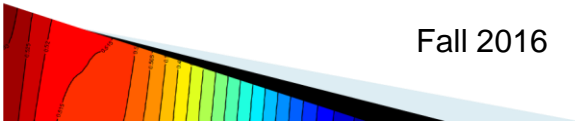


GNG 1106
Fundamentals of Engineering Computation
Module 2 - More on Fundamental Concepts

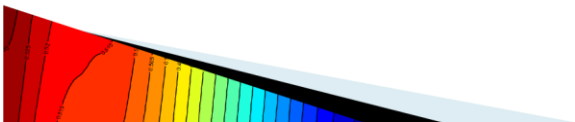


Fall 2016



1

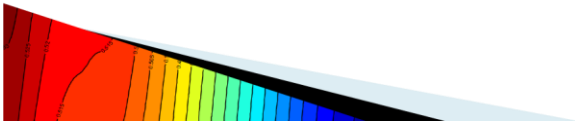
Topic 1: Data Types and Simple Variables



2

Data Types in C

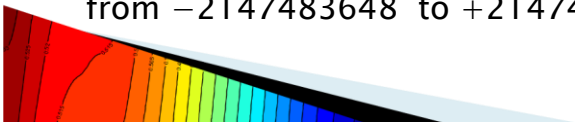
- ▶ The basic “data types” in C are literals, variables and symbolic constants.
- ▶ Literals express values and are used in expressions.
- ▶ The content of a variable can be changed by a program but a symbolic constant cannot be changed.
 - Symbolic constants also have names, as variables, but do not occupy memory, they are treated more like literals.
- ▶ All variables and symbolic constants must be declared and defined before usage in a C program.



3

Literal values

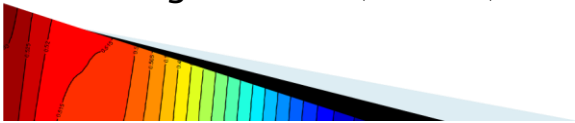
- ▶ In all programming languages, numbers and values are represented as literal values.
- ▶ Literal values have types as do variables. The following shows how literal values can be represented in C.
 - Integer values: 1, 2, -301, etc.
 - Real values: 1.0, 2.0, -310.345, 3.124e-21, etc.
 - Characters: 'a', 'b', 'z', '0', '\$', etc.
 - Character strings: "This is a string of characters"
- ▶ The range of values that can be represented vary according to compilers used.
 - For example, CodeBlocks uses 4 bytes to represent an integer, which means that integer values can range from -2147483648 to +2147483647



4

Integer Literal Values

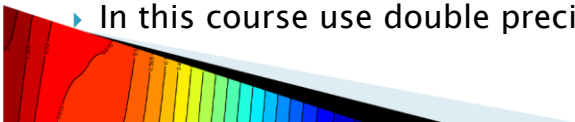
- ▶ By default, C treats integer literal values as signed values (with negative values)
 - Occupies 2 or 4 bytes according to the compiler used (CodeBlocks uses 4 bytes).
 - With 4 bytes an integer values can range from -2147483648 to $+2147483647$ or as unsigned values from 0 to 4294967295
- ▶ C programs cannot treat integer values outside its valid range.
- ▶ In this course we shall work with signed integer values (default).



5

Real Literal Values

- ▶ The real literal value in C contains three parts:
`xx.yyzz`
 - The decimal part (or integer), `xx`, to the left of the decimal point (mandatory including the decimal point).
 - The fraction part, `yy`, to the right of the decimal point,
 - The exponential part, `ezz`, that follows the fractional part. The exponential part multiplies `xx.yy` by 10^{zz}
- ▶ Real values in C are represented in either single precision or double precision (IEEE 764)
 - Single precision (type `float`) occupies 4 bytes
 - Double precision (type `double`) occupies 8 bytes
 - Literal values in CodeBlocks are represented using double precision.
- ▶ In this course use double precision.

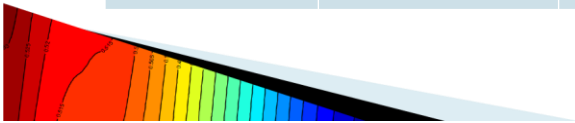


6

Character Literal Values

- ▶ As with all data, a character is represented using a binary code
 - The ASCII code (American Standard Code for Information Exchange).
 - Some examples of ASCII code:

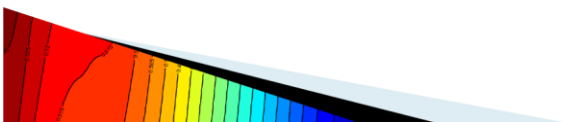
Character	Integer Equivalent	Binary Code
LF (new line)	10	0001010
SP (space)	32	0100000
0	48	0110000
A	65	1000001
A	97	1100001



7

Character Literal Values

- ▶ In C a character literal value normally consists of a letter surrounded by single quotes
 - Lower case characters: 'a', 'z'
 - Upper case characters: 'A', 'M'
 - Control characters: '\n' (new line), '\t' (tabulation), '\b' (carriage return)
 - Space: ' '
 - Punctuation: '?', '\'', '!', '?', '\\'
 - Note the use of the \ in the case of the characters ' and \.

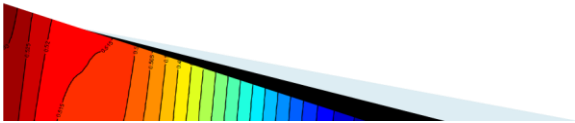


8

Character Strings

- ▶ The character string is not a simple type
 - It is composed of a sequence of characters.
 - We shall study more closely the character string in Module 4 after introducing arrays.
- ▶ Strings play an important role in programs
 - Recall `printf("Character string\n");`
- ▶ String literals consist of characters enclosed within a pair of double quotes.

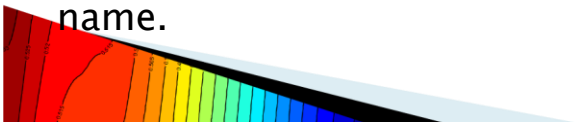
```
"Simple character string"  
"Line 1\n Line 2\n Line 3\n"  
"A string with\"double quotes\"\\n"
```



9

The Computer Variable

- ▶ The *variable* plays an important role in software, since it is the basic unit that contains data on which programs operate.
- ▶ Recall the three characteristics of a variable:
 - Has a **location** in memory that contains its binary value.
 - Has an **address** used to locate the variable in memory.
 - Has a **type** which defines how to interpret the binary value (also defines the number of bytes occupied by the variable).
- ▶ Recall the rules and conventions for variable name.

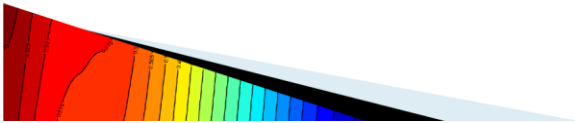


10

C Variables

- Variables must be declared via declarations.
 - Declarations are usually placed after the first { of main (or of a function definition) and before the first command.
 - A declaration contains a variable name and its type.
- There are 4 basic data types in C:

char	stores one character: a to z, A to Z, !, \$,...
int	stores an integer: 1, 101, -1462,...
float	stores a real number: 0.5, -122.34,...
double	stores a real number in double precision.



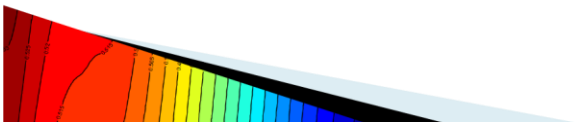
11

Symbolic Constants

- “Magic numbers” sprinkled throughout a program is generally considered to be an example of bad programming style.
- If a “magic number” must be used in the program, then it is best to associate the number to a symbolic constant that has a descriptive name and then to use the constant in the program.
- Symbolic constants are defined using the pre-processor directive `define` E.g.:

```
#define NBR_OF_CUBES 455
#define PI 3.141593
```

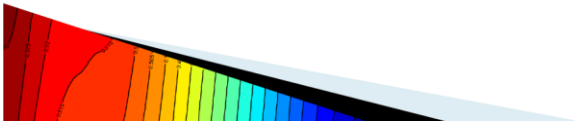
 - Pre-processor directives do not require a ; at the end.
 - The same rules for variables names are applied to symbolic constants, BUT convention dictates that symbolic constants names are in UPPER CASE as shown above.
 - Use the `_` character to make names readable.



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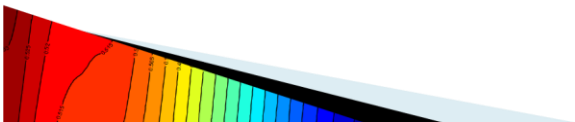
Symbolic Constants

- The pre-processor performs a textual substitution of the symbolic constant name with the associated quantity (directly to the right) everywhere in the code before compilation.
 - No memory space is used for a symbolic constant. **They are not variables.**
 - A program cannot change the value associated with a symbolic constant.
 - **Be careful with the ;**
E.g.: `#define MAX 100;`
will result in a substitution of `MAX` by `100;` everywhere in the program!



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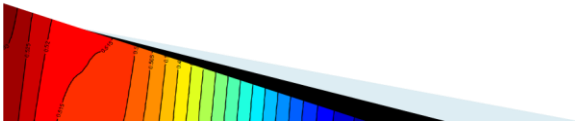
Topic 2: Arithmetic and Logic Expressions



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Evaluating arithmetic expressions

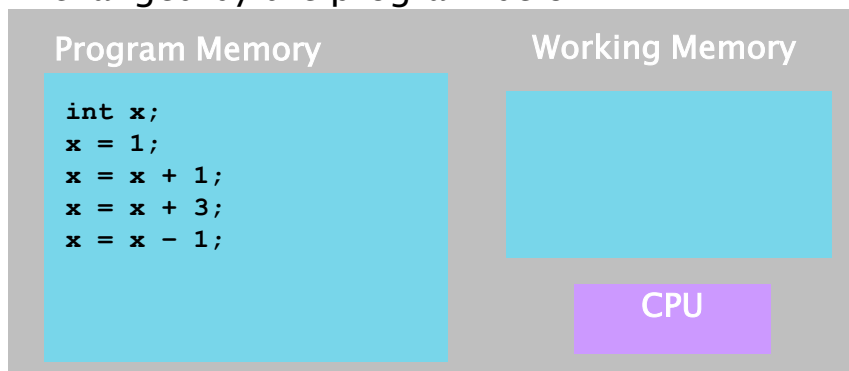
- ▶ Recall basic arithmetic expressions from last week
 - Binary operators: +, -, /, *
 - CPU applies operators one at a time
 - Assignment operator, =, assigns a value to a variable



15

Exercise: Increment/decrement instructions

- ▶ Show how the value of the variable `x` is changed by the program below.



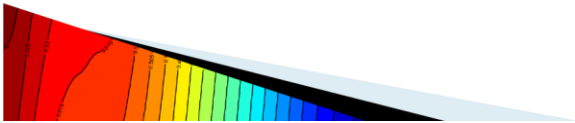
- ▶ The above operations are increment and decrement instructions.



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Increment/Decrement Operators

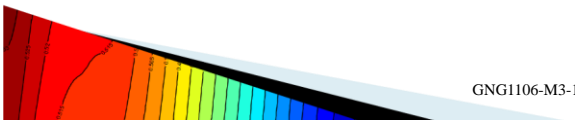
- ▶ There exists in C, special operators for adding or subtracting 1 from a variable
 - These operators are
 - The increment operator: `++`
 - The decrement operator: `--`.
 - These operators present subtleties that can easily lead to bugs.
 - You may use them, but at your own risk.



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Rules of Operator Precedence

- C evaluates arithmetic expressions according to the following rules of operator precedence.
 - 1 Contents of parentheses are evaluated first.
 - If there are many “levels” of parentheses, then the innermost pair is evaluated first; the next innermost pair is evaluated second...
 - If there are many pairs of parentheses on the same level then they are evaluated left to right.
 - 2 Negation (unary) is evaluated next.
 - 3 Multiplications, divisions and moduli are evaluated next.
 - If there are many then they are evaluated from left to right.
 - 4 Additions and subtractions are evaluated last.
 - If there are many, they are evaluated left to right.



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Examples of precedence

$$e = a * (b * (c + d));$$

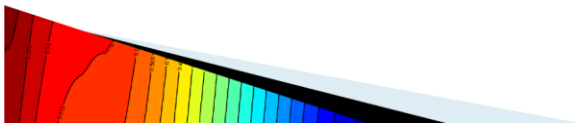
(3) (2) (1)

$$e = (a + b) * (c + d);$$

(1) (3) (2)

$$e = p * r \% q + w / x - y;$$

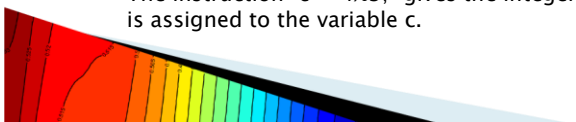
(1) (2) (4) (3) (5)



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Operations with integers

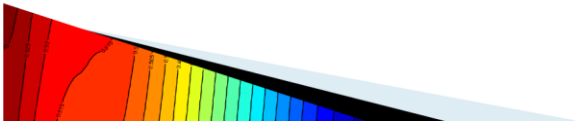
- ▶ **Operations with integer values gives integer values.**
 - "3 + 4" gives the integer value "7", and thus the instruction "c = 3 + 4;" assigns the value 7 to the variable c.
 - "3 * 4" gives the integer value "12", and thus the instruction "c = 3 * 4;" assigns the value 12 to the variable c.
- ▶ **The division of integer values gives only the quotient.**
 - The instruction "c = 3/4;" gives the integer value 0 (note that the remainder 3 is lost), i.e. the integer value 0 is assigned to the variable c.
 - The instruction "c = 4/3;" gives the integer value 1 (note the remainder 1 is lost), i.e. the integer value 1 is assigned to the variable c.
- ▶ **The operation that gives the remainder of an integer division is the modulo operation; in C the modulo operator is %.**
 - The instruction "c = 3%4;" gives the integer value 3, i.e. the integer value 3 is assigned to the variable c.
 - The instruction "c = 4%3;" gives the integer value 1, i.e. the integer value 1 is assigned to the variable c.



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Operations with real values

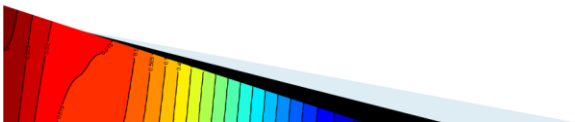
- ▶ **Operations with real values gives real values.**
 - "3.1 + 4.2" gives the real value "7.3", thus the instruction "c = 3.1 + 4.2;" assigns the value 7.3 to the variable c.
 - "3.1 * 4.2" gives the real value "13.02", thus the instruction "c = 3.1 * 4.2;" assigns the value 13.02 to the variable c.
 - "3.1 / 4.2" gives the real value "0.73809523809523814000", thus the instruction "c = 3.1 / 4.2;" assigns the value "0.73809523809523814000" to the variable c.
 - Note that using the Windows calculator, the result of the division is "0.73809523809523809523809523809524".
 - This means that the precision of the C program is less than that of the calculator. The value shown above was displayed using the instruction "printf("3.1 / 4.2 = %.15f\n", 3.1/4.2);".
 - Representation of real values are not exact in software. This can lead to errors in calculations and even logical errors.



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Operations with values of mixed types.

- ▶ In C, arithmetic operators applied to mixed types (i.e. with integers and real values) use an implicit rule of promotion. The rule of promotion is applied with binary operators that operate on 2 values of different type.
- ▶ When an operator is applied to one real value and one integer value, the integer value is converted (i.e. promoted) to a real value before applying the operator.
- ▶ In the case of the operation "3 + 4.1", the integer value is first converted to "3.0" and then added to "4.2" to give the value "7.1".
- ▶ In the case of the operation "3/4.1", the integer value is first converted to "3.0" and then divided by "4.1" to give the value "0.73170731707317083000"



22

Division of integers

- Suppose that `a`, `b` and `c` are of type `int`.

E.g.: `a = 3;`

`b = 4;`

`c = a / b;` → `c` 0

`c = b / a;` → `c` 1

- The division of integers returns the quotient.

The Modulus

- Operation that computes the remainder of a division of integers. Suppose that `a`, `b` and `c` are of type `int`.

E.g.: `a = 3;`

`b = 4;`

`c = a % b;` → `c` 3

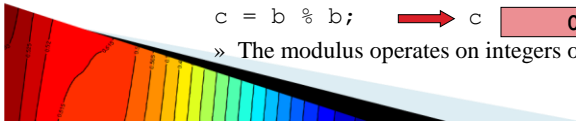
`c = -a % -b;` → `c` -3

Sign of remainder is sign of numerator.

`c = b % a;` → `c` 1

`c = b % b;` → `c` 0

» The modulus operates on integers only.



23

Mixed Type Arithmetic

- An expression that contains variables of many types will be converted in memory by the C compiler according to the implicit rule of promotion.

- The promotion hierarchy of our 4 basic data types is as follows:

`double` ← highest type

`float`

`int`

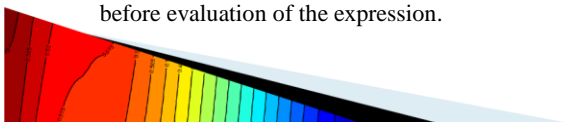
`char` ← lowest type

- The hierarchy is organized according to the amount of information that can be stored in the data type.

➤ A double variable can contain the same amount of information as all of the “lower” data types.

- The implicit rule of promotion followed by the C compiler when evaluating mixed type expressions is:

- All variables in an expression are promoted to the highest type (in temporary memory) before evaluation of the expression.



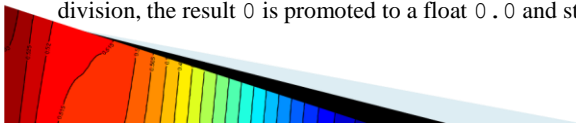
24

- Consider the following examples of mixed type expressions.

```
E.g.:  int a, b, c;
        float x, y, z;
        a = 3;
        b = 4;
        x = 1.0;
        y = 2.5;
```

No conversions	<code>c = a + b;</code>	→	c	7	
No conversions	<code>z = x + y;</code>	→	z	3.5	
1 conv. from int to float	<code>z = a + b;</code>	→	z	7.0	
1 conv. from int to float	<code>z = x + a;</code>	→	z	4.0	
1 conv. from float to int	<code>c = x + y;</code>	→	c	3	Loss of information!
2 conversions	<code>c = x + a;</code>	→	c	4	
1 conv. from int to float	<code>z = a / b;</code>	→	z	0.0	

- Care must be taken when storing a real number into an `int`. The real number will be truncated and only the integer portion will be stored.
- Careful with the division of integers; in the last example, `a / b` is evaluated as an integer division, the result 0 is promoted to a float `0.0` and stored in `z`.



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The Cast Operator

- The unary cast operators can be used to force the type conversion of a variable.

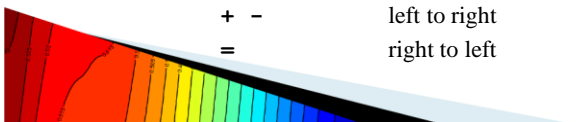
E.g.: (same variable definitions as in the previous example)

```
z = (float) a / b; → z 0.75
```

- `(float) a` forces the conversion of `a` to type `float`,
- according to the implicit rule of promotion, `b` is converted to type `float`,
- the division is then evaluated as a division of real numbers and the result is assigned to `z` which is of type `float`.
- A unary operator operates on one argument only: the argument directly to its right.
- A cast operator exists for each data type in C: `(double)`, `(float)`, `(int)`, `(char)`.

Summary of Hierarchy and Associativity of Arithmetic Operators

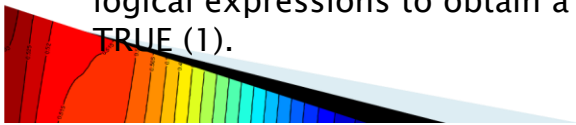
```
()          left to right
- (type)    right to left
* / %       left to right
+ -         left to right
=           right to left
```



26

Logical Expressions

- ▶ Logical expressions give a TRUE / FALSE result
 - In C FALSE is the value 0 and TRUE any other value
- ▶ We shall see soon that logical expressions plays a role in programming “decisions” and “repetitions”.
- ▶ Logical expressions can compare values
- ▶ Logical expressions can also include a number of comparisons
- ▶ Expressions involving operators comparison operators such as “equal”, “greater than”, and logical operators such as AND, OR, and NOT
- ▶ Like arithmetic expressions the computer evaluates logical expressions to obtain a value: FALSE (0) or TRUE (1).



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Logical Expressions in C

Relational, Equality and Logical Operators in C

- The following relational operators exist in C:

Operation	C Operator	C Example	Description
x>y	>	x > y	is greater than
x<y	<	x < y	is less than
x≥y	>=	x >= y	is greater or equal to
x≤y	<=	x <= y	is less than or equal to

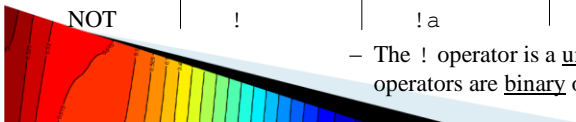
- The following equality operators exist in C:

Operation	C Operator	C Example	Description
x=y	==	x == y	is equal to
x≠y	!=	x != y	is not equal to

- The following logical operators exist in C:

Operation	C Operator	C Example	Description
AND	&&	a && b	and
OR		a b	or
NOT	!	!a	not

– The ! operator is a unary operator while the && and || operators are binary operators.

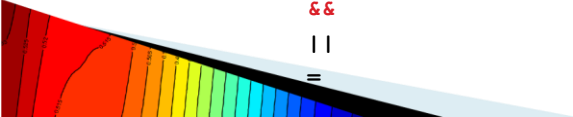


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Rules of Logical Operator Precedence in C

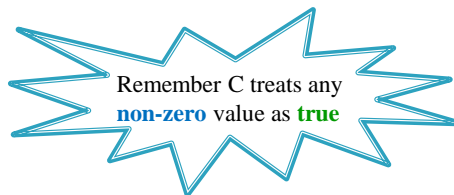
- In a logical expression,
 - the logical not ! operator has highest precedence,
 - the relational operators have the next highest precedence,
 - then come the equality operators,
 - then the logical && operator,
 - and finally the logical || operator which has the lowest precedence.
- The following table summarizes in order of precedence the associativity of all the C operators that we have seen to date.

()	left to right	
.	left to right	
- ! (type)	right to left	unary operators
* / %	left to right	
+ -	left to right	
< <= > >=	left to right	
== !=	left to right	
&&	left to right	
	left to right	
=	right to left	



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- ▶ Parentheses can be used in a logical expression. They have the highest precedence and thus can be used to change the precedence of logical operations just like in an arithmetic expression.
- ▶ The above rules of precedence and associativity are followed by the C compiler when evaluating expressions that contain an arithmetic part and a logical part.
 - You are **strongly encouraged to use parentheses in order to clarify such mixed expressions.**
- ▶ The result of a logical expression can only be **true** or **false**.
- ▶ In C, a logical expression that evaluates to **false** has the integer result **0** and a logical expression that evaluates to **true** has the integer value **1**.



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- In C, a **non-zero** integer value (1, 2, -1...) is interpreted as being **true** in a logical expression. Suppose that the variables `x` and `y` are of type `int`; shown below are the truth tables for our logical operators in C, operating on the variables `x` and `y`.

- Truth table for the logical and:

X	Y	X and Y
T	T	T
T	F	F
F	T	F
F	F	F

In a C expression

x	y	x && y
NZ	NZ	1
NZ	0	0
0	NZ	0
0	0	0

- Truth table for the logical or:

X	Y	X or Y
T	T	T
T	F	T
F	T	T
F	F	F

In a C expression

x	y	x y
NZ	NZ	1
NZ	0	1
0	NZ	1
0	0	0

- Truth table for the logical not:

X	not X
T	F
F	T

In a C expression

x	!x
NZ	0
0	1

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- Here are a few examples of valid logical expressions in C:

```
int k = -3, m = -4;
float a = 5.5, b = 1.5;
a < 10.5 + k;
a + b >= 6.5;
k != a - b;
b - k > a;
!( a == 3 * b );
-k <= k + 6;
a < 10 && a > 5;
k / m >= 0.75;
```

Result

1
1
1
0
1
1
1
0

- In C, logical expressions always evaluate to the integers **1** or **0** (for **true** or **false**).

→ We can use a variable of type `int` to store the result of a logical expression and treat this variable as a logical variable.

E.g.: `int log_var, k = -3, l = -4;`

`float a = 5.5, b = 1.5;`

`log_var = a < 10.5 + k;`

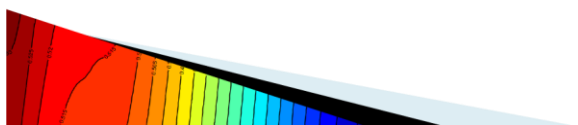
`log_var = (a + b) >= 6.5;`

→ log_var **1**

→ log_var **1**

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Topic 3: More on Input and Output

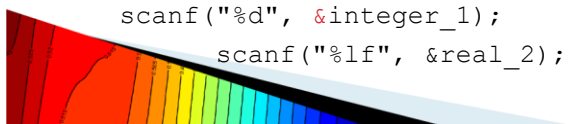


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Review of Basic Input and Output

- C standard functions are used for input/output: `printf` to display text on the console, and `scanf` to read and convert typed text from the keyboard.
 - The header file `stdio.h` contains the required prototypes and definitions
- Conversion specifiers are used by both functions for converting text to and from data values
 - `%d` converts integer values (type `int`) used by both `printf` and `scanf`
 - `%f` converts real values (type `double`) for `printf`
 - `%lf` converts real values (type `double`) for `scanf`
- Recall that in the case of `scanf` the `&` operator is used to pass the address of the variable for storing values read from the keyboard. In the case of the `printf`, the value of the variable is passed to the function.
- Examples:

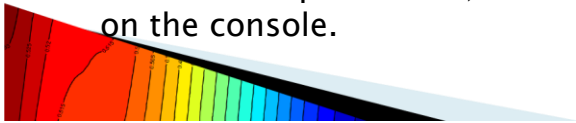
```
printf("The integer value of var is %d\n",var)
printf("The sum is %f\n", sum);
scanf("%d", &integer_1);
scanf("%lf", &real_2); // real_2 is a double
```



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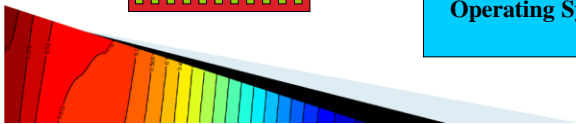
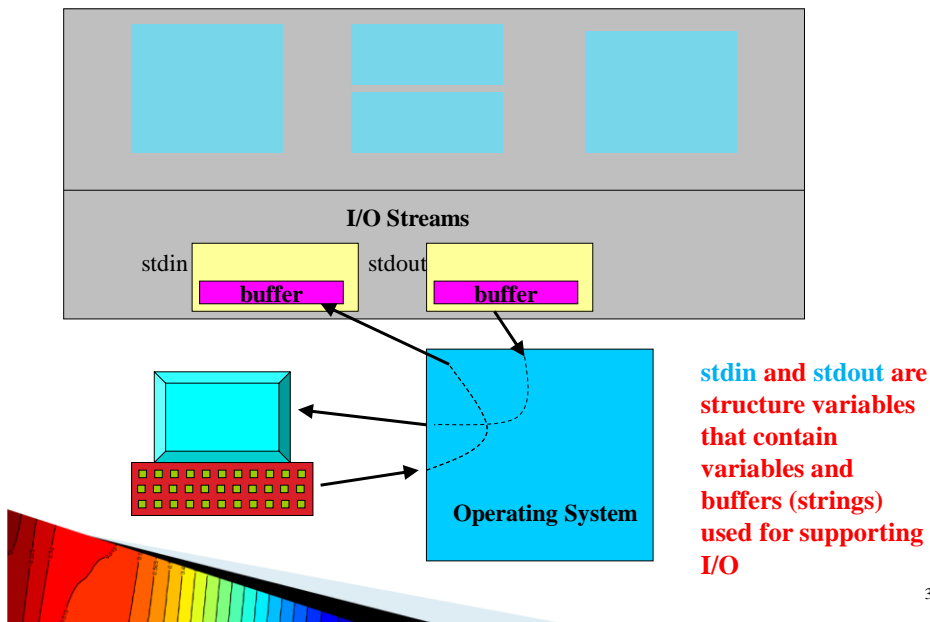
Programming Model and I/O

- ▶ For input, the operating system fills a « buffer » with a string
 - See the next slide
 - The characters typed up to the carriage return are stored in the buffer (`stdin` structure this is the standard input stream)
 - The string becomes available to the program only after the carriage return
 - The conversion specifiers are used by `scanf` to know how to convert the characters in the string to the desired values
- ▶ For output, `printf` will convert values passed and insert into a string (buffer, `stdout` structure is the standard output stream) used by the OS for display on the console.



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Programming Model and I/O



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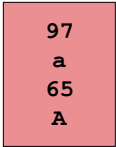
Character Output

- ▶ Recall that
 - A content of a variable of type `char` can be interpreted as a character or an integer
 - A variable of type `int` containing an integer in the range 0 through 127 inclusively, can be interpreted as being a character or an integer.
 - The content of a variable of type `int` can be interpreted as an integer.
- ▶ The conversion specifier `%d` is to be used when we wish to print out the content of a variable as an integer and the conversion specifier `%c` is used when we wish to interpret the variable as a character.

E.g.:

```
char character_1 = 'a';
int integer_1 = 65;
printf("%d\n", character_1);
printf("%c\n", character_1);
printf("%d\n", integer_1);
printf("%c\n", integer_1);
```

On Screen



```
97
a
65
A
```

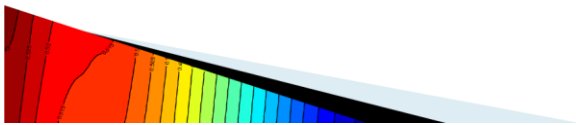
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Character input: the input stream

- ▶ Recall that the input stream provides the buffer containing the input data
 - `scanf()` is used to read a character from this buffer using the `%c` code conversion specifier
 - E.g.:
- ```
scanf("%c", &character_1);
scanf("%c", &integer_1);
```
- ▶ Consider the entry of a single character:
    - We type the character on the keyboard and then we hit the enter or carriage return key to signify that we have completed typing in the entry.
      - ✓ This signals the OS that the data can be passed to the program in the buffer of the input stream.
    - The carriage return inserts the character new line (ASCII equivalent 10) into the input stream after our typed character.
    - The input stream thus contains two item:
      - The character typed in and the new line symbol (ASCII equivalent 10).
  - ➔ When we read in a character using `scanf`, we must usually clear the input stream to get rid of the new line symbol; this can be achieved by invoking the function `fflush`.

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- ▶ The input stream is referenced with `stdin`, which is used as the argument in `fflush`.
  - E.g.: `fflush(stdin);`
  - The header file `stdio.h` contains the prototype of `fflush` and the definition of `stdin`
  - `stdin` stands for standard input stream; it is a pointer that points to the standard input that contains the memory buffer where the keyboard entries are stored by the OS.
- ▶ It is good practice to clear the input stream using `fflush` before/after reading in characters.

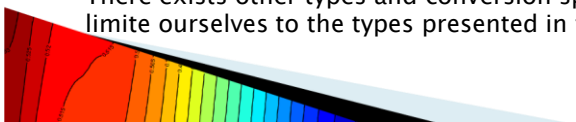


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### Summary of Conversion Specifiers to be Used in printf and scanf

| Type   | printf                          | scanf                                |
|--------|---------------------------------|--------------------------------------|
| char   | <code>%c, %d, %i</code>         | <code>%c</code>                      |
| int    | <code>%d, %i</code>             | <code>%d, %i</code>                  |
| float  | <code>%f, %e, %E, %g, %G</code> | <code>%f, %e, %E, %g, %G</code>      |
| double | <code>%f, %e, %E, %g, %G</code> | <code>%lf, %le, %lE, %lg, %lG</code> |

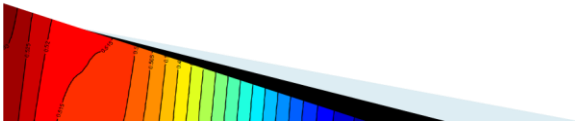
- `%i` is equivalent to `%d`
- `%d` and `%i` converts the char to an integer value for `char`
- Note the differences for conversion specifiers for a `double` and `float`. The same specifiers are used for `printf`, but for `scanf`, an “l” is added for the `double`.
- The conversion specifier `%e` prints out the number in scientific notation: `1.0e0`
- The conversion specifier `%E` prints out the number in scientific notation: `1.0E0`
- The conversion specifier `%g` prints out the number in `%f` or in `%e`
- The conversion specifier `%G` prints out the number in `%f` or in `%E`
- There exists other types and conversion specifiers in C, but we shall limite ourselves to the types presented in this course.



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## Example: characters.c

- ▶ Program shows how `char` and `int` variables can be treated as both integers and characters.
- ▶ Program demonstrates reading characters with `scanf` and how `fflush` is used to clear the input buffer.

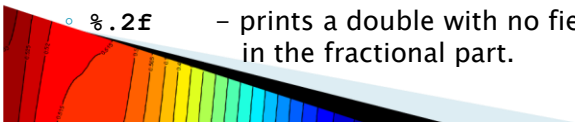


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## On Formatting Output

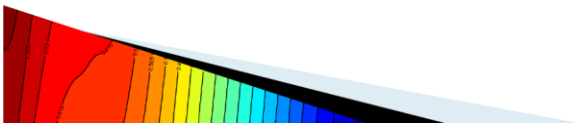
- ▶ The following shows examples on formatting numbers to help
  - Align them within fields to create tables
  - Determine how many decimal numbers to use in the fractions of real numbers.
- ▶ Simple presentation: `%w.pc` where
  - `w` defines a minimum field width (minimum amount of space the value occupies)
  - `p` precision (defines the number of decimal numbers in the fraction of a real number)
  - `c` the conversion character (e.g. `f`, `d`, etc.)
- ▶ Examples:
  - `%10d` – prints an integer value in a field of 10 characters,
  - `%10.2f` – prints a double value in a field of 10 characters with 2 numbers in the fractional part.
  - `%.2f` – prints a double with no field definition and 2 numbers in the fractional part.

See C  
Reference card  
for details



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# Topic 4 Math Library



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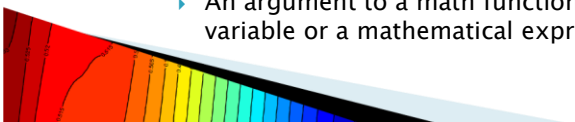
## Standard Math Functions

- ▶ The following slide provides a list standard C math functions.
  - The most popular math functions are available.
  - Google them to get details or consult the appendix of the recommended text.
- ▶ The preprocessor directive `#include <math.h>` provides the C compiler with definitions used by the standard math functions in the program. This directive is normally placed after the directive `#include <stdio.h>` before `main()`.
- ▶ All standard math functions except three (`frexp`, `ldexp` and `modf`) require arguments of type `double` and all standard math functions return a number of type `double`.
- ▶ The value returned by a math function can be
  - assigned to a variable for future use:

```
x = sin(angle);
```
  - used in an arithmetic expression, or as an argument sent in to another function:

```
c = sqrt(PI + pow(z, 3.0));
```

    - ▶ An argument to a math function can be a symbolic constant, a variable or a mathematical expression.



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- ▶ The rules of promotion are applied to the arguments of math functions if they are not of type `double`. These same rules are applied to the value returned by the function if it is not stored into a variable of type `double`.
- ▶ Some of the most commonly encountered math functions:

| Math Function | C Math Function        | Note on Usage                                                               |
|---------------|------------------------|-----------------------------------------------------------------------------|
| $\sqrt{x}$    | <code>sqrt(x)</code>   | $x$ must be $\geq 0.0$                                                      |
| $x^y$         | <code>pow(x, y)</code> |                                                                             |
| $e^x$         | <code>exp(x)</code>    |                                                                             |
| $\log_e x$    | <code>log(x)</code>    |                                                                             |
| $\log_{10} x$ | <code>log10(x)</code>  |                                                                             |
| $ x $         | <code>fabs(x)</code>   |                                                                             |
| $\sin(x)$     | <code>sin(x)</code>    | } $x$ is in radians.                                                        |
| $\cos(x)$     | <code>cos(x)</code>    |                                                                             |
| $\tan(x)$     | <code>tan(x)</code>    |                                                                             |
| $\arcsin(x)$  | <code>asin(x)</code>   | -1 $\leq x \leq 1$ and $-\pi/2 \leq \text{return} \leq \pi/2$ , in radians. |
| $\arccos(x)$  | <code>acos(x)</code>   | -1 $\leq x \leq 1$ and $0 \leq \text{return} \leq \pi$ , in radians.        |
| $\arctan(x)$  | <code>atan(x)</code>   | $-\pi/2 \leq \text{return} \leq \pi/2$ , in radians.                        |
| $\sinh(x)$    | <code>sinh(x)</code>   | } Hyperbolic functions.                                                     |
| $\cosh(x)$    | <code>cosh(x)</code>   |                                                                             |
| $\tanh(x)$    | <code>tanh(x)</code>   |                                                                             |

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- ▶ The function `ceil(x)` rounds  $x$  to the smallest integer that is greater than or equal to  $x$ .

◦ E.g.:

|                         |             |
|-------------------------|-------------|
| <code>ceil(9.0)</code>  | yields 9.0  |
| <code>ceil(9.2)</code>  | yields 10.0 |
| <code>ceil(9.5)</code>  | yields 10.0 |
| <code>ceil(9.8)</code>  | yields 10.0 |
| <code>ceil(-9.8)</code> | yields -9.0 |
| <code>ceil(-9.5)</code> | yields -9.0 |
| <code>ceil(-9.2)</code> | yields -9.0 |
| <code>ceil(-9.0)</code> | yields -9.0 |

Returns an integer as a double.

- ▶ The function `floor(x)` rounds  $x$  to the largest integer that is less than or equal to  $x$ .

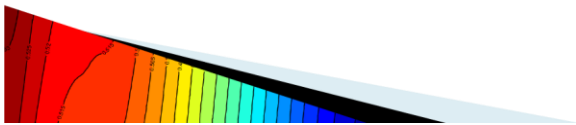
◦ E.g.:

|                          |              |
|--------------------------|--------------|
| <code>floor(9.0)</code>  | yields 9.0   |
| <code>floor(9.2)</code>  | yields 9.0   |
| <code>floor(9.5)</code>  | yields 9.0   |
| <code>floor(9.8)</code>  | yields 9.0   |
| <code>floor(-9.8)</code> | yields -10.0 |
| <code>floor(-9.5)</code> | yields -10.0 |
| <code>floor(-9.2)</code> | yields -10.0 |
| <code>floor(-9.0)</code> | yields -9.0  |

Returns an integer as a double.

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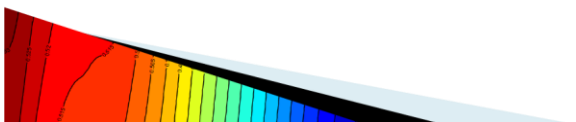
# Topic 5: Debugging



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## Types of Errors Encountered in Computing

- ▶ **Syntax errors.**
  - They are C “grammar and spelling” errors.
  - They occur during compilation.
  - The compiler does not understand what you are trying to do.
  - The compiler usually provides a clue as to where the error is.
  - Re-compile your code after correcting a few syntax errors since a single error often causes many others to occur.
- ▶ **Execution and logical errors.**
  - The program compiles without error but it does not run as expected.
  - May have a fatal error during execution such as a division by zero
    - E.g.: `c = a / b;` with `b` containing 0.
  - May have logical errors in instructions.
  - Debugging is the art of finding and correcting logical errors



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## Debugging Logical Errors

- ▶ To find and correct logical errors, be systematic
  - Trace the program (e.g. using programming model) to see how variables change during the execution of the program.
  - Add `printf` instructions in your program to output values of variables to trace how they change.
  - Use the debugger if the programming environment has one (ours does).
- ▶ Finding where variables have unexpected results allows you to zero in on statements that are causing the errors
- ▶ Golden Rule: when debugging, make changes for a reason to your code to correct the error.

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## Next Module

- ▶ Topic 1: Structures
- ▶ Topic 2: Arrays
- ▶ Topic 3: More Standard C Functions

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