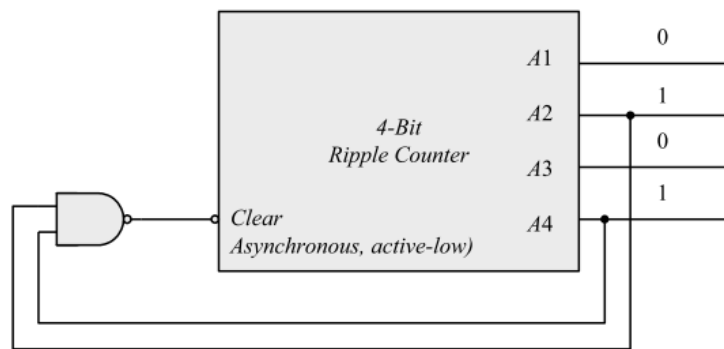


**ITI1100C & ITI1500**  
**Assignment/Devoir #6**  
**Solutions**

- 6.11** (a) A count down counter. / Compteur décroissant  
 (b) A count up counter. / Compteur croissant

**6.13**



- 6.19** (b) From the state table in Table 6.5: /a partir de la table 6.5

$$D_{Q1} = Q'_1$$

$$D_{Q2} = \sum (1, 2, 5, 6)$$

$$D_{Q4} = \sum (3, 4, 5, 6)$$

$$D_{Q8} = \sum (7, 8)$$

$$\text{Don't care: } d = \sum (10, 11, 12, 13, 14, 15)$$

Simplifying with maps:

$$D_{Q2} = Q_2Q'_1 + Q'_8Q'_2Q_1$$

$$D_{Q4} = Q_4Q'_1 + Q_4Q'_2 + Q'_4Q_2Q_1$$

$$D_{Q8} = Q_8Q'_1 + Q_4Q_2Q_1$$

(a)

| Present state | Next state | Flip-flop inputs  |                   |                   |                   |
|---------------|------------|-------------------|-------------------|-------------------|-------------------|
|               |            | $J_{A_8} K_{A_8}$ | $J_{A_4} K_{A_4}$ | $J_{A_2} K_{A_2}$ | $J_{A_1} K_{A_1}$ |
| 0000          | 0001       | 0 x               | 0 x               | 0 x               | 1 x               |
| 0001          | 0010       | 0 x               | 0 x               | 1 x               | x 1               |
| 0010          | 0011       | 0 x               | 0 x               | x 0               | 1 x               |
| 0011          | 0100       | 0 x               | 1 x               | x 1               | x 1               |
| 0100          | 0101       | 0 x               | x 0               | 0 x               | 1 x               |
| 0101          | 0110       | 0 x               | x 0               | 1 x               | x 1               |
| 0110          | 0111       | 0 x               | x 0               | x 0               | 1 x               |
| 0111          | 1000       | 1 x               | x 1               | x 1               | x 1               |
| 1000          | 1001       | x 0               | 0 x               | 0 x               | 1 x               |
| 1001          | 0000       | x 1               | 0 x               | 0 x               | x 1               |

$$\begin{aligned} J_{A_1} &= 1 \\ K_{A_1} &= 1 \\ J_{A_2} &= A_1 A_8' \\ K_{A_2} &= A_1 \\ J_{A_4} &= A_1 A_2 \\ K_{A_4} &= A_1 A_2' \\ J_{A_8} &= A_1 A_2' A_4 \\ K_{A_8} &= A_1 \end{aligned}$$

$$d(A_8, A_4, A_2, A_1) = \Sigma (10, 11, 12, 13, 14, 15)$$

| Present state<br><i>ABC</i> | Next state<br><i>ABC</i> | Flip-flop inputs |       |       |       |       |       |
|-----------------------------|--------------------------|------------------|-------|-------|-------|-------|-------|
|                             |                          | $J_A$            | $K_A$ | $J_B$ | $K_B$ | $J_C$ | $K_C$ |
| 000                         | 001                      | 0                | x     | 0     | x     | 1     | x     |
| 001                         | 010                      | 0                | x     | 1     | x     | x     | 1     |
| 010                         | 011                      | 0                | x     | x     | 0     | 1     | x     |
| 011                         | 100                      | 1                | x     | x     | 1     | x     | 1     |
| 100                         | 100                      | x                | 0     | 0     | 0     | 1     | x     |
| 101                         | 110                      | x                | 0     | 1     | x     | x     | 1     |
| 110                         | 000                      | x                | 1     | x     | 1     | 0     | x     |
| 111                         | xxx                      | x                | x     | x     | x     | x     | x     |

