

1. Given info : $N_0 = 10,000$, $N = 500,000$, time = 3 hours. Asked for n.

$$N = N_0(2^n); 500,000 = 10,000(2^n); 500,000/10,000 = 2^n; 50 = 2^n; \log 50 = \log 2^n, \log 50 = n \log 2; \log 50 / \log 2 = n$$

n = 5.6 doublings

2. Given $N_0 = 10,000$, $n = 5.6$ (from previous). Asked for N at 24h.

$$N = N_0(2^n); N = 10,000(2^n), \text{ need to find n for 24 h} = (24/3) * 5.6 = 44.8$$

$$N = 10,000(2^{44.8}) = \mathbf{3.1 \times 10^{17} \text{ cells}}$$

3. Given info : n for 3 hours = 5.6 (from previous). Asked for g

$$g = t/n = 180 \text{ minutes} / 5.6 = \mathbf{32.1 \text{ minutes}}$$

4. Given $N_0 = 10,000$, $t = 6\text{h}$; Need N for 6h

$$N = N_0(2^n); N = 10,000(2^n), \text{ need to find n for 6 h}$$

$$n \text{ for 6 h} = t/g = 360 \text{ min.} / 32.1 \text{ min.} = 11.2$$

$$N = 10,000(2^{11.2}) = 2.4 \times 10^7 \text{ cells/mL}$$

$$\text{Diluted by } 10^5, \text{ therefore } (2.4 \times 10^7 \text{ cells/mL}) / 10^5 = 2.4 \times 10^2 \text{ cells/mL}$$

$$\text{Plate 0.1 mL; therefore } 2.4 \times 10^2 \text{ cells/mL} \times 0.1 \text{ mL} = \mathbf{24 \text{ Cells or CFU}}$$

5. Given $N_0 = 10,000$, $t = 2\text{h}$; Need N for 2h

$$N = N_0(2^n); N = 10,000(2^n), \text{ need to find n for 2 h}$$

$$n \text{ for 2 h} = t/g = 120 \text{ min.} / 32.1 \text{ min.} = 3.7$$

$$N = 10,000(2^{3.7}) = 1.3 \times 10^5 \text{ cells/mL}$$

$$\text{Need to find volume of one square; vol. of counting chamber} = 0.2 * 0.2 * 0.01 \text{ cm} = 0.0004 \text{ cc} = 0.0004 \text{ mL}; \text{ therefore vol. of one square} = 0.0004 / 40 = 0.00001 \text{ mL}$$

$$\text{Number of cells/sq} = 0.00001 \text{ mL} * 1.3 \times 10^5 \text{ cells/mL} = \mathbf{1.3 \text{ cells}}$$

6. Given $g = 3\text{h}$, $N = 81,920$, $t = 42\text{h}$; Asked for N_0

$N = N_0(2^n)$; $81,920 = N_0(2^n)$; need to find n for 42h.

$$n = t/g = 42/3 = 14$$

$$81,920 = N_0(2^{14}); N_0 = (81,920/2^{14}) = \underline{\underline{5 \text{ cells}}}$$

7. Given $g = 1.5\text{h}$, $N_0 = 6$, $N = 12,288$; Asked for t

$N = N_0(2^n)$; $12,288 = 6(2^n)$; $(12,288/6) = 2^n$; $2048 = 2^n$; $\log 2048 = \log 2^n$; $\log 2048 = n \log 2$;

$$n = \log 2048 / \log 2; n = 11$$

$$t = ng = 11 \times 1.5 = \underline{\underline{16.5\text{h}}}$$

8. Given $\mu = 0.00019\text{cells/min}$, $N_0 = 500$, $N = 56570$; Asked for t

$56570 = N_0(2^n)$; $56570 = 500(2^n)$; $(56570/500) = 2^n$; $113 = 2^n$; $\log 113 = n \log 2$; $\log 113 / \log 2 = n$; $n = 6.82$

$$g = \ln 2 / \mu; g = 0.693 / 0.00019 = 3648\text{min} = 2.5 \text{ days}$$

$$t = ng = 2.5 \text{ jours} \times 6.82 = \underline{\underline{17.3\text{d}}}$$

9. Given $g = (g @ 4)/10$, $N_0 = 500$, $N = 56570$; Asked for t

$$g @ \text{RT} = 2.5\text{j}/10 = 0.25\text{d}$$

$$t = ng = 6.82 (\text{according to previous}) \times 0.25\text{d} = \underline{\underline{1.7\text{d}}}$$

10. Given $N_0 = 5$; g (Glucose) = 15 minutes, g (Lactose) = 20 min; t (glucose = 60 min., t (lactose = 120 min.) ; Asked for N 3hours or 180 min.

$$n \text{ for one hour (glucose)} = t/g = 60/15 = 4$$

$$N \text{ for one hour (glucose)} = N_0(2^n) = 5(2^4) = 80$$

$$n \text{ for two hours (lactose)} = t/g = 120/20 = 6$$

$$N \text{ for two hours (lactose) starting from } N \text{ of glucose} = N_0(2^n) = 80(2^6) = \underline{\underline{5120 \text{ bacteria}}}$$

11. 9×10^7

12. (cell number : t); (5×10^6 : t40) & (1×10^7 : t60); therefore **g= 20min.**

13. Time span represented by the line = 160 min.; $n=t/g = 160/20 =$ **8 doublings**

14. 300 minutes represents end of exponential phase. Therefore number of cells at this time point will be the same at 375 minutes.

Want N for 300 min. $N=N_0(2^n)$, Need to choose N_0 : (arbitrarily chose 5×10^6 : t40)

Need time span (t): $300-40= 260\text{min.}$

Need n for 260min. $n=t/g=260/20=13$

Therefore N for 300 min. = $(5 \times 10^6)(2^{13})=$ **4.1×10^{10}**

15. Given $N_0= \text{O.D. of } 0.25$, $N = \text{O.D. of } 1.0$

Need to find n; $N=N_0(2^n)$; $1.0=0.25(2^n)$; $n=2$

Need to find time span: $t=n*g=2*20=40\text{min.}$

Therefore an O.D. of 1.0 will be reached 40min. after start point of 42 min.; **82 minutes**

16. Given $N_0= \text{O.D. of } 0.25$, Asked for N @ 124 min.

Need n for time span; Time span = $124-42=82\text{min.}$; $n=t/g = 82/20 = 4.1$

$N=N_0(2^n)$, $N=0.25(2^{4.1}) =$ **O.D of 4.3**

17. Need N for 100 min.; Need to choose N_0 : (arbitrarily chose 5×10^6 : t40)

Need time span (t): $100-40= 60\text{min.}$

Need n for 60min. $n=t/g=60/20=3$

Therefore N for 100 min. = $(5 \times 10^6)(2^3)= 4 \times 10^7$

Neisseria being diplococcus, one CFU = 2 cells; therefore $(4 \times 10^7)/2=$ **2×10^7**

18. Need N_0 for 0 min.; Need to choose N: (arbitrarily chose 5×10^6 : t40)

Need time span (t): $40 - 0 = 40$ min.

Need n for 40min. $n = t/g = 40/20 = 2$

Therefore $N = N_0(2^n)$, $5 \times 10^6 = N_0(2^2)$; $(5 \times 10^6)/4 = N_0 = \underline{1.25 \times 10^6}$

19. Need N for 92 min.; Need to choose N_0 : (arbitrarily chose 5×10^6 : t40)

Need time span (t): $92 - 40 = 52$ min.

Need n for 52min. $n = t/g = 52/20 = 2.6$

Therefore N for 92 min. = $(5 \times 10^6)(2^{2.6}) = 3 \times 10^7$

μ in initial medium = $\ln 2/g = \ln 2/20 = 0.035$

μ in new medium is 2x lower, $= 0.035/2 = 0.017$; $g = \ln 2/\mu = \ln 2/0.017 = 40.8$ min.

N after 60 minutes in new medium:

$N_0 = 3 \times 10^7$ (@92 min.)

t = 60 min.

$n = t/g = 60/40.8 = 1.5$

$N = N_0(2^n)$, $N = 3 \times 10^7(2^{1.5}) = \underline{8.5 \times 10^7}$

20. Need N @40min and N @120, want $N@120/N@40$

$N@40\text{min} = 5 \times 10^6$; $N@120 = 8 \times 10^7$; $8 \times 10^7/5 \times 10^6 = \underline{16X}$