

Math 180 Midterm Version 1. Please answer all questions on the scantron provided.

1. If you decompose 40320 into a product of primes, the sum of the exponents is
 - (a) 8
 - (b) 9
 - (c) 10
 - (d) 11
 - (e) none of the above

2. The sum of the exponents of the prime decomposition of $\text{lcm}(121, 99)$ is
 - (a) 2
 - (b) 3
 - (c) 4
 - (d) 5
 - (e) none of the above

3. 1362 modulo 11 is congruent to
 - (a) 9
 - (b) 8
 - (c) 7
 - (d) 6
 - (e) none of the above

4. Which of the following is a zero divisor of \mathbb{Z}_{15}
 - (a) 14
 - (b) 9
 - (c) 7
 - (d) 4
 - (e) 1

5. Decode the “word” izt knowing it was encoded using the cipher $3x - 1$

- (a) man
- (b) set
- (c) day
- (d) lcw
- (e) none of the above

6. Which of the following is irreducible?

- (a) $x^4 + 2x^2 + 2$
- (b) $x^2 - 2x - 2$
- (c) $x^2 + 2x + 1$
- (d) $x^3 + x^2 + 1$
- (e) $x^2 + 2x + 4$

7. If $\frac{4 - i}{1 - 2i} = a + ib$ for $a, b \in \mathbb{R}$ then $b =$

- (a) $\frac{6}{5}$
- (b) $\frac{7}{5}$
- (c) $\frac{8}{5}$
- (d) $\frac{9}{5}$
- (e) none of the above

8. If $\sqrt{2 + i} = a + ib$ for $a, b \in \mathbb{R}$ then $b =$

- (a) $\sqrt{1 + \frac{1}{2}\sqrt{5}}$
- (b) $\sqrt{2 + \frac{1}{2}\sqrt{5}}$
- (c) $\sqrt{3 + \frac{1}{2}\sqrt{5}}$
- (d) $\sqrt{5 + \frac{1}{2}\sqrt{5}}$
- (e) none of the above

Page left blank for your work.