

Seepage and Effective Stress

Q1

From the question: $\Delta h = 30\text{cm}$

$$l_A = l_B = l_C = 15\text{cm}$$

Calculation of the rate of water supply q in cm^3/h .

$$q = Aki$$

The flow is normal to the layers, Hence:

$$k = \frac{l_A + l_B + l_C}{\frac{l_A}{k_A} + \frac{l_B}{k_B} + \frac{l_C}{k_C}} = \frac{15 + 15 + 15}{\frac{15}{2 \times 10^{-2}} + \frac{15}{2 \times 10^{-3}} + \frac{15}{8 \times 10^{-5}}} = 2.31 \times 10^{-4} (\text{cm/s})$$

and

$$i = \frac{\Delta h}{l_A + l_B + l_C} = \frac{30}{15 + 15 + 15} = 0.667$$

$$A = 10 \times 10 = 100 (\text{cm}^2)$$

$$q = Aki = 100 \times 2.31 \times 10^{-4} \times 0.667 \times 3600 = 55.47 (\text{cm/h})$$

Q2.

Figure 2 shows the flow net diagram, from which $N_f = 3.5$ and $N_d = 9$. The overall loss in total head is 3.00m. Then

$$q = kh \frac{N_f}{N_d} = 5 \times 10^{-5} \times .00 \times \frac{3.5}{9} = 5.8 \times 10^{-5} \text{ (m}^3/\text{s / m)}$$

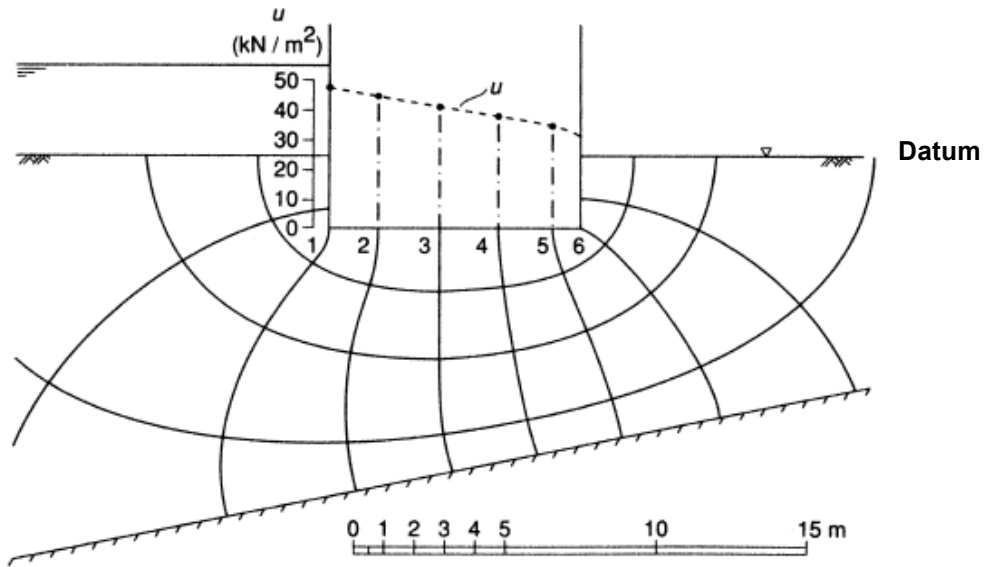
The pore water pressure is determined at the points of intersections of the equipotential with the base of the structure. The total head (h) at each point is obtained from the flow net. The elevation head (z) at each point on the base of the structure is -2.50m. The calculations are below and the distribution of pressure is plotted to scale in the figure.

Point	h (m)	$h-z$ (m)	$u = \gamma_w (h - z)$ (kN/m²)
1	2.33	4.83	47
2	2.00	4.50	44
3	1.67	4.17	41
4	1.33	3.83	37
5	1.00	3.50	34
6	0.67	3.17	31

e.g. for point 1:

$$h_1 = \frac{n_1}{n_d} \times h = \frac{7}{9} \times 3 = 2.33 \text{ (m)}$$

$$h_p = h_1 - z_1 = 2.33 - (-2.5) = 4.83 \text{ (m)}$$



The uplift force on the base of the structure is equal to the area of the pressure diagram and is 316 kN per unit length.

Q3.

Given:

$$\rho_{sat(clay)} = 1925 \text{ kg/m}^3$$

$$\gamma_{sat(clay)} = \frac{1925 \times 9.81}{1000} = 18.88 \text{ kN/m}^3$$

At point A

$$\sigma_A = (10 - 7.2) \gamma_{sat(clay)} + h\gamma_w = 2.8 \times 18.88 + h\gamma_w = 52.86 + h\gamma_w \text{ (kPa)}$$

$$u_A = 6\gamma_w = 6 \times 9.81 = 58.86 \text{ (kPa)}$$

For heave (For clay stability)

$$\sigma_A - u_A = 0$$

$$\sigma_A = u_A$$

$$52.86 + h\gamma_w = 58.86$$

$$h = \frac{58.86 - 52.86}{9.81} = 0.61 \text{ m}$$

Q4.

Step 1: Calculate the unit weights;

0 - 2 m

$$S = 40\% = 0.4 ; w = 0.05$$

$$e = wG_s/S = \frac{0.05 \times 2.7}{0.4} = 0.34$$

$$\gamma = G_s \frac{(1+w)}{(1+e)} \gamma_w = \frac{2.7 (1+0.05)}{1+0.34} \times 9.8 = 20.7 \text{ kN/m}^3$$

2– 5.4 m

$$S = 1; w = 0.12$$

$$e = wG_s = 0.12 \times 2.7 = 0.32$$

$$\gamma = \left(\frac{G_s + e}{1 + e} \right) \gamma_w = \left(\frac{2.7 \times 0.32}{1 + 0.32} \right) \times 9.8 = 22.4 \text{ kN/m}^3$$

5.4 – 20.6 m

$$S = 1; w = 0.28$$

$$e = wG_s = 0.28 \times 2.7 = 0.76$$

$$\gamma = \left(\frac{G_s + e}{1 + e} \right) \gamma_w = \left(\frac{2.7 \times 0.76}{1 + 0.76} \right) \times 9.8 = 19.3 \text{ kN/m}^3$$

Step 2: calculate the stress table or spreadsheet

Depth (m)	Thickness (m)	σ (kPa)	u (kPa)	$\sigma' = \sigma - u$ (kPa)
3	3	$20.7 \times 2 + 22.4 \times 1 = 63.8$	0	63.8
5.4	2.4	$63.8 + 22.4 \times 2 = 117.6$	$2.4 \times 9.8 = 23.5$	94.1
20.6	15.2	$117.6 + 19.3 \times 15.2 = 411$	$23.5 + 15.2 \times 9.81 = 172.5$ or $17.6 \times 9.8 = 172.5$	238.5

