

# DATA

Population

SAMPLE

Subset of population

Example:

All students

attending Ryerson University

$$N = 30,000$$

↓  
population size

30,000 X's  
values.

$X = \text{G.P.A. for a student}$

$$n = 30 \text{ or } 40 \text{ etc}$$

↓  
sample size

$X = \text{G.P.A. for a student}$

Quantitative

pop Mean =  $\mu$

pop Standard deviation =  $\sigma$

Unknown

Sample Mean =  $\bar{X}$

Sample Standard deviation =  $S$

Known

①  $\pi$  = population proportion of retail outlet included the GST in their prices

sample data

$X$  = # of retail outlet included the GST in their prices = 165  
 $n$  = sample size = 300  
 $p = \frac{X}{n} = \frac{165}{300}$  ✓ to define RR using C.V.  $\alpha = 0.05$

Hypothesis Statement

$H_0 : \pi \leq 0.5$

$H_a : \pi > 0.5$

3 symbols :  $\neq, >, <$  } just like calculator input (TEST)

$H_0 : \pi \leq \pi_0$   
 $H_a : \pi > \pi_0$  }  $\pi_0$  is always given when you assume  $H_0$  is true  $\pi = \pi_0$

To test the above hypothesis :

- 1) Setup the RR  $\rightarrow$  i.e. set up the decision frame
- 2) Calculate the test statistics / p-value using sample data, you use this information to make 2 decisions :

- I) Statistical decision : a) Reject  $H_0$   
 b) Do not reject  $H_0$

II) Managerial decision : There is <sup>(no)</sup> evidence

$$H_0: \pi = 0.5$$

$$H_a: \pi \neq 0.5 \quad (\text{Two tailed test})$$

→ Z test

Sample data

$$X = 369$$

convert p to Z calc

$$n = 899$$

$$p = \frac{\text{Sample}}{\text{prop}} = \frac{X}{n}$$

CALC PRO = TEST

$$Z = (1-p) \rightarrow \begin{cases} Z_{\text{calc}} = -5.3697 \\ p\text{-value} = 0.0000008 \end{cases}$$

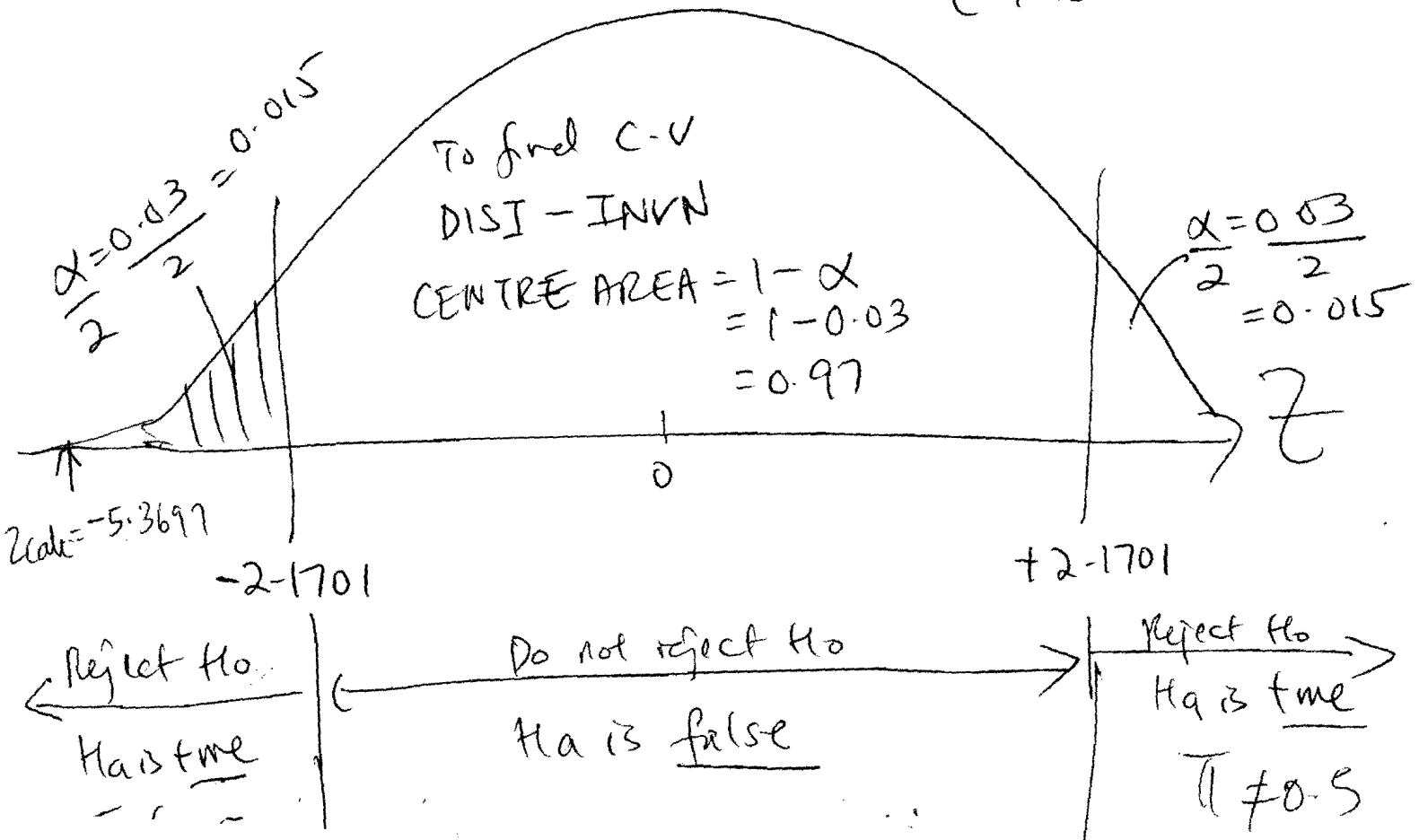
I) Set up RR

→ 1)  $\alpha = 0.03$

→ 2) Critical value Z

→ 3) where RR?

$H_a: \pi \neq 0.5$   
(two tailed)



I)  $H_0: \pi \leq 0.5$

$H_a: \pi > 0.5$

Setup the RR

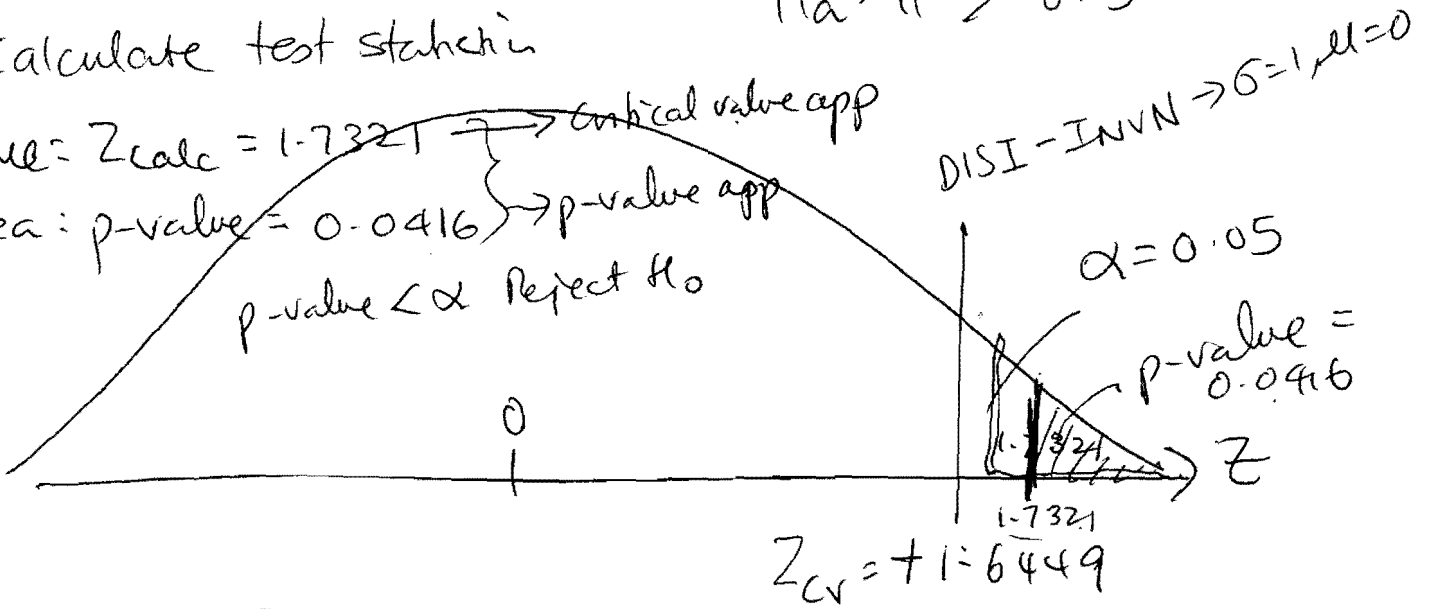
- 1)  $\alpha = 0.05$  Always
- 2) Critical value  ~~$Z_c$~~
- 3) Where is the RR area?  $H_a: \pi > 0.5$

II-) Calculate test statistic

1) Value:  $Z_{calc} = 1.7321$  → critical value app

2) Area:  $p\text{-value} = 0.0416$  → p-value app

$p\text{-value} < \alpha$  Reject  $H_0$



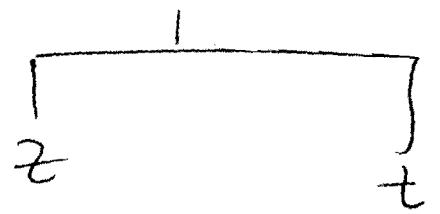
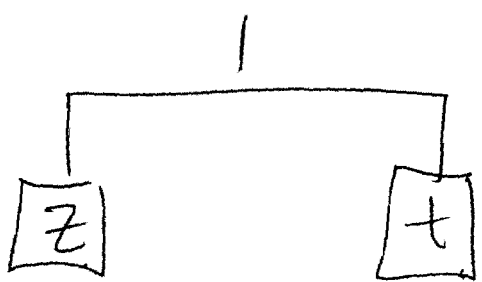
$Z_{calc} < 1.6449$ <u>Do not reject <math>H_0</math></u> $H_a$ is <u>false</u> There is <u>NO</u> evidence to support $\pi > 0.5$	$Z_{calc} > 1.6449$ <u>Reject <math>H_0</math></u> $H_a$ is true There is <u>evidence</u> $\pi > 0.5$
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To find CI

To find Critical value

INTR

DIST



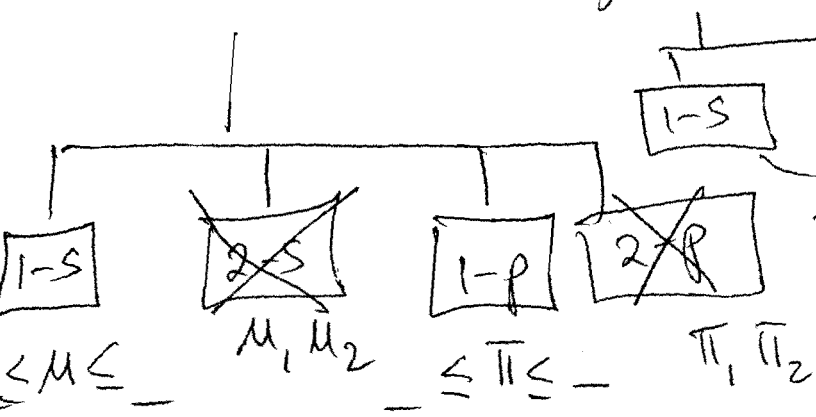
$\sigma$  is given/know

$\sigma$  is not given or know

NORM

DIST

INVM



$\mu_1, \mu_2$

$\leq \mu \leq$

$\leq \mu \leq$

$\leq \pi \leq$



↓  
t  
↓  
Inv t

Cauton

Cauton

Always Var (F2)

Always Var/F2

Tail:

Area:

Area:

$\sigma = 1$   
 $\mu = 0$

↓  
refers to

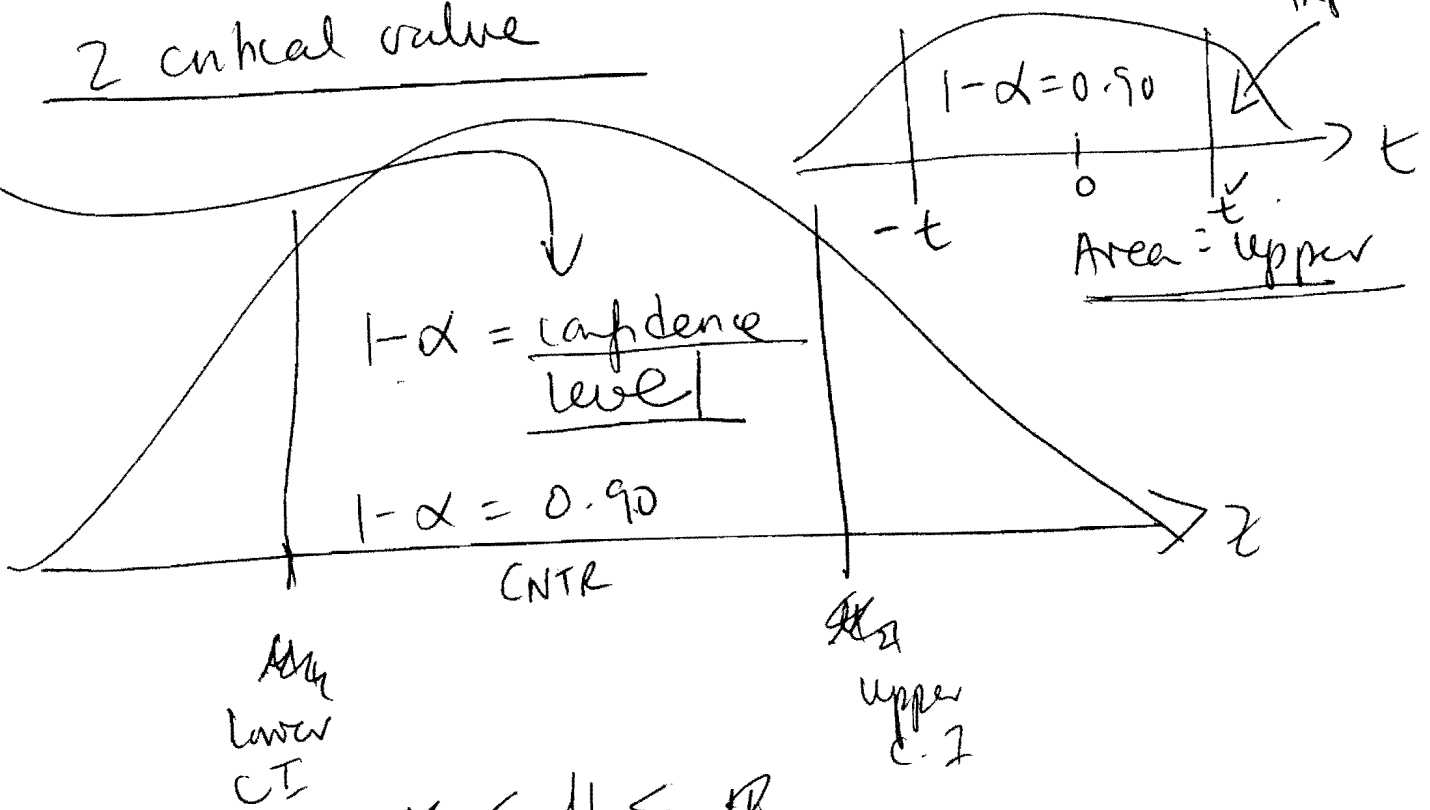
upper tail  
Area always

# To find Confidence Interval

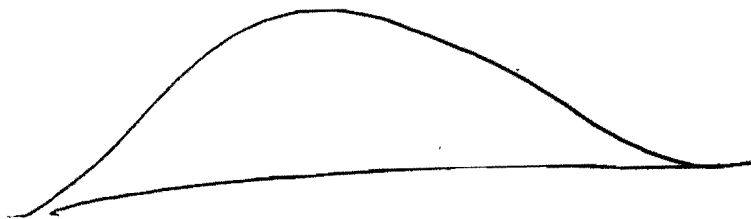
90% confidence interval for  $\mu$  or  $\bar{x}$

Find the critical value ( $Z$  or  $t$ )

$Z$  critical value



For hypothesis test  $\rightarrow$  given  $\alpha =$  significance level



# Hypothesis test

TEST

Z

t

1-S

~~2-S~~

1-P

~~2-P~~

1-S

~~2-S~~

~~REG~~

$H_0: \mu = 70$   
 $H_a: \mu \neq 70$

$H_0: \mu = 70$   
 $H_a: \mu \neq 70$

~~$H_0: \mu_1 - \mu_2 = 0$   
 $H_a: \mu_1 - \mu_2 \neq 0$~~

$H_0: \pi \geq 0.5$   
 $H_a: \pi \neq 0.5$

~~$H_0: \pi_1 - \pi_2 = 0$   
 $H_a: \pi_1 - \pi_2 \neq 0$~~

