

Name: _____

Student Number: _____

CHM 2311
Final Exam
April 29 2009
Professor Darrin Richeson

There are 15 pages in this exam (including supporting materials and tables). Please count the pages to make sure none are missing.

You may *carefully remove* the last three pages of the exam and use them for scratch work.

Please write legibly and show your work to receive credit for your answers.
Partial marks *may in some cases* be awarded for partially correct work.

Question	Mark	Question	Mark
1	/5	8	/4
2	/9	9	/13
3	/7	10	/16
4	/16	11	/5
5	/10	12	/12
6	/9		
7	/4		
		Total	/110

Good luck and have a great summer!

1. (5 points) A hydrogen orbital has the following **complete** wave function (both angular and radial portions of the wave function are included and the angular part is written in Cartesian coordinate form):

$$\psi(r, \theta, \varphi) = R(r)\{Y(\theta, \varphi)\} = \frac{1}{81\sqrt{15}} \left(\frac{2Z}{a_0}\right)^{3/2} (\rho)^2 e^{-\rho/3} \left\{ \frac{1}{4} \sqrt{\frac{15}{\pi}} \frac{x^2 - y^2}{r^2} \right\}$$

where $\rho = \frac{Zr}{a_0}$ and $Z = 1$ for a hydrogen atom

$$a_0 = 52.9 \text{ pm}$$

- a. For this orbital, determine the distance from the nucleus in picometers at which **all radial** nodes occur.

The radial component becomes zero (has a node) when $\rho^2 = 0$ or $\rho = 0 = Zr/a_0$

*This is only true at the $r = 0$ – the nucleus **no radial nodes***

- b. Determine the quantum numbers n and l for this orbital. **Clearly** show the process by which you determined these values. Identify the orbital (1s, 2s, 2p_x, etc...).

*In part (a) we determined that there are **no radial nodes**.*

The number of angular nodes can be determined from the angular part of the wavefunction. From the equation, $\psi = 0$ for $x^2 - y^2 = 0$ (and all values for z). Rearranging gives a node for $x = y$ and for $x = -y$

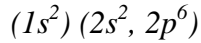
There are 2 angular nodes. This corresponds to $l = 2$ or a d orbital.

The equation for the number of radial nodes is given by $n - l - 1 = \text{number of radial nodes}$. Since $n - l - 1 = 0$ then $n = 2 + 1 = 3$

Therefore this is a 3d orbital and specifically the 3d_{x²-y²} orbital.

2. (9 points) a. Calculate Z_{eff} for a 2p electron on each of the following species. O^{2-} , F^- , Na^+ , Mg^{2+} .

Each of these ions has the same electronic configuration:



This means that they all have the same s value

$$s = (2 \times 0.85) + (7 \times 0.35) = 4.15$$

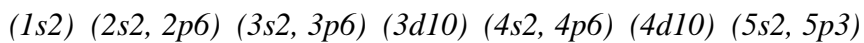
$$Z_{\text{eff}} = Z_{\text{actual}} - s$$

Ion	Z	Z_{eff}
O^{2-}	8	3.85
F^-	9	4.85
Na^+	11	6.85
Mg^{2+}	12	7.85

Match the ion with the radii in the following table.

Crystal (Ionic) Radius	Ion
119pm	
86pm	
116pm	
126pm	

Calculate the Z_{eff} for a 4d electron of antimony (symbol Sb)

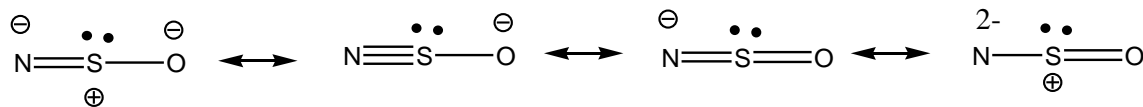


$$Z_{\text{eff}} = Z - s = 51 - 9 \times 0.35 + 36 \times 1 = 51 - 3.15 = 47.85$$

3. (7 points) There are potentially three isomers for the anion NSO^- . The two known species are NSO^- and SNO^- . The isomer SON^- is unknown. Suggest reasonable resonance structures for each of these three isomers.

There are 18 electrons in this anion.

The following are reasonable Lewis structures for the NSO^- ion:



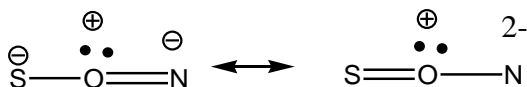
Other Lewis structures can be drawn with more bonds on O or S, but this creates unlikely positive formal charges on oxygen, the most electronegative of the three atoms. The second structure shown (triple bond between N and S) should be most correct, as it not only involves the lowest formal charges, but has the negative formal charge on the most electronegative atom (O).

For the SNO^- ion:



The most correct Lewis structure should be the second one (S-N double bond). Again, the negative formal charge is on the O-atom for this structure. Other structures can be drawn, but again, positive formal charges on O or structures which break the octet rule would be obtained.

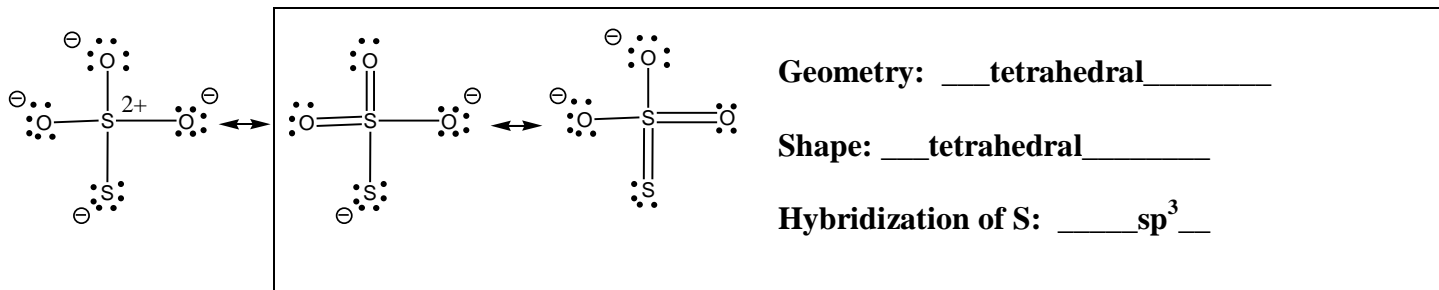
For the SON^- ion, both reasonable resonance structures have positive formal charges on O.



4. (16 points) Draw the most stable Lewis structure and all *significant* resonance contributors for each of the molecules below. In your final answer, show all bonded pairs of electrons as lines between the bonded atoms and show all non-bonded electrons as dots. Indicate any *non-zero formal charges* on every element where they occur.

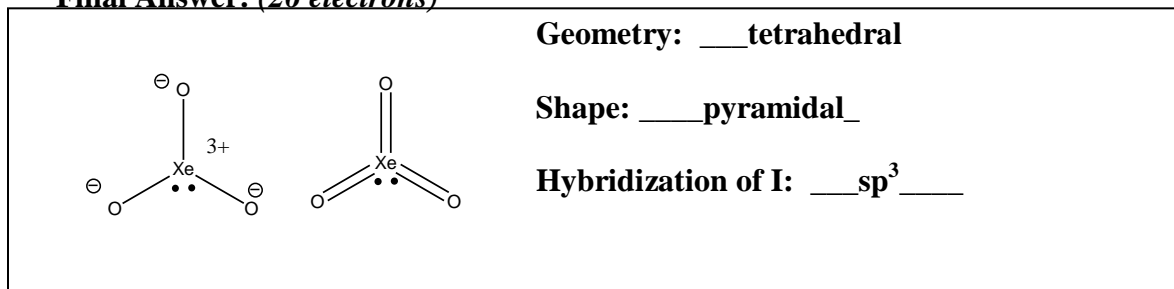
a. SSO_3^{2-} (thiosulfate)

Final Answer: (32 electrons)



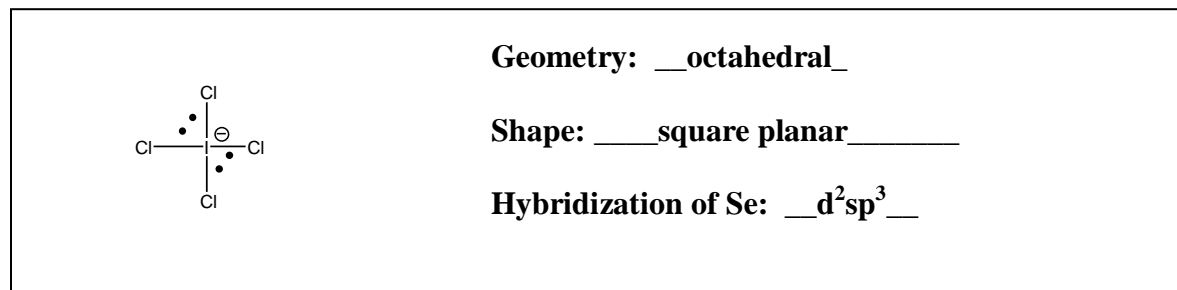
b. XeO_3

Final Answer: (26 electrons)



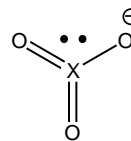
c. ICl_4^-

Final Answer: (36 electrons)



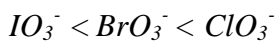
5. (10 points) The series of halate anions IO_3^- , BrO_3^- , and ClO_3^- is known.

This part is not necessary – 26 electrons



Predict a trend in bond angles for these species. Explain.

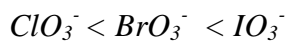
_____ < _____ < _____



*The larger the central atom allows for closer approach of the bonding pairs = smaller angle
(could also mention the decreasing relative role of s orbital in bonding down the group)*

Predict a trend in bond lengths for these species. Explain.

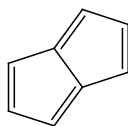
_____ < _____ < _____



As the radius increases the bond length increases – $R_I > R_{Br} > R_{Cl}$

6. (9 points) Determine the point group for each of the following molecules.

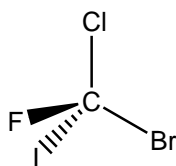
A.



(planar)

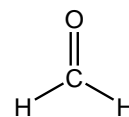
Point Group: A. D_{2h}

B.



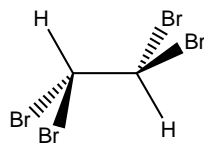
B. C₁

C.



C. C_{2v}

D.



Point Group: D. C_{2h}

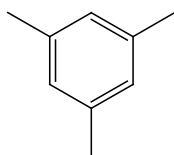
E. SbF₅

E. D_{3h}

F. d_{xz} orbital

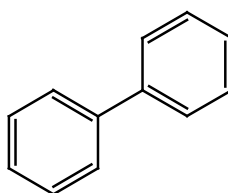
F. D_{2h}

G.



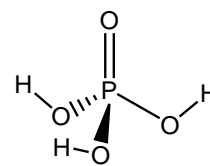
Point Group: A. D_{3h}

H.



B. D_{2h}

I.



C. C_{3v}

7. (4 points; ½ point per blank) In the questions below you will determine the irreducible representations for specific orbitals on a central atom of a molecule in a given point group. You may use the back of one of the exam pages for your scratch work. It is *not necessary to determine the symmetry labels*.
- a. A d_z^2 orbital on the central atom of a molecule in the D_3 point group

D_3	E	$2C_3$	$3C_2$		
	1	1	1		d_z^2

- b. A p_z orbital on the central atom of a molecule in the D_{3h} point group

D_{3h}	E	$2C_3$	$3C_2$	σ_h	$2S_3$	$3\sigma_v$	
	1	1	-1	-1	-1	1	p_z

8. (4 points; ½ point per blank) Given the symmetry labels for the following irreducible representations, fill in the missing characters:

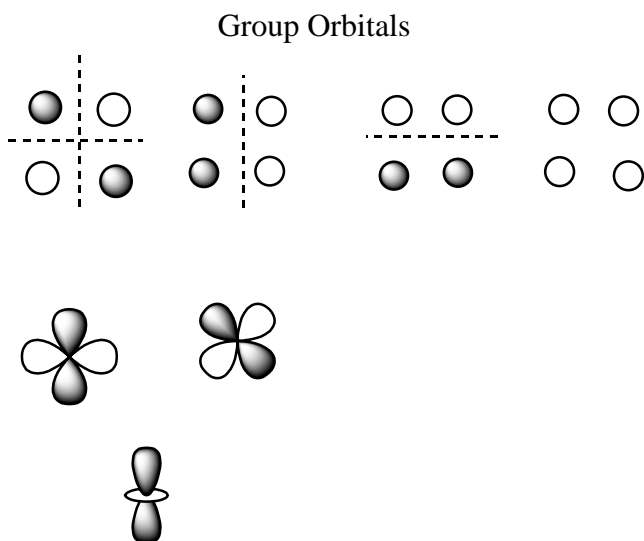
C_{3v}	E	$2C_3$	$3\sigma_v$
A_2	1	1	-1

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v'(yz)$	
B_2	1	-1	-1	1	d_{yz}

D_{3d}	E	$2C_3$	$3C_2$	i	$2S_6$	$3\sigma_d$
A_{2g}	1	1	-1	1	1	-1

9. (13 points) We discussed the bonding in a planar AH_4 species. In this problem we will extend these ideas to include d orbitals on the central A atom.

- What are the group orbitals for planar AH_4 ? (provide simple drawings)
- Consider all of the d orbitals on the central atom. Clearly indicate the group orbitals that have appropriate symmetry to interact with the d orbitals on A?
- What is the maximum number of bonds that could be made for this hypothetical AH_4 molecule?



No interactions with xz or yz

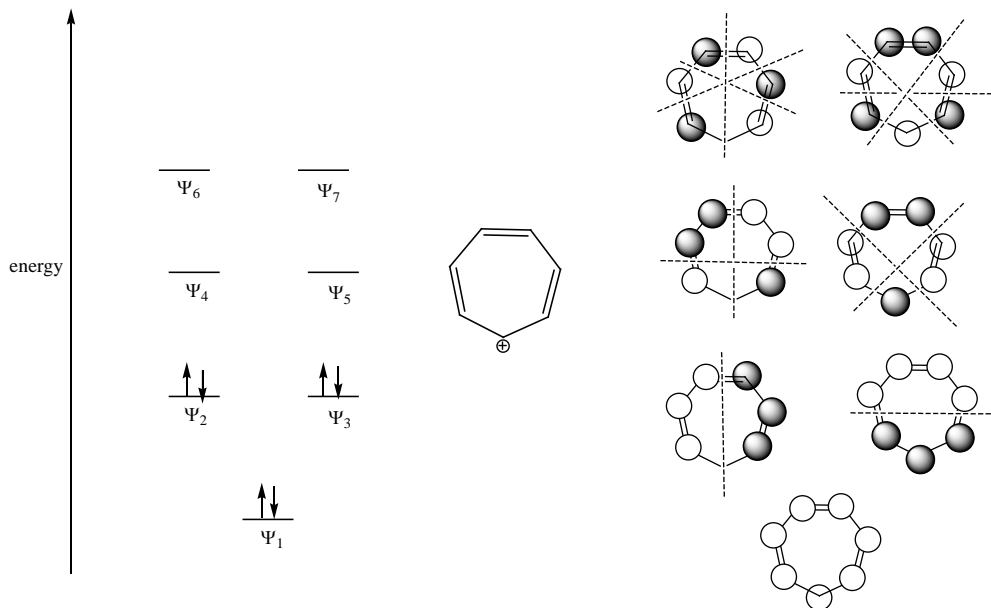
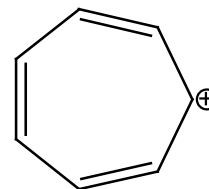
Two possible interactions z^2 and 4th orbital, x^2-y^2 and the 1st **OR** xy and 1st orbital
(depends on orientation of x and y axes)

As a result two bonds can form.

To get interactions with 2nd and 3rd orbitals would use the p_x and p_y . The 4th can also interact with an s orbital.

10. a. (15 points) In the space below, draw a π -MO diagram for the cycloheptatrienyl cation. Your diagram should include the following:

- Sketches of all of the bonding and antibonding π -orbitals
- Relative energy levels of all orbitals indicated by appropriate placement of orbitals on the vertical energy axis.
- Electrons in the appropriate molecular orbitals



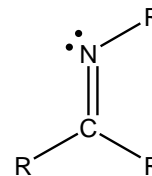
Could also do this from the linear arrangement and then cyclize – see my notes

b. (2 points) Does the Hückel rule predict that the cycloheptatrienyl cation will be aromatic or antiaromatic? Is your MO diagram consistent with this prediction? Explain.

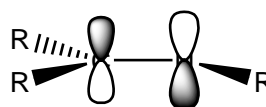
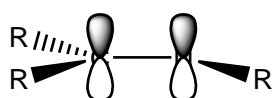
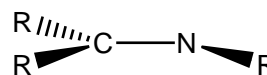
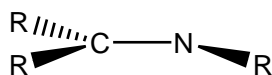
There are 6π electrons which is $4n+2$ π electrons ($n = 1$): Huckel's rule predicts aromaticity

As shown in the MO diagram above, the highest-occupied orbital of the cycloheptatrienyl cation would be bonding and stabilized. This indicates the delocalization in the ring results in stabilization, which is consistent with the prediction of Huckel's rule

11. The molecule shown to the right belongs to a class called “imines”. (R represents a substituent group whose identity is not important for this problem.) All of the atoms of the imine are in the same plane. Even though you might not know anything about imines, you should be able to apply the orbital concepts to explain some reactivity.



- a. (2 points) A nucleophile is a chemical reagent that reacts with a site of positive charge on another molecule. Such a reaction can be viewed as the nucleophile donating a pair of electrons. To evaluate attack of the imine π -system by a nucleophile, we need to identify the HOMO and LUMO orbitals of the imine. On the skeletons below, sketch these “frontier orbitals” and label them as HOMO and LUMO respectively.



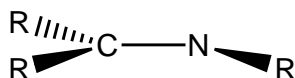
HOMO pi

Lumo pi star

- b. (1 point) Circle the orbital above whose interaction with the nucleophile is most important to the success of this reaction.

HOMO localized on N and LUMO localized on C

- c. (2 points) Will the nucleophile be more likely to attack at the C or the N atom? Use an arrow to show the preferred **angle of approach** of the nucleophile on the skeleton below and explain the rationale behind your prediction.



Attack at C.

12. (12 points) In this problem you will prepare a molecular orbital diagram for the π **system only** for the molecule ozone (O_3). Explain clearly the steps that you use to reach your final answer. You should clearly indicate the nature of all of the π interactions in your MO energy level diagram, indicate the number of electrons involved in the π system and provide the **overall** bond order for ozone?

Analogue of allyl anion.

18 electrons or 9 pairs

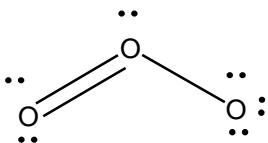
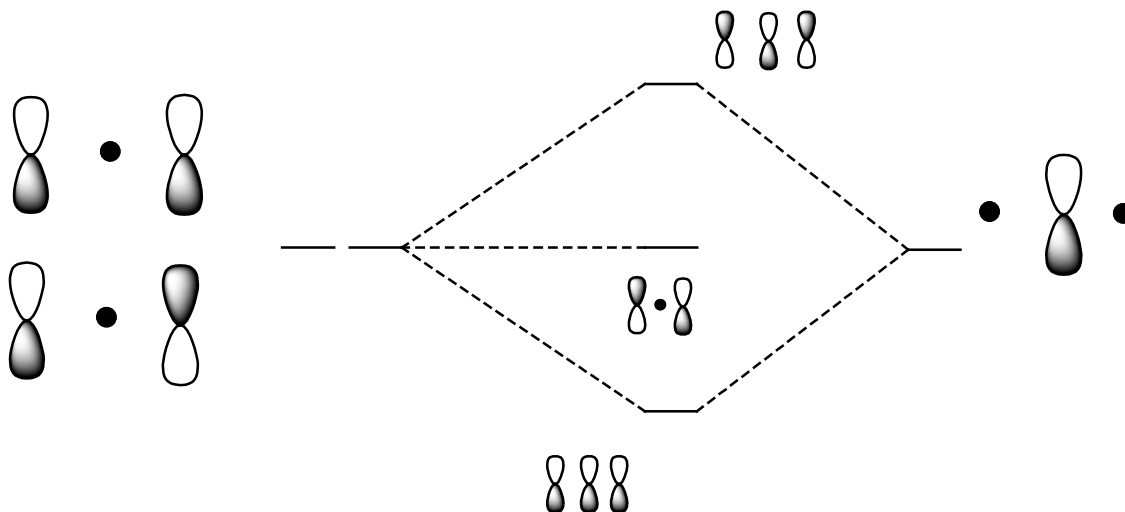
2 pairs for sigma bonds

2 lone pairs on the outer O = 4 pairs

1 lone pair on the central O = 1 pair

7 pairs are used for the non- π bonding leaving 2 pairs for π

Group (outer)



Element	Orbital Potential Energy (eV)						
	1s	2s	2p	3s	3p	4s	4p
H	-13.6						
He	-24.5						
Li		-5.5					
Be		-9.3					
B		-14.0	-8.3				
C		-19.5	-10.7				
N		-25.5	-13.1				
O		-32.4	-15.9				
F		-46.4	-18.7				
Ne		-48.5	-21.6				
Na				-5.2			
Mg				-7.7			
Al				-11.3	-6		
Si				-15.0	-7.8		
P				-18.7	-10.0		
S				-20.7	-12.0		
Cl				-25.3	-13.7		
Ar				-29.3	-15.9		
K						-4.3	
Ca						-6.1	
Zn						-9.4	
Ga						-12.6	-6
Ge						-15.6	-7.6
As						-17.6	-9.1
Se						-20.8	-11.0
Br						-24.1	-12.5
Kr						-27.5	-14.3

D _{2h}	E	C ₂ (z)	C ₂ (y)	C ₂ (x)	<i>i</i>	σ(xy)	σ(xz)	σ(yz)	
A _g	1	1	1	1	1	1	1	1	x ² , y ² , z ²
B _{1g}	1	1	-1	-1	1	1	-1	-1	R _z , xy
B _{2g}	1	-1	1	-1	1	-1	1	-1	R _y , xz
B _{3g}	1	-1	-1	1	1	-1	-1	1	R _x , yz
A _u	1	1	1	1	-1	-1	-1	-1	
B _{1u}	1	1	-1	-1	-1	-1	1	1	z
B _{2u}	1	-1	1	-1	-1	1	-1	1	y
B _{3u}	1	-1	-1	1	-1	1	1	-1	x

C_{4v}	E	$2C_4$	C_2	$2\sigma_v$	$2\sigma_d$	
A_1	1	1	1	1	1	z, x^2+y^2, z^2
A_2	1	1	1	-1	-1	R_z
B_1	1	-1	1	1	-1	x^2-y^2
B_2	1	-1	1	-1	1	xy
E	2	0	-2	0	0	$(x,y) (R_x, R_y) (xz, yz)$

D_{4h}	E	$2C_4$	C_2	$2C_2'$	$2C_2''$	i	$2S_4$	σ_h	$2\sigma_v$	$2\sigma_d$	
A_{1g}	1	1	1	1	1	1	1	1	1	1	x^2+y^2, z^2
A_{2g}	1	1	1	-1	-1	1	1	1	-1	-1	R_z
B_{1g}	1	-1	1	1	-1	1	-1	1	1	-1	x^2-y^2
B_{2g}	1	-1	1	-1	1	1	-1	1	-1	1	xy
E_g	2	0	-2	0	0	2	0	-2	0	0	(xz, yz)
A_{1u}	1	1	1	1	1	-1	-1	-1	-1	-1	
A_{2u}	1	1	1	-1	-1	-1	-1	-1	1	1	z
B_{1u}	1	-1	1	1	-1	-1	1	-1	-1	1	
B_{2u}	1	-1	1	-1	1	-1	1	-1	1	-1	
E_u	2	0	-2	0	0	-2	0	2	0	0	(x, y)

1		2		3		4		5		6		7		8		9		10		11		12		13		14		15		16		17		18	
IA		IIA		IIIB		IIB		VIIB		VIB		VIB		VIB		VIII		VIII		IB		IIB		IIIA		IVA		VA		VIA		VIIA		VIIIA	
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
Electronegativity	Symbol	Atomic number	Relative atomic mass	Most frequent oxidation number	Name	Electronegativity	Symbol	Atomic number	Relative atomic mass	Most frequent oxidation number	Name	Electronegativity	Symbol	Atomic number	Relative atomic mass	Most frequent oxidation number	Name	Electronegativity	Symbol	Atomic number	Relative atomic mass	Most frequent oxidation number	Name	Electronegativity	Symbol	Atomic number	Relative atomic mass	Most frequent oxidation number	Name	Electronegativity	Symbol	Atomic number	Relative atomic mass	Most frequent oxidation number	Name
2.1	H 1	1.00794	1.00794	1+	Hydrogen	2.1	H 1	1.00794	1.00794	1+	Hydrogen	2.1	H 1	1.00794	1.00794	1+	Hydrogen	2.1	H 1	1.00794	1.00794	1+	Hydrogen	2.1	H 1	1.00794	1.00794	1+	Hydrogen	2.1	H 1	1.00794	1.00794	1+	Hydrogen
1.0	Li 3	6.941	9.012182	1+	Lithium	1.5	Be 4	9.012182	9.012182	2+	Beryllium	1.0	Li 3	6.941	9.012182	1+	Lithium	1.5	Be 4	9.012182	9.012182	2+	Beryllium	1.0	Li 3	6.941	9.012182	1+	Lithium	1.5	Be 4	9.012182	9.012182	2+	Beryllium
0.9	Na 11	22.989768	22.989768	1+	Sodium	1.2	Mg 12	24.3050	24.3050	2+	Magnesium	0.8	K 19	39.0983	39.0983	1+	Potassium	1.3	Ca 20	40.078	40.078	2+	Calcium	0.8	K 19	39.0983	39.0983	1+	Potassium	1.3	Ca 20	40.078	40.078	2+	Calcium
0.8	Rb 37	85.4678	85.4678	1+	Rubidium	1.3	Sr 38	87.62	87.62	2+	Strontium	1.0	Y 39	88.90585	88.90585	3+	Yttrium	1.3	Zr 40	91.224	91.224	4+	Zirconium	1.0	Y 39	88.90585	88.90585	3+	Yttrium	1.3	Zr 40	91.224	91.224	4+	Zirconium
0.7	Cs 55	132.90543	132.90543	1+	Cesium	1.1	Ba 56	137.327	137.327	2+	Barium	0.7	Fr 87	223.0197	223.0197	1+	Francium	1.1	La 57	138.9055	138.9055	3+	Lanthanum	1.1	Ba 56	137.327	137.327	2+	Barium	0.7	Fr 87	223.0197	223.0197	1+	Francium
0.7	Fr 87	223.0197	223.0197	1+	Francium	1.1	Ba 56	137.327	137.327	2+	Barium	0.7	Fr 87	223.0197	223.0197	1+	Francium	1.1	La 57	138.9055	138.9055	3+	Lanthanum	1.1	Ba 56	137.327	137.327	2+	Barium	0.7	Fr 87	223.0197	223.0197	1+	Francium
0.7	Fr 87	223.0197	223.0197	1+	Francium	1.1	Ba 56	137.327	137.327	2+	Barium	0.7	Fr 87	223.0197	223.0197	1+	Francium	1.1	La 57	138.9055	138.9055	3+	Lanthanum	1.1	Ba 56	137.327	137.327	2+	Barium	0.7	Fr 87	223.0197	223.0197	1+	Francium

Under normal conditions, bold symbols correspond to solid state, bold italics correspond to liquid state, italic correspond to gaseous state and normal correspond to synthetic elements.