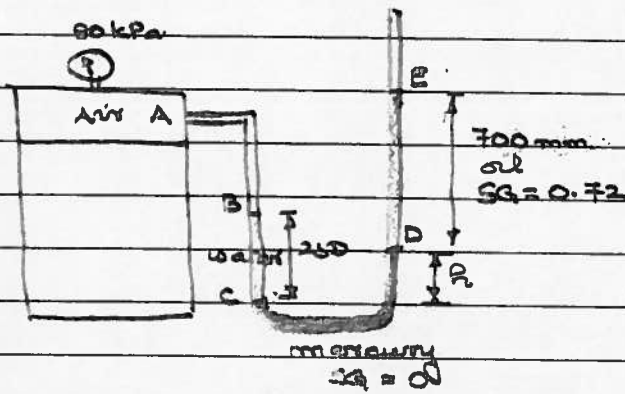


ENGR 251/4 XX : Thermodynamics

Quiz #1 Solutions:

1.



$$P_E = P_{atm}$$

$$P_D = P_E + 700 \text{ mm oil}$$

$$P_C = P_D + R \text{ mm mercury}$$

$$P_B = P_C - 250 \text{ mm water}$$

$$P_A = P_B$$

$$\therefore P_A = P_{atm} + 700 \text{ mm of oil} + R \text{ mm of mercury} - 250 \text{ mm of water}$$

$$\therefore P_A (\text{Gage}) = 700 \text{ mm of oil} + R \text{ mm of mercury} - 250 \text{ mm of water}$$

$$\therefore 30 \text{ kPa} = \frac{0.700 \times 0.72 \times 1000 \times 9.81}{1000} \text{ kPa}$$

$$+ \frac{R \times 10^{-3} \times 13.6 \times 1000 \times 9.81}{1000} \text{ kPa}$$

$$- \frac{0.250 \times 1000 \times 9.81}{1000} \text{ kPa}$$

$$30 = 4.944 + R \times 10^{-3} \times 133.4 - 2.453$$

$$\therefore R = 581.0 \text{ mm}$$

② (a) 2 kg H₂O at 100°C and 5 MPa

T = 100°C (P_{sat} = 101.42 kPa) (A4)

P = 5 MPa.

P > P_{sat} ∴ Compressed liquid

At P = 5 MPa

T = 100°C

v = 0.0010410 m³/kg

V = mv

= 2 × 0.0010410 = 0.0020820 m³

(b) 2 kg of saturated mixture, V = 1.0 m³, T = 110°C

(a) P = P_{sat @ T}
= 143.38 kPa. (A4)

(b) v = $\frac{1.0}{2} = 0.50 \text{ m}^3/\text{kg}$.

v_f = 0.001052 m³/kg

v_g = 1.2094 m³/kg

v = v_f(1-x) + v_gx.

∴ x = $\frac{v - v_f}{v_g - v_f} = \frac{0.50 - 0.001052}{1.2094 - 0.001052} = 0.4129$

(c) Saturated mixture, x = 0.60, V = 1.0 m³, T = 110°C

At v_f = 0.001052 v_g = 1.2094 u_f = 461.27 u_{fg} = 2056.4

v = (1-x)v_f + xv_g
= 0.40 × 0.001052 + 0.6 × 1.2094 = 0.72606 m³/kg.

m = $\frac{V}{v} = \frac{1.0}{0.72606} = 1.377 \text{ kg}$.

u = u_f + x u_{fg}
= 461.27 + 0.6 × 2056.4 = 1695.1 kJ/kg

∴ U = mu
= 1.377 × 1695.1 = 2334.2 kJ.

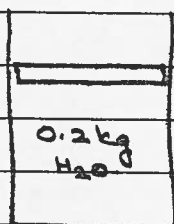
(4) $U = 1000 \text{ kJ}$, $P = 50 \text{ kPa}$, $T = 100^\circ\text{C}$.

A6: $v = 3.4187 \text{ m}^3/\text{kg}$, $u = 2511.5 \text{ kJ/kg}$.

$$m = \frac{U}{u} = \frac{1000}{2511.5} = 0.3982 \text{ kg}$$

$$V = m v = 0.3982 \times 3.4187 = 1.361 \text{ m}^3$$

3.



Initial: $x_1 = 0.80$, $P_1 = 100 \text{ kPa}$.

A5: $v_f = 0.001043$, $v_g = 1.6941$

$u_f = 417.4$, $u_g = 2088.2$.

$$\therefore v_1 = 0.2 v_f + 0.8 v_g = 1.3554 \text{ m}^3/\text{kg}$$

$$u_1 = x u_f + (1-x) u_g = 2088.0 \text{ kJ/kg}$$

Final $P = 100 \text{ kPa}$, $T = 150^\circ\text{C}$

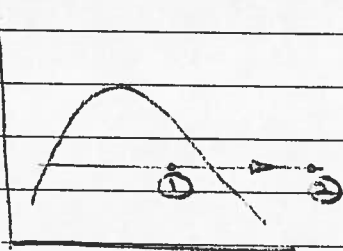
$T_{\text{sat @ } P} = 99.6^\circ\text{C}$

\therefore Super-Heated steam.

A6: $v_2 = 1.9367 \text{ m}^3/\text{kg}$

$u_2 = 2582.9 \text{ kJ/kg}$

(a)



(b) $V_2 - V_1 = m v_2 - m v_1$

$$= 0.2 (1.9367 - 1.3554) = 0.11626 \text{ m}^3$$

$U_2 - U_1 = m u_2 - m u_1$

$$= 0.2 (2582.9 - 2088.0) = 99.98 \text{ kJ}$$