

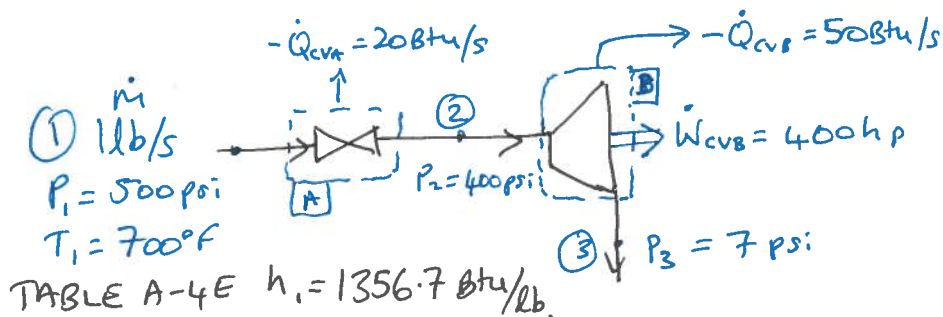
ENGG 311 (Fall 2016)
QUIZ 4

Time Allowed: 30 minutes

14th November 2016

Steam at 500 lbf in^{-2} and 700°F flows through a pressure reducing valve and steam turbine operating in series. At the valve outlet (corresponding to the turbine inlet) the pressure is 400 lbf in^{-2} , and at the turbine outlet the pressure is 7 lbf in^{-2} . At a steam flow rate of 1 lb/s , the work developed by the turbine is 400 hp , and the heat transfer rates from the valve and turbine are 20 Btu/s and 50 Btu/s respectively. The process is operating at steady state and kinetic and potential energy effects are negligible. Determine:

- a) the specific enthalpy of the steam at the valve outlet (Btu/lb),
 b) the temperature at the valve outlet ($^\circ\text{F}$),
 c) the specific enthalpy of the steam at the turbine outlet (Btu/lb),
 and d) the state of the steam at the turbine outlet: if it is superheated determine its temperature ($^\circ\text{F}$), if it is a vapour-liquid mixture determine its temperature ($^\circ\text{F}$) and quality.



(a) 1st LAW, CVA, steady state KE + PE negligible.

$$\dot{Q}_{CVA} = \dot{m}(h_2 - h_1) \quad \therefore h_2 = h_1 + \frac{\dot{Q}_{CVA}}{\dot{m}}$$

$$h_2 = 1356.7 \frac{\text{Btu}}{\text{lb}} + \frac{-20 \text{ Btu} \cdot \text{s}}{1 \text{ s} \cdot \text{lb}} = \underline{\underline{1336.7 \frac{\text{Btu}}{\text{lb}}}}$$

(b) TABLE A-4E $P_2 = 400 \text{ psi}$ $T = 600^\circ\text{F}$ $h = 1306.6 \text{ Btu/lb}$
 $T = 700^\circ\text{F}$ $h = 1362.5 \text{ Btu/lb}$

Interpolation

$$T_2 = \left[600 + \left(\frac{1336.7 - 1306.6}{1362.5 - 1306.6} \right) \cdot 100 \right]^\circ\text{F} = \underline{\underline{653.8^\circ\text{F}}}$$

(c) 1st LAW C.V. B

$$\dot{Q}_{CTB} - \dot{W}_{CTB} = \dot{m}(h_3 - h_2)$$

$$\therefore h_3 = h_2 + \frac{(\dot{Q}_{CTB} - \dot{W}_{CTB})}{\dot{m}}$$

$$\dot{W}_{CTB} = 400 \text{ hp} \cdot \frac{2545 \text{ Btu}}{1 \text{ hp} \cdot \text{h}} \cdot \frac{1 \text{ h}}{3600 \text{ s}} = 287.78 \text{ Btu/s}$$

$$\therefore h_3 = \left[1336.7 + \frac{(-50 - 287.78)}{1} \right] \frac{\text{Btu}}{\text{lb}}$$

$$\therefore h_3 = \underline{\underline{1003.92 \frac{\text{Btu}}{\text{lb}}}}$$

Mark
20

(d) State ③ $P_3 = 7 \text{ psi}$ $h_3 = 1003.92 \text{ Btu/lb.}$

TABLE A-3E 7 psi : $h_f = 144.8 \frac{\text{Btu}}{\text{lb}}$ $h_g = 1136.9 \text{ Btu/lb.}$

\therefore Saturated-vapor - liquid mixture. at $T_{\text{sat}} = T_3 = \underline{\underline{176.82^\circ\text{F.}}}$

$$x_3 = \frac{h_3 - h_f}{h_{fg}} = \left(\frac{1003.92 - 144.8}{992.1} \right) = \underline{\underline{0.8660}}$$

or 86.6%