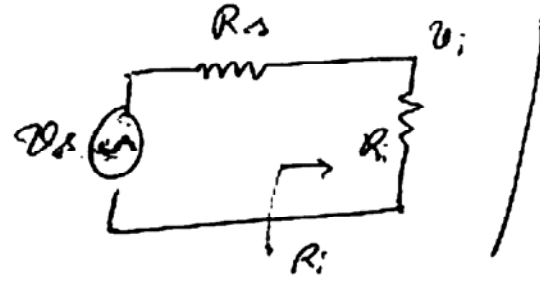


iii) Find the voltage gain $A_{v1} = v_i/v_s$, voltage gain $A_{v2} = v_o/v_i$ and the overall voltage gain $A_v = v_o/v_s$. Show the derivation of necessary expressions in your computations (9 marks):

$A_{v1} = \frac{v_i}{v_s}$



$A_{v1} = \frac{v_i}{v_s} = \frac{R_i}{R_i + R_s}$

$= \frac{20}{20 + 80} = \frac{20}{100}$

$= \underline{\underline{0.2}}$

$A_{v2} = \frac{v_o}{v_i}$

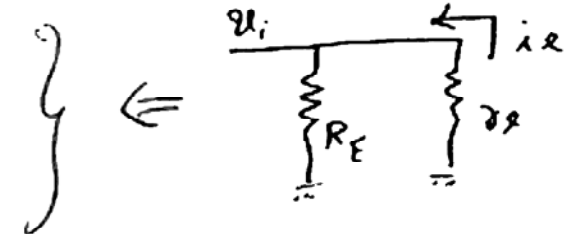
$v_o = -\alpha i_x R_L' \rightarrow (1)$

$R_L' = R_C \parallel R_L = 4k \parallel 4k = 2k$

we have

$v_i = -i_x r_x$

$\therefore i_x = -v_i / r_x$



(1) \Rightarrow

$v_o = -\alpha \left(-\frac{v_i}{r_x} \right) \cdot R_L'$

$A_{v2} = \frac{v_o}{v_i} = \frac{\alpha R_L'}{r_x}$

$= \frac{0.98 \times 2k}{25}$

$= \underline{\underline{78.4}}$

$\alpha = \frac{\beta}{\beta + 1}$

$= \frac{50}{50 + 1}$

$= 0.98$

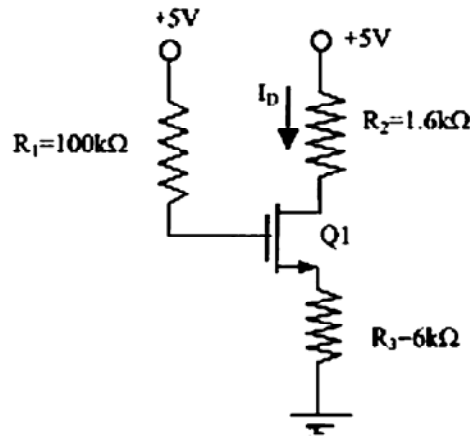
$A_{v1} = 0.2$

$A_{v2} = 78.4$

$A_v = 15.68$

$A_{v0} = A_{v1} \times A_{v2} = 0.2 \times 78.4 = \underline{\underline{15.68}}$

4) MOSFET.



IGNORE λ

a) In the figure above, the transistor has $V_t = 1V$, $V_A = 30V$, $k_n = 100 \mu A/V^2$, $L = 1 \mu m$ and $W = 10 \mu m$.

i) Find the bias current I_D (5 marks):

Assume saturation. $I_D = \frac{1}{2} k_n \frac{W}{L} (V_{GS} - V_t)^2$

$$I_D = 0.5 \times 10^{-3} [36 \times 10^6 I_D^2 - 48 \times 10^3 I_D + 16]$$

$$I_D = 18 \times 10^3 I_D^2 - 24 I_D + 8 \times 10^3$$

$$18 \times 10^3 I_D^2 - 25 I_D + 8 \times 10^3 = 0$$

$$I_D = \left. \begin{matrix} 0.89 \text{ mA} \\ 0.5 \text{ mA} \end{matrix} \right\} \text{ or } \left. \begin{matrix} I_D = 0.5 \text{ mA} \\ V_D = 5 - 1.6 \times 0.5 \\ = 2 - 0.8 = 1.2 \end{matrix} \right\} \Rightarrow \left. \begin{matrix} V_D > V_{GS} - V_t \\ 1.2 > 5 - 1 \\ 1.2 > 4 \end{matrix} \right\} \Rightarrow \text{Mode = SATURATION}$$

$$\begin{aligned} k_n &= 100 \mu A/V^2, \frac{W}{L} = 10 \\ \frac{1}{2} k_n &= 0.5 \times 10^{-3} \\ V_{GS} &= V_G - V_S \\ &= 5 - I_D R_3 \\ &= 5 - 6 \times 10^3 I_D \\ V_{GS} - V_t &= 4 - 6 \times 10^3 I_D \\ (V_{GS} - V_t)^2 &= 36 \times 10^6 I_D^2 - 48 I_D \times 10^3 + 16 \end{aligned}$$

ii) Verify the mode of operation of the transistor and state what mode the transistor is in (3 marks):

$V_{DS} \geq V_{GS} - V_t$ for saturation

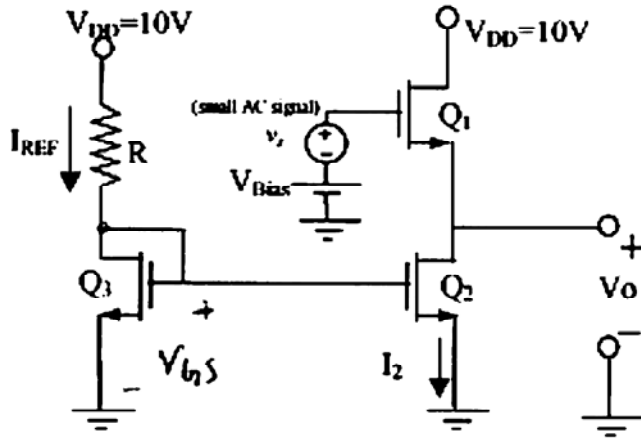
$V_D > V_G - V_t$

$1.2 > 5 - 1$

$1.2 > 4$

Mode = SATURATION

4) b) MOSFET (continued....)



For the figure on the left, the transistors have
 $V_t = 1V$, $V_A = 30V$,
 $k_n' = 100\mu A/V^2$,
 $L_1 = 1\mu m$, $W_1 = 10\mu m$,
 $L_2 = 1\mu m$,
 $L_3 = 1\mu m$, $W_3 = 10\mu m$.

Using these data compute the following:

i) If $I_{REF} = 1mA$, find R (5 marks):

$$I_{REF} = I_{D3} = \frac{1}{2} k_n' \left(\frac{W}{L}\right)_3 (V_{GS} - V_t)^2$$

$$\therefore 1mA = \frac{1}{2} \times 100 \times 10^{-6} \times 10 (V_{GS} - V_t)^2$$

$$\therefore 1mA = 0.5 \times 10^{-3} (V_{GS} - V_t)^2$$

$$\therefore (V_{GS} - V_t)^2 = 2$$

$$\therefore V_{GS} - V_t = \pm 1.4 = \underline{1.4}$$

$$V_{GS} = 1.4 + 1 = 2.4$$

$$V_{GS} = 2.4 V$$

$$\therefore R = \frac{10 - 2.4}{1mA} = \underline{7.6k}$$

$$R = \underline{7.6k}$$

ii) If $I_2 = 0.5mA$, find W_2 (3 marks):

$$\frac{I_2}{I_{REF}} = \frac{(W/L)_2}{(W/L)_3}$$

$$\left(\frac{W}{L}\right)_2 = 0.5 \times \left(\frac{W}{L}\right)_3 = 0.5 \times 10$$

$$\therefore (W)_2 = 1\mu m \times 5 = \underline{5\mu m}$$

$$W_2 = \underline{5\mu m}$$

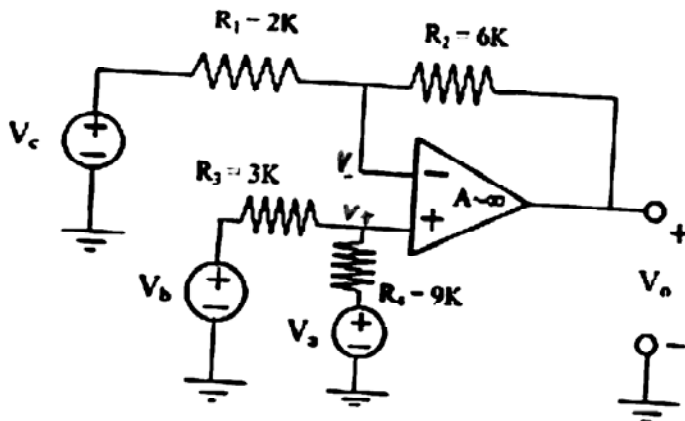
iii) What is the minimum value of V_o for which $I_2 = 0.5mA$ (3 marks):

$$V_{D2} > V_{GS} - V_t$$

$$\Rightarrow V_{D2} > \underline{1.4 V}$$

$$\text{Minimum } V_o = \underline{1.4}$$

5) Operational Amplifier



a) For the circuit shown, find the expression for \$V_o\$ as a function of \$V_a\$, \$V_b\$ and \$V_c\$ (assume the op amp is ideal) (10 Marks)

\$\Rightarrow\$ The above ckt. has both the inverting and non-inverting configuration based operations.

\$\Rightarrow\$ Analyze individually and use the superposition theorem to get the final output.

\$V_a\$ [\$V_b = 0, V_c = 0\$] : $V_+ = V_a \left[\frac{3}{3+9} \right] = \frac{V_a}{4}$

$V_{oa} = \left[1 + \frac{6}{2} \right] V_+ = 4 \frac{V_a}{4} = \underline{\underline{V_a}}$

\$V_b\$ [\$V_a = 0, V_c = 0\$] : $V_+ = V_b \left[\frac{9}{3+9} \right] = \frac{3}{4} V_b$

$V_{ob} = \left[1 + \frac{6}{2} \right] V_+ = 4 \cdot \frac{3}{4} V_b = \underline{\underline{3V_b}}$

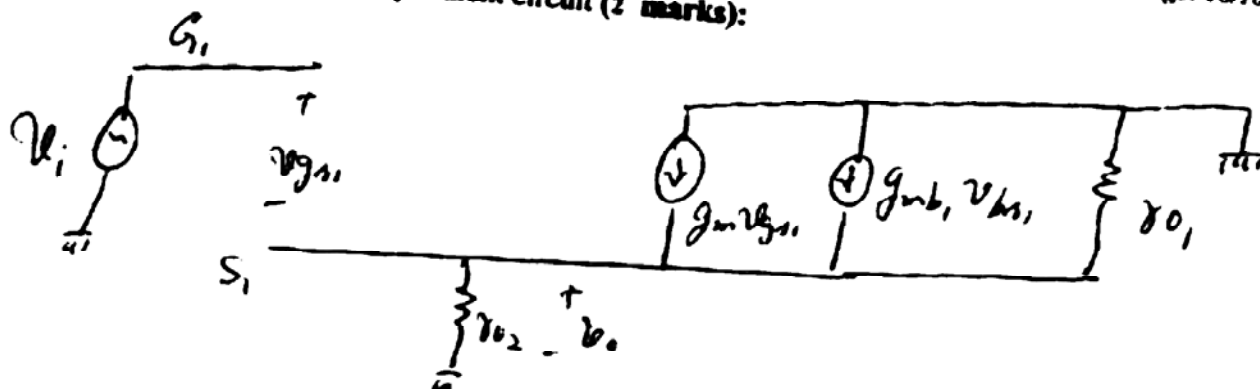
\$V_c\$ [\$V_b = 0, V_a = 0\$] :

$V_{oc} = -\frac{6}{2} V_c = -3V_c$

Total $V_o = V_a + 3V_b - 3V_c$

$v_o = V_a + 3V_b - 3V_c$

iv) Draw the small signal equivalent circuit (2 marks):

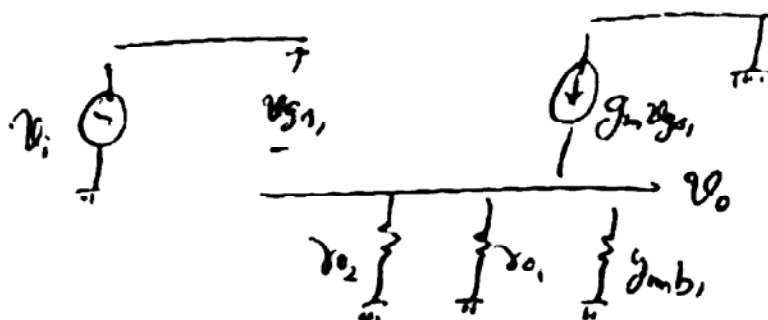


v) If $I_D = 0.5 \text{ mA}$, $\chi = 0.1$ and Q_1 is in saturation, find $A_v = v_o/v_i$ (4 marks):

$$g_m = \sqrt{2k_n' \left(\frac{W}{L}\right) I_{D_S}} = \sqrt{2 \times 100 \times 10^{-6} \left(\frac{10}{1}\right) 0.5 \times 10^{-3}} = 10^3 \sqrt{10} = 3.1623 \times 10^3$$

$$g_{mb} = \chi g_m = 0.1 \times 3.1623 \times 10^3 = 0.31623 \times 10^3$$

$$r_o = \frac{V_A}{I_D} = \frac{30}{0.5 \times 10^{-3}} = 60 \text{ k}$$



$$\begin{aligned} R_S' &= r_{o2} \parallel r_{o1} \parallel \frac{1}{g_{mb}} \\ &= 60 \text{ k} \parallel 60 \text{ k} \parallel \frac{1}{g_{mb}} \\ &= 30 \text{ k} \parallel 3.1623 \text{ k} \\ &= 2.86 \text{ k} \end{aligned}$$

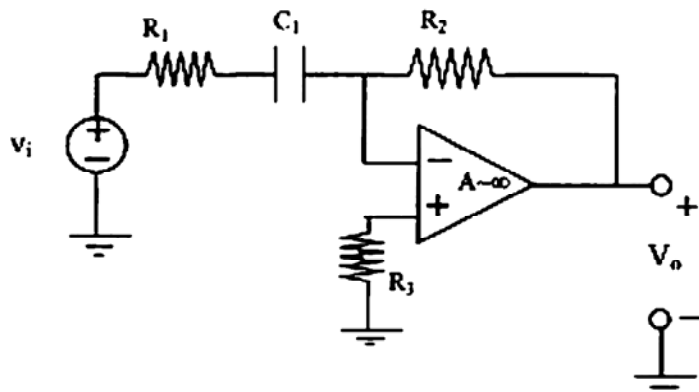
$$v_i = v_o + v_{gs1} \quad v_o = g_m v_{gs1} \cdot R_S'$$

$$v_{gs1} = \frac{v_o}{g_m R_S'}$$

$$v_i = v_o + \frac{v_o}{g_m R_S'}$$

$$\boxed{\frac{v_o}{v_i} = \frac{g_m R_S'}{1 + g_m R_S'}} = \frac{3.1623 \times 10^3 \times 2.86 \times 10^3}{1 + 3.1623 \times 10^3 \times 2.86 \times 10^3} = A_v = 0.9$$

5) b) Operational Amplifier (continued....)



i) For the above circuit, assuming ideal op-amp, derive the gain $H(j\omega) = V_o(j\omega)/V_i(j\omega)$. Show the steps. (6 Marks)

$$H(j\omega) = \frac{V_o(j\omega)}{V_i(j\omega)} = - \frac{Z_2}{Z_1} ; \quad \begin{matrix} Z_2 = R_2 \\ Z_1 = R_1 + \frac{1}{j\omega C_1} \end{matrix}$$

$$H(j\omega) = - \frac{R_2}{R_1 + \frac{1}{j\omega C_1}} = - \frac{(R_2/R_1)}{1 + \frac{j\omega C_1 R_1}{1}}$$

ii) If $R_1 = 5K\Omega$, $R_2 = 15K\Omega$, $R_3 = 10K\Omega$, $C_1 = 1\mu F$ and frequency is 1MHz, compute the gain-magnitude in DBs and gain-phase in degrees. (3 Marks)

$$H(j\omega) = - \frac{15 \times 10^3}{5 \times 10^3 + \frac{1}{j \times 6.2832 \times 10^6 \times 10^{-6}}} = - \frac{15 \times 10^3}{5 \times 10^3 - j0.1592}$$

$\omega = 2\pi f = 2 \times 3.1416 \times 10^6 = 6.2832 \times 10^6$

$$|H(j\omega)| = 3, \quad \angle \phi = 180^\circ$$

$$= 20 \log(3) = 20 \times 0.4771$$

$$|H(j\omega)| = 9.54 \text{ DBs}$$

$$\angle H(j\omega) = 180^\circ \text{ Degrees}$$

iii) What class of filter does the above circuit belong to? (1 Mark)

High-pass filter