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STUDENT NAME: _____ NUMBER: _____

PA NUMBER L12

ELEC 3605, ELECTRICAL ENGINEERING

TEST #2, NOVEMBER 2014

TIME: ONE HOUR

TEST #2 CONTAINS THREE QUESTIONS

AUTHORIZED MEMORANDA: (1) Foundations of Electric Circuits, Cogdell

(2) ELEC 3605 Course Pack Fall, 2014

(3) Calculator

1. <6 Marks>

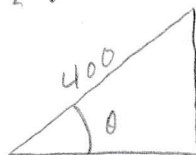
Given that the loads are **single-phase**, complete the following table.

Load	Real Power P in watts	Reactive Power Q in vars	Apparent Power in VA	Voltage In Volts	Current In Amps	Power Factor
#1	200	100	223.6	150	1.49	0.894 lag
#2	320	-240.2	400	40	10	0.80 lead

6/6

Load #1 : $S = \sqrt{P^2 + Q^2} = \sqrt{200^2 + 100^2} = 223.6 \text{ VA}$
 $PF = \frac{P}{S} = \frac{200}{223.6} = 0.894 \quad \theta = \cos^{-1} 0.894 = 26.62^\circ$
 $S = VI \quad I = \frac{S}{V} = \frac{223.6}{150} = 1.49 \text{ A}$

Load #2 :



$\theta = \cos^{-1} 0.8$
 $= 36.9^\circ$

$P = S \cos \theta = 400 (0.8) = 320 \text{ W}$
 $Q = S \sin \theta = 400 \sin 36.9 = 240.2 \text{ VAR S}$
 $S = VI \Rightarrow V = \frac{S}{I} = \frac{400}{10} = 40 \text{ V}$

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2. <6 Marks>

Given that the loads are balanced three-phase, complete the following table.

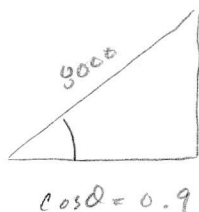
Load	Real Power P in watts	Reactive Power Q in vars	Apparent Power in VA	Line-to-Line Voltage In Volts	Line Current In Amps	Power Factor
#1	8000	2000	8246.2	476.1	10	0.97 lag
#2	7200	-3481.8	8000	423.8	5	0.90 lead

$$\text{Load \#1: } S = \sqrt{P^2 + Q^2} = \sqrt{8000^2 + 2000^2} = 8246.2 \text{ VA}$$

$$S = \sqrt{3} V_{LL} I_L \rightarrow 8246.2 = \sqrt{3} V_{LL} (10) \quad V_{LL} = \frac{8246.2}{\sqrt{3} (10)} = 476.1 \text{ V}$$

$$\text{PF} = \frac{P}{S} = \frac{8000}{8246.2} = 0.97$$

Load #2:



$$P = S \cos \theta = 8000 (0.9) = 7200 \text{ W}$$

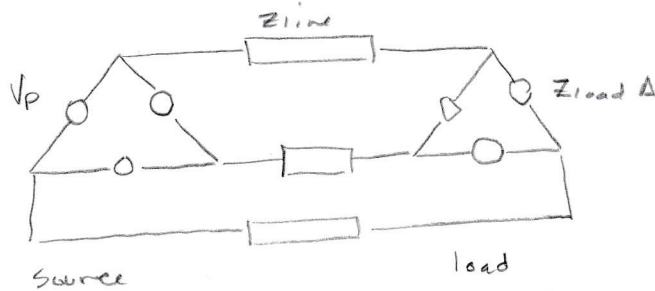
$$Q = S \sin \theta = 8000 \sin(\cos^{-1} 0.9) = 3481.8 \text{ VARs}$$

$$S = \sqrt{3} V_{LL} I_L \rightarrow 8000 = \sqrt{3} V_{LL} (5) \quad V_{LL} = \frac{8000}{5 \times \sqrt{3}} = 923.8 \text{ V}$$

3. <8 Marks>

A three-phase source is connected to a balanced delta load through a three-phase feeder with an impedance of $(0.388 + j1.499) \Omega$ per phase. Each side of the delta has an impedance of $(18.187 + j10.5) \Omega$, and the line-to-line voltage at the load is 8000 volts. Calculate:

- The line current
- The magnitude of the phase current
- The power factor of the load
- The real power, the reactive power, and the apparent power of the load
- The line-to-neutral and the line-to-line voltage at the source.



$$Z_{line} = 0.388 + j1.499 \Omega$$

$$Z_{load \Delta} = 18.187 + j10.5 \Omega$$

$$V_{LL} = 8000 \text{ V}$$

a)

$$Z_{load Y} = \frac{Z_{load \Delta}}{3} = \frac{18.187 + j10.5}{3} = 7 \angle 29.9^\circ \Omega$$

$$V_p = \frac{V_{LL}}{\sqrt{3}} = \frac{8000}{\sqrt{3}} = 4618.8 \text{ V}$$

$$I_{line} = \frac{V_p}{Z_T} = \frac{4618.8}{7 \angle 29.9} = 659.8 \angle -29.9 \text{ A}$$

b)

$$I_p = \frac{I_{line}}{\sqrt{3}} = \frac{659.8 \angle -29.9}{\sqrt{3}} = 380.9 \angle -29.9 \text{ A}$$

c)

$$PF = \cos \theta = \cos 29.9 = 0.866 \text{ lag (} -\cos \theta \text{)}$$

d)

$$S = \sqrt{3} V_{LL} I_{line}$$

$$= \sqrt{3} (8000) (659.8 \angle -29.9)$$

$$= 9131.4 \angle -29.9 \text{ kVA}$$

$$P = S \cos \theta$$

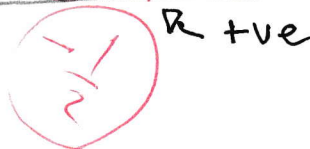
$$= 9131.4 \angle -29.9 (0.866)$$

$$= 7907.8 \angle -29.9 \text{ kW}$$

$$Q = S \sin \theta \quad \theta = \cos^{-1} 0.866 \approx 30^\circ$$

$$= 9131.4 \angle -29.9 \sin 30$$

$$= 4565.7 \angle -29.9 \text{ kVARs}$$



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e) →
in next page

$$V_{LL} = \sqrt{3} V_{LN} = \sqrt{3} (5383.47 \text{ V}) = 9324.47 \text{ V}$$

$$V_{LN} = (0.59 \cdot 87.29 \text{ VA}) (0.308 + j1.499 \Omega) + 4618.8 \text{ V} = 5383.47 \text{ V}$$