

Université d'Ottawa
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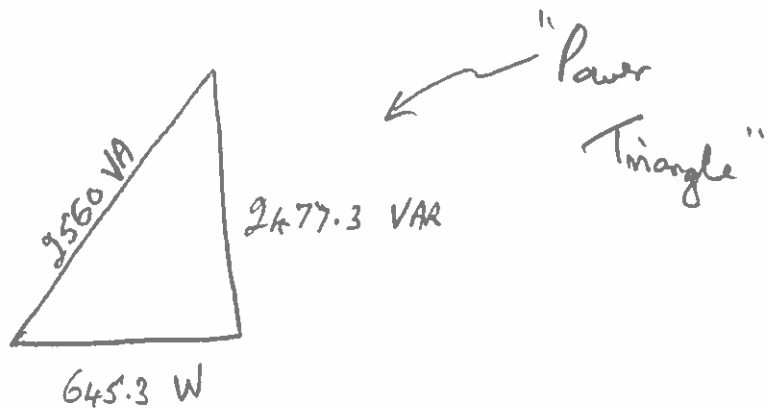
University of Ottawa
Faculty of Engineering

School of Electrical Engineering
and Computer Science

ELG 3316

Electric Machines & Power Systems

Answers / Solutions to Assignment #1



(e). We can see from \tilde{S} that $\phi_{PF} = 75.4^\circ$.

So the power factor is $PF = \cos(75.4^\circ) = 0.252$

Since $\phi_{PF} > 0$, we know that it is a lagging PF.

(f). In order to have a unity power factor (i.e. $PF = 1$)

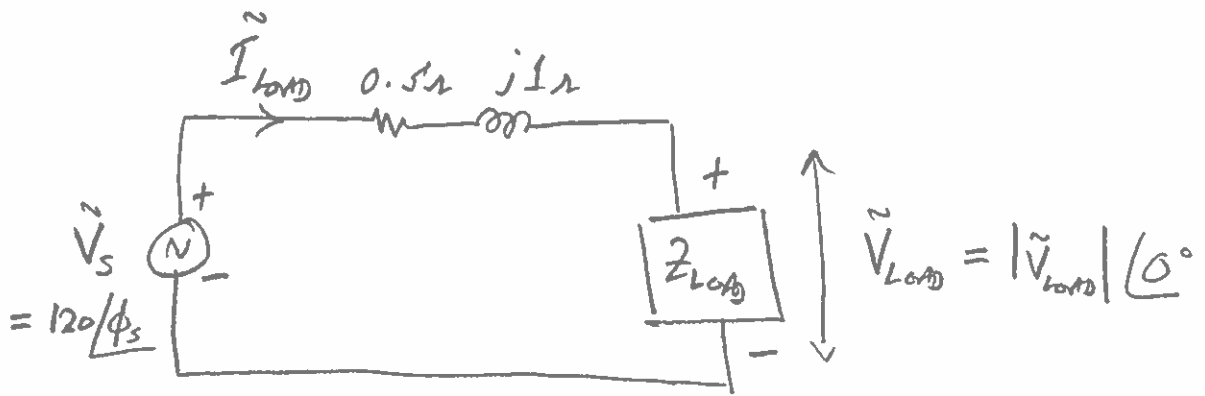
we must have $Q = 0$. At present $Q = 2477.3$.

So we must add a capacitor which will provide

a $Q = -2477.3$.

See Simulation Lab.

Q4



- No currents or voltages have been specified with a particular phase angle. Since phases are always relative we are free to select a phase reference with respect to which all other phases will be calculated. In this solution we have chosen the phase of the load voltage as the reference, with its phase at 0° . We cannot then select the phase of any other voltages or currents; these must be calculated. We have written the phase of \vec{V}_s as being ϕ_s ; it must be calculated.

- $|\vec{I}_{Load}| = 8$ ← This is given. But we don't know its phase. Thus we don't know \vec{I}_{Load} .

$\cos \phi_{PF} = 0.85$ lagging ← The load pf is given.

$\phi_{PF} = \cos^{-1} 0.85$
 $= 31.8^\circ$

So $\phi_{PF} > 0$

The phase of \tilde{V}_{LOAD} is $\phi_v = 0^\circ$

The phase of \tilde{I}_{LOAD} is ϕ_i , but is not yet known.

$$\text{Now by definition } \phi_{PF} = \phi_v - \phi_i \Rightarrow \phi_i = -31.8^\circ$$

\uparrow \uparrow
 31.8° 0°

$$\therefore \tilde{I}_{LOAD} = 8 \angle -31.8^\circ$$

• Analyze KVL around the circuit. This gives us

$$\tilde{V}_s - \tilde{I}_{LOAD} (0.5 + j1) - \tilde{V}_{LOAD} = 0$$

\uparrow \uparrow \uparrow
 $120 \angle \phi_s$ $(8 \angle -31.8^\circ) (0.5 + j1)$ $|\tilde{V}_{LOAD}| \angle 0^\circ$

\downarrow \downarrow \downarrow

120 cos ϕ_s 7.61 + j4.69 $|\tilde{V}_{LOAD}| \cos 0^\circ + |\tilde{V}_{LOAD}| \frac{\sin 0^\circ}{0} = 0$
+ j120 sin ϕ_s

Equate Real parts of both sides: $120 \cos \phi_s - 7.61 - |\tilde{V}_{LOAD}| = 0$ — (1)

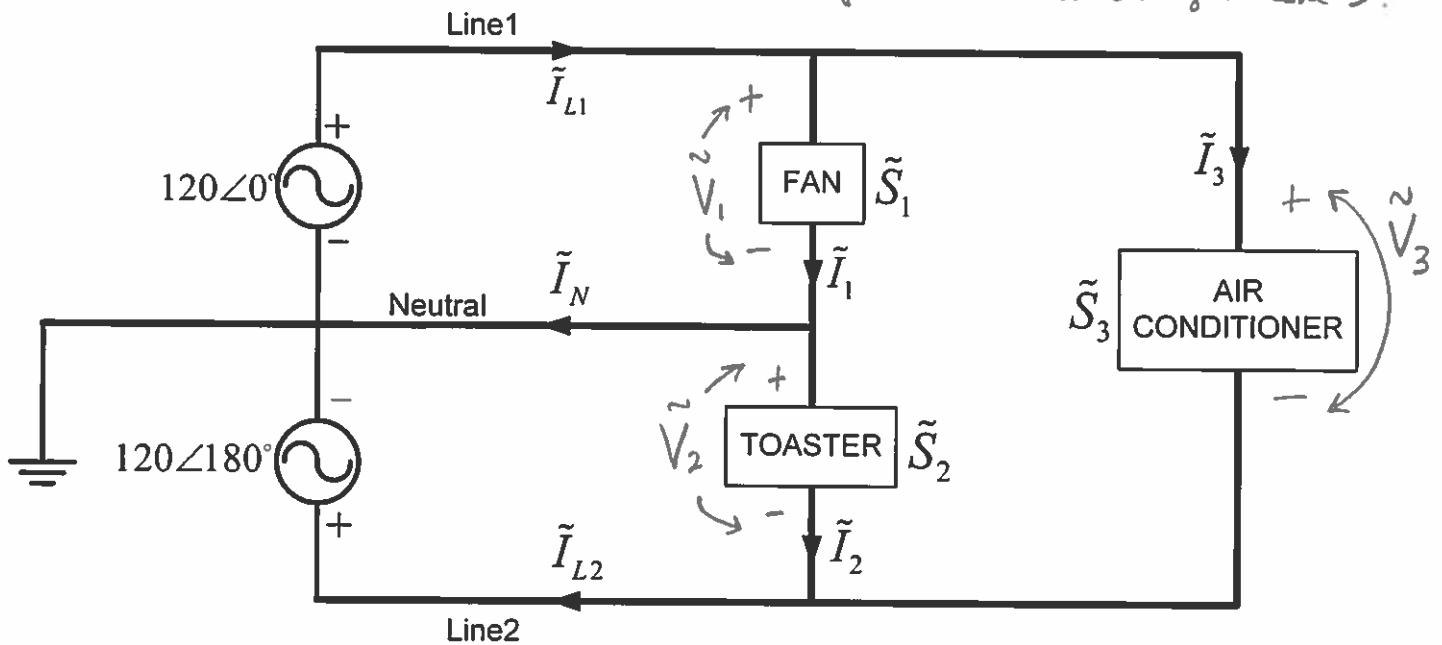
Equate Imag. parts of both sides: $120 \sin \phi_s - 4.69 = 0$ — (2)

$$\textcircled{2} \text{ gives } \phi_s = \sin^{-1} \left(\frac{4.69}{120} \right) = 2.24^\circ$$

If we substitute this into $\textcircled{1}$ it gives us

$$|\tilde{V}_{\text{LOAD}}| = 112.28 \text{ Volts.}$$

Q4 (Note that I will be using some additional symbols, and so have indicated them on the circuit diagram. This must always be done).



• We can immediately write $\tilde{V}_1 = 120 \angle 0^\circ$ and $\tilde{V}_2 = -120 \angle 180^\circ$
 Just apply KVL.

• Fan $\tilde{V}_1 = 120 \angle 0^\circ$
 $|\tilde{I}_1| = 5$, but $\cos \phi_{PF} = 0.8$ lagging $\Rightarrow \phi_{PF} = 36.87^\circ \Rightarrow \phi_i^{(1)} = -36.87^\circ$
 $\therefore \tilde{I}_1 = 5 \angle -36.87^\circ$

• Toaster $\tilde{V}_2 = -120 \angle 180^\circ = 120 \angle 0^\circ$
 $|\tilde{I}_2| = 11$, and unity PF implies current in phase with voltage, so $\phi_i^{(2)} = 0^\circ$

Make sure you know why

$\therefore \tilde{I}_2 = 11 \angle 0^\circ$

• Air Con KVL gives $\vec{V}_2 + \vec{V}_1 - \vec{V}_3 = 0$

$$\therefore \vec{V}_3 = 120 \angle 0^\circ + 120 \angle 0^\circ = 240 \angle 0^\circ$$

$$|\vec{I}_3| = 24. \text{ Power factor is } 0.85 \text{ lagging.}$$

$$\text{Thus } \phi_{pf} = 31.8^\circ \Rightarrow \phi_i = -31.8^\circ$$

$$\therefore \vec{I}_3 = 24 \angle -31.8^\circ$$

(a).

$$\vec{S}_{\text{TOTAL}} = \vec{S}_1 + \vec{S}_2 + \vec{S}_3$$

$\vec{V}_1 \vec{I}_1^*$
 \downarrow
 $(120)(5) \angle 36.87^\circ$

$\vec{V}_2 \vec{I}_2^*$
 \downarrow
 $(120)(11) \angle 0^\circ$

$\vec{V}_3 \vec{I}_3^*$
 \downarrow
 $(240)(24) \angle 31.8^\circ$

~~⊗~~
DON'T FORGET
THE CONJUGATE
OPERATION!

$$\therefore \vec{S}_{\text{TOTAL}} = \underbrace{6684}_{P_{\text{TOTAL}}} + j \underbrace{3413}_{Q_{\text{TOTAL}}} = 7505 \angle 27^\circ$$

Total power consumed by house is $P_{\text{TOTAL}} = \underbrace{6684 \text{ W}}_{6.684 \text{ kW}}$

$$(b). \quad \tilde{I}_{L1} = \tilde{I}_1 + \tilde{I}_3 = 5 \angle -36.87^\circ + 24 \angle -31.8^\circ = 29 \angle -32.8^\circ \text{ A}$$

$$\tilde{I}_{L2} = \tilde{I}_2 + \tilde{I}_3 = 11 \angle 0^\circ + 24 \angle -31.8^\circ = 33.87 \angle -22^\circ \text{ A}$$

$$\tilde{I}_N = \tilde{I}_1 - \tilde{I}_2 = 5 \angle -36.87^\circ - 11 \angle 0^\circ = 7.6 \angle 23.9^\circ \text{ A}$$

Note that the current in the neutral line is not zero.

This is not a three-phase system; we never said that currents in 'neutral' lines will always be zero. Only in balanced three-phase systems. In unbalanced three-phase systems it is also not zero.