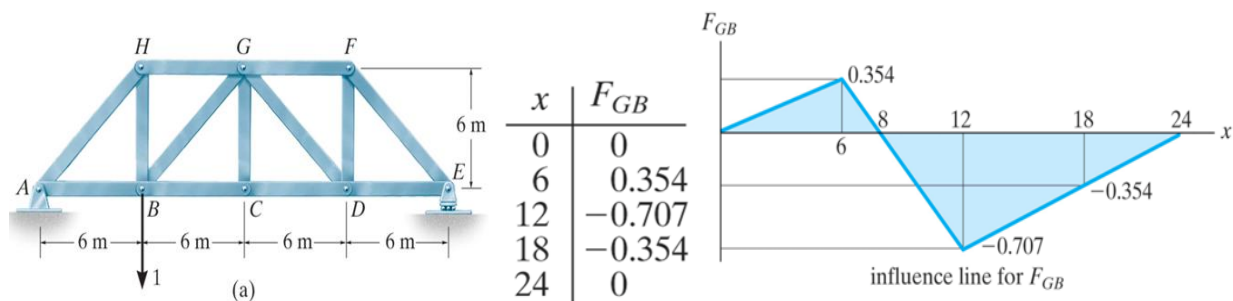
Answer: Maximum Tensile axial force = $20 * 1.33 = 26.6$ kips

Example #2

Determine the **maximum compressive axial force** that can be developed in **member GB** of the truss due to:

- a concentrated live load of 50 kN and
- a distributed live load of 5 kN/m.
- The loading is applied at the bottom chord.

Recall we had found the influence line for member GB (see below)



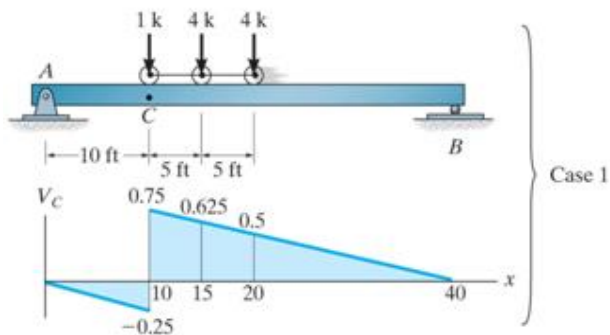
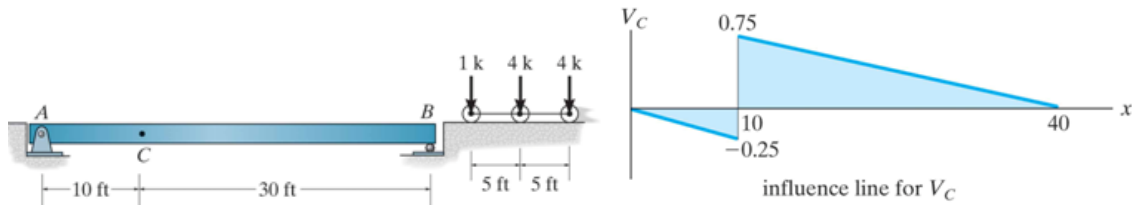
Answer: Maximum Compressive axial force =

$$50*(0.707) + 5 [(1/2 * 4*0.707) + (1/2 * 12*0.707)] = 63.6 \text{ kips (C)}$$

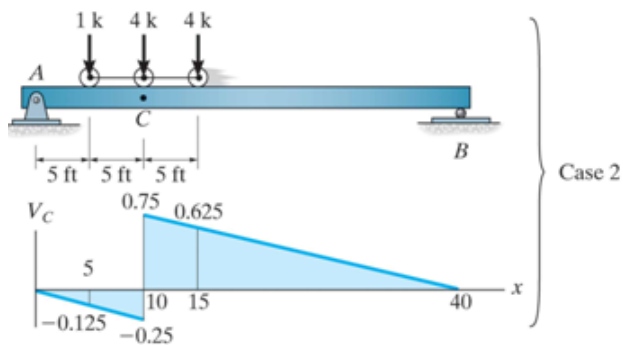
4. Examples: Truck loads

Example: bridge beam

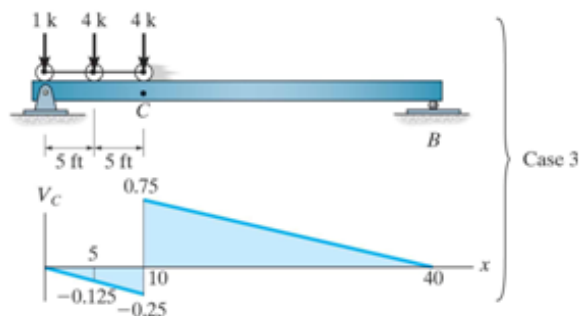
Find the placement of the truck loads that causes **maximum positive shear at C**



$$V_C = 1 \times (0.75) + 4 \times (0.625) + 4 \times (0.5) = 5.25 \text{ k}$$



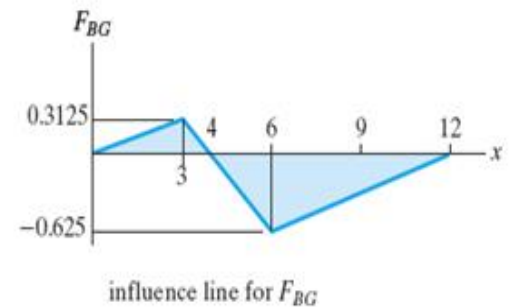
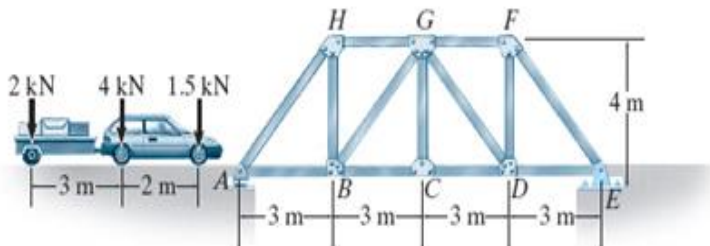
$$V_C = 1 \times (-0.125) + 4 \times (0.75) + 4 \times (0.625) = 5.375 \text{ k}$$



$$V_C = 1 \times (0) + 4 \times (-0.125) + 4 \times (0.75) = 2.5 \text{ k}$$

Example: bridge truss

Determine the maximum compressive force developed in member BG of the side truss in Fig. 6-32a due to the right side wheel loads of the car and trailer. Assume the loads are applied directly to the truss and move only to the right.

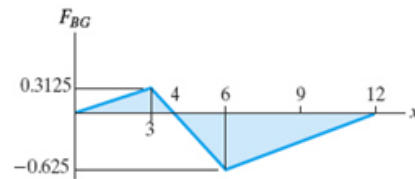


3 cases to consider:

1. with **1.5 kN** load @ point C

$$F_{BG} = 1.5 \text{ kN}(-0.625) + 4(0) + 2 \text{ kN}\left(\frac{0.3125}{3 \text{ m}}\right)(1 \text{ m})$$

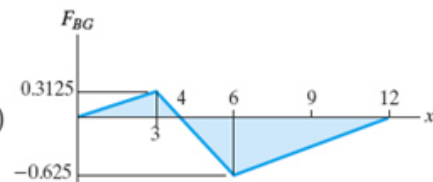
$$= -0.729 \text{ kN}$$



2. with **4 kN** load @ point C

$$F_{BG} = 4 \text{ kN}(-0.625) + 1.5 \text{ kN}\left(\frac{-0.625}{6 \text{ m}}\right)(4 \text{ m}) + 2 \text{ kN}(0.3125)$$

$$= -2.50 \text{ kN}$$

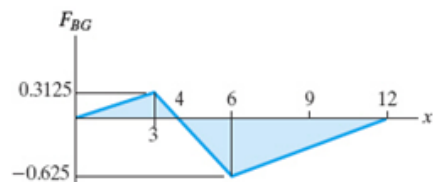


3. with **2 kN** load @ point C

$$F_{BG} = 2 \text{ kN}(-0.625) + 4 \text{ kN}\left(\frac{-0.625}{6 \text{ m}}\right)(3 \text{ m}) + 1.5 \text{ kN}\left(\frac{-0.625}{6 \text{ m}}\right)(1 \text{ m})$$

$$= -2.66 \text{ kN}$$

Ans.



Since this final case results in the largest answer, the critical loading occurs when the 2-kN load is at C.