

## Formula Sheet:

**Forces**

**Units:**  $F$ : [N] or  $[\text{kg} \frac{\text{m}}{\text{s}^2}]$   $a$ :  $[\frac{\text{m}}{\text{s}^2}]$   $m$ : [kg]

**First Law:**  $F_{\text{net}} = 0$

**Second Law:**  $F_1 = m_1 a_1$   $F_{\text{net}} = F_1 + F_2 + F_n$

**Third Law:**  $F_{A \text{ on } B} = -F_{B \text{ on } A}$

**Ramps:**  $F_c = mg \sin \theta$   $F_{\text{perpendicular}} = mg \cos \theta$

**Unit 2: Work and Heat**

**Units:**  $W, E, Q$  : [J], or [Nm]  $\Delta T$  : [K]  $y$ : [m]  $v$ : [m/s]

$\Delta r$  : [m]  $c$ : [J/(kg · K)]  $P$ : [J/s or Watt]  $\Delta t$  :s

**Isolated:**  $\Delta U = U_{\text{final}} - U_{\text{initial}} = 0$

**Closed:**  $\Delta U = Q + W$

**Work on a mass:**  $W = F \Delta r \cos \theta$  \*Both F, r are magnitudes. Use angle b/w Force and r

**Work:**  $W = \Delta E_{\text{mechanical}}$

**Energy:**  $E_k = \frac{1}{2} m v^2$   $E_{\text{th}} = mc \Delta T$   $E_{\text{pot}} = mgy$

**Work-Energy:**  $W = E_{k_f} - E_{k_i}$  \*This means the system must receive or release work equal to  $\Delta E_k$  to change speed

**Conservation of Energy:**  $\Delta E_{\text{total}} = 0$

**Gasses**

**Units:**  $p$  [pa]  $V$  [  $\text{m}^3$  ]  $p$ (density) :  $\text{kg}/\text{m}^3$   $W, E, \Delta U$  : [J]

$$T: [K] \quad M: (\text{kg/mol}) \quad A \left[ \frac{m^2}{s} \right] \quad C: [\text{J}/(\text{mol} \cdot K)]$$

**Constants:**  $r = 8.314 \text{ J/mol}$        $T[K] = T(\text{Celsius}) + 273.15$

**Ideal Gas Law:**       $pV = nRT$        $\frac{p_i V_i}{T_i} = \frac{p_f V_f}{T_f}$        $M = \frac{\rho}{p} RT$

**Kinetic Gas Theory;**       $pV = \frac{1}{3} Nm \langle v^2 \rangle$

**Internal Energy:**       $U = E_k = \frac{1}{2} m v^2 = \frac{3}{2} pV = \frac{3}{2} nRT = \frac{3}{2} Nk \Delta T$

\* $k = 1.38E-23$ ,  $U=0$ , when  $T=0$

**RMS:**       $\sqrt{\langle v \rangle^2} = v_{\text{rms}} = \sqrt{\frac{3RT}{M}} = \sqrt{\frac{3kT}{m}} \quad M = \frac{3RT}{v_{\text{rms}}^2}$

\* $v_{\text{rms}}$  is proportional to  $T$

### Thermodynamics:

**Work:**       $W = -p \Delta V$

\*note:  $p$  is constant

**Heat:**       $Q = nC \Delta T$

**First Law:**       $\Delta U = Q + W$

**Isochoric:**       $V = \text{const} \quad \frac{p_i}{T_i} = \frac{p_f}{T_f} \quad W = 0 \rightarrow \quad U = Q = nC \Delta T = \frac{3}{2} nR \Delta T$

**Isothermal:**       $T = \text{const} \quad p_i V_i = p_f V_f \quad \Delta U = 0 \quad W = nRT \ln(V_i/V_f) = nRT \ln(p_f/p_i) \quad Q = -W$

**Isobaric:**       $P = \text{const} \quad V_i/T_i = V_f/T_f$

$W = -p \Delta V = -nR \Delta T$

$Q = \Delta U - W = \frac{5}{2} nR \Delta T \quad Q = nC \Delta T$

**Adiabatic:**  $Q = 0$        $\Delta U = W = \frac{3}{2} nR \Delta T$

\*Note: There is heat transfer, but temperature still changes

$$p_i V_i^{5/3} = p_f V_f^{5/3} \qquad V_i T_i^{3/2} = V_f T_f^{3/2} \qquad p_i^{-2/3} T_i^{5/3} = p_f^{-2/3} T_f^{5/3}$$

### Transfer of Energy and Matter:

L: [m]       $\Lambda$ : [m]  $\lambda$ : [J/(smk)]      D: [ m<sup>3</sup> /s]    c [mol/ m<sup>3</sup>]

**Fourier's Law:**       $\frac{Q}{t} = \lambda A \left( \frac{T_{high} - T_{low}}{L} \right)$

$\lambda$  = Heat conductivity,  $Q/t$  = rate of heat transfer, A = cross sectional area

**Fick's:**       $\frac{m}{t} = DA \left( \frac{\Delta \rho}{L} \right)$        $\frac{n}{t} = \frac{C_{high} - C_{low}}{L}$

**Arrhenius:**       $D = D_0 e^{-\frac{\Delta E}{kT}}$        $\ln D = \ln D_0 - \left( \frac{\Delta E}{kT} \right)$

**Einstein:**       $\Lambda = \sqrt{2Dt}$

### Mirrors, Lenses

p, f, q, L, R: [m]       $S_o = 25 \text{cm} = 0.25 \text{m}$

**Focal length :**       $f = R/2$

**Magnification:**       $M = (-q/p)$

**Snell's:**       $n_1 \sin \alpha = n_2 \sin \beta$        $v = c/n$       n cannot be less than 1

**Angular Magnification:**       $\theta/\theta_o$        $m = s_o/p$

**Max. Angular Magnification:**  $m = 1 + s_o/p$

**Microscopic Magnification:**  $= m_o \times m_e = \frac{-L \cdot s_o}{f_o \cdot f_e}$

**Depth:**       $q = -(n_2/n_1)p$

**Spherical Interfaces:**       $\frac{n_1}{p} + \frac{n_2}{q} = \frac{n_2 - n_1}{R}$