

$$R_s = R_u$$

$$T_1 = 10^\circ\text{C} = 283.15\text{K}$$

$$P_1 = 120\text{kPa} \quad P_2 = 800\text{kPa}$$

$$P_1 V_1^n = P_2 V_2^n$$

Question #3 [15 pts]

Argon gas is compressed in a polytropic process with $n = 1.20$ contained in a piston-cylinder device. The initial temperature and pressure are 10 °C and 120 kPa, respectively, and the final pressure is 800 kPa. Assume $R_s = 0.2081 \text{ kJ/kg}\cdot\text{K}$ and average constant specific heats $c_v = 0.3122 \text{ kJ/kg}\cdot\text{K}$. Calculate:

a) the initial and final specific volume, in m^3/kg

$$P_1 V_1 = m R_s T_1 \quad \left. \begin{array}{l} P_2 V_2 = m R_s T_2 \\ P_1 V_1^n = P_2 V_2^n \end{array} \right\} \begin{array}{l} V_1 = \frac{R_s T_1}{P_1} = \frac{(0.2081)(283.15\text{K})}{120\text{kPa}} = 0.4908 \text{ m}^3/\text{kg} \\ V_2 = 0.100998 \text{ m}^3/\text{kg} \end{array}$$

b) the final temperature, in K

$$T_2 = \frac{P_2 V_2}{R_s} = \frac{(800)(0.100998)}{0.2081} = 422.8 \text{ K}$$

(-0.5)

b) the specific work required, in kJ/kg

$$W_{1-2} = \int_1^2 P dv = \frac{P_2 V_2 - P_1 V_1}{1-n} = \frac{(800)(0.100998) - (120)(0.4908)}{1-1.2} = -109.51 \text{ kJ/kg}$$

c) the change of specific internal energy, in kJ/kg

$$\Delta U = \int_1^2 c_v dT = c_v (T_2 - T_1) = 0.3122 (422.8 - 283.15) = 43.6 \text{ kJ/kg}$$

ok

d) The total specific heat transferred, in kJ/kg

$$\Delta U = \delta Q - \delta W \quad \delta Q = \Delta U - \delta W = 43.6 - (-109.51) = 153.11 \text{ kJ/kg}$$

e) What will be the required specific work, in kJ/kg, if the compression of argon from 10 °C and 120 kPa to the final pressure of 800 kPa is done in an isothermal process?

$$W_{1-2} = \int_1^2 P dv = P_1 V_1 \ln\left(\frac{V_2}{V_1}\right) = (120)(0.4908) \ln\left(\frac{0.100998}{0.4908}\right) = -93.11 \text{ kJ/kg}$$

(12.5/15)