

Full Name: _____

Seat Number: _____

Student Number: _____

CHM 2311
Midterm 1
February 26, 2009
Professor Darrin Richeson

You have 80 minutes to complete this exam.

Please read the questions carefully.

There some useful equations and a periodic table on the last 2 pages of the exam.

Please write legibly and show your work to receive credit for your answers.

Partial marks *may in some cases* be awarded for partially correct work.

| Question | Mark | | Question | Mark |
|--------------|-------------|--|-----------|-------------|
| 1 | / 10 | | 6 | / 2 |
| 2 | / 6 | | 7 | / 5 |
| 3 | / 5 | | 8 | / 12 |
| 4 | / 3 | | 9 | / 8 |
| 5 | / 3 | | 10 | / 6 |
| Total | | | | /60 |

1. (10 points) In class, we looked at a one-dimensional particle in a box with infinite potential energy walls and length of a .

(a) A ground state electron in a one-dimensional box absorbs 1480 nm light. The box has a length of 1.34 nm. What is the value of n for this excited particle?

First notice that this is a particle in a box not a hydrogen atom. We do not use the Balmer equation!

Also note that the ground state of the electron is $n = 1$

Energy of 1480 nm light using $E = h\nu = hc/\lambda = 6.626 \times 10^{-34} \text{ Js } (3 \times 10^8 \text{ m/s}) / 1480 \times 10^{-9} \text{ m}$

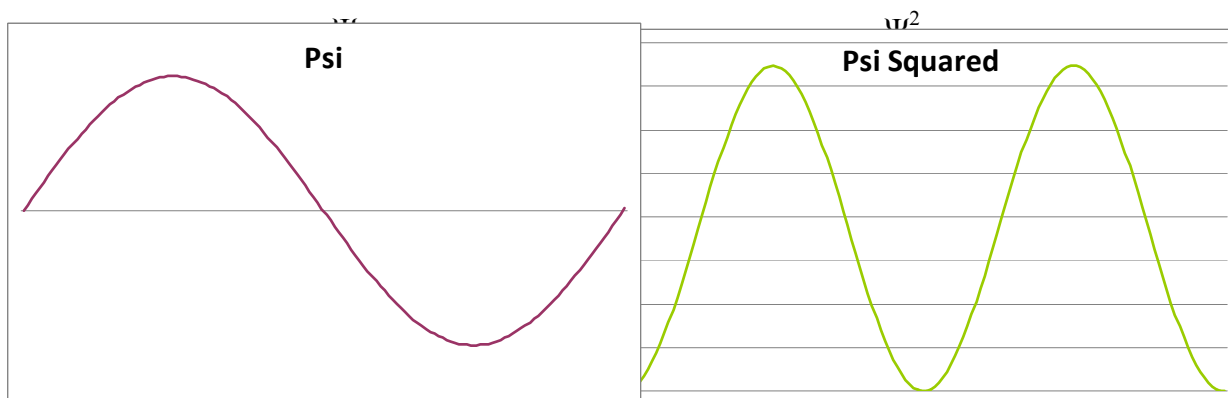
$E = 1.34 \times 10^{-19} \text{ J}$ This value corresponds to the energy difference between the $n = 1$ and n state
Now we need to calculate the value of n using this energy:

$$n^2 = \frac{E8ma^2}{h^2} = \frac{(1.34 \times 10^{-19} \text{ J})(8)(9.11 \times 10^{-31} \text{ kg})(1.34 \times 10^{-9} \text{ m})^2}{(6.626 \times 10^{-34} \text{ J} \cdot \text{s})^2}$$

$$n^2 = 4.0$$

$$n = 2$$

(b) Sketch the wave function, ψ , and the probability function, ψ^2 , for the quantum level, n , found in part (a) above.



(c) What value(s) of x correspond to a minimum probability for the electron?

At the values 0 and a

Also at the value $a/2$

2. (6 points) After the particle in a box, we moved to solutions of the Schrödinger equation in three dimensions and obtained 3 quantum numbers.

What are their symbols and possible values?

| Quantum number | Possible Values |
|----------------|-------------------------|
| n | Integers beginning at 1 |
| l | 0, 1, 2...n-1 |
| m_l | -l...0...+l |

3. (5 points) The angular portion of a hydrogen orbital can be expressed in either Cartesian or polar coordinates. An example of an angular wave function is given by:

Cartesian coordinates
$$Y(x, y, z) = \sqrt{\frac{15}{4\pi}} \frac{xz}{r^2}$$

(a). Which planes (a plane being defined by two of the three coordinates x, y or z) correspond to nodes for this orbital?

*Zero values are obtained for $x = 0$ and any values of z or y
or $z = 0$ and any value of x and y .*

*This is equivalent to saying that there are nodes for the **xy plane** (perpendicular to the z axis) and for the **yz plane** (perpendicular to the x axis).*

(b) If this same orbital has 1 **radial** node, identify the orbital using the conventional label (e.g. 2s, 4p_x, 3d_{z²}, etc.) and **show the thought process** by which you were able to reach your answer.

This orbital has two angular nodes and is therefore a d orbital. More specifically it is the d_{xz} orbital. The fact that there is one radial node indicates that it is the 4d_{xz}.

4. (3 points) Calculate Z_{eff} for an electron in the 4p orbital of the Sn atom.

Electronic configuration of Sn $[\text{Kr}] 5s^2 4d^{10} 5p^2 = [1s^2 2s^2 2p^6 3s^2 3p^6 4s^2 3d^{10} 4p^6] 5s^2 4d^{10} 5p^2$
 $(1s^2)(2s^2 2p^6)(3s^2 3p^6)(3d^{10}) (4s^2 4p^6)(4d^{10})(5s^2 5p^2)$

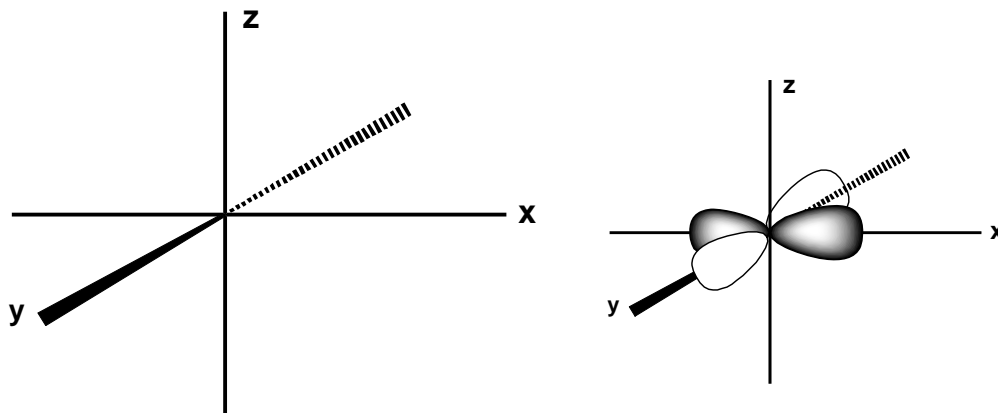
See slide 194 from Ch. 2 – the electrons to the right of the 4p do not shield the 4p

$$0.35 \times 7 + 0.85 \times 18 + 10 \times 1 = 27.75 = \sigma$$

$$Z_{\text{eff}} = Z - \sigma = 50 - 27.75 = 22.25$$

5. (3 points) We learned in class and from the text that we can only distinguish between areas of high-probability and low-probability for the electron density. We can be sure of the location of zero-probability features of the orbitals.

(a) (2 point) Sketch the $3d(x^2 - y^2)$ orbital on the coordinate axes provided. Clearly indicate the phase of each lobe



b) (1 point) How many angular nodes does the $3d(x^2 - y^2)$ have? 2

6. a) (1 point, no part marks) Arrange the following in order of increasing ionization energy.

Na, K, Cl, P Cl > P > Na > K

b) (1 point, no part marks) Arrange the following in order of increasing (more negative) electron affinity.

P, Al, In, Cl Cl > P > Al > In

7. (5 points) Provide a detailed valence electronic configuration including the number of unpaired electrons for a phosphorus atom? Is this atom paramagnetic or diamagnetic? PCl₅ is a stable compound. Using your answer in part (a), provide a valence bond description (including hybridization) for the bonding in this compound.

$1s^2 2s^2 2p^6 3s^2 3p^3$ or $[Ne] 3s^2 3p^3$

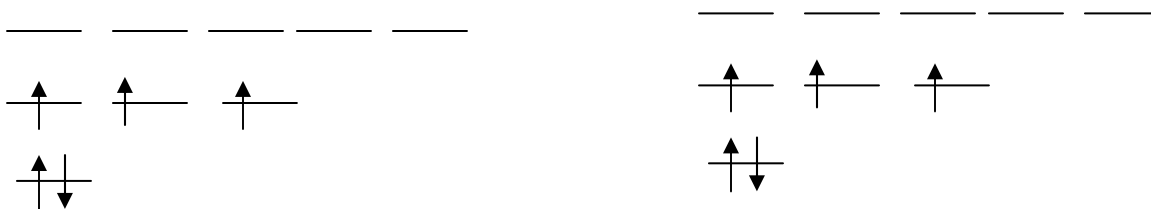
The three electrons in the 3p level are unpaired and thus the atom is paramagnetic

3points

See slide 153

Using unhybridized orbitals, P can only form 3 bonds to chlorine atoms. In order to make 5 bonds we will need 5 unpaired electrons. Promote one of the 3s electrons to the 3 d level. Hybridization of the 3s + 3x3p + 1x3d = dsp³ 5 singly-occupied sp³d orbitals can now be used to make 5 P-Cl bonds

3p
3s



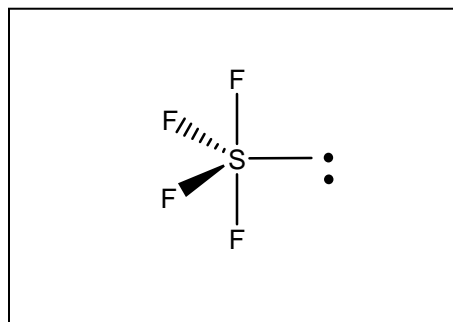
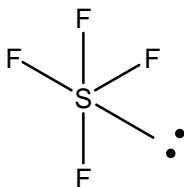
2points

8. (12 points, 1/2 point per blank; *no partial credit*) For the following molecules:
 Draw the Lewis structure
 Determine the VSEPR shape and geometry of the molecule
 Draw the three-dimensional representation of the molecule in the box provided
 Determine whether the molecule is polar or non-polar
 Give the hybridization of the central atom
 Indicate any *non-zero formal charges* on every element where they occur.

(a). SF₄

3-D Drawing:

LEWIS: $6 + 7 \times 4 = 34$ electrons



Geometry: _____ trigonal bipyramidal _____

Shape: _____ seesaw _____

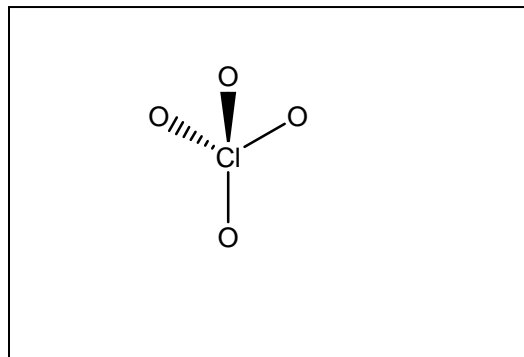
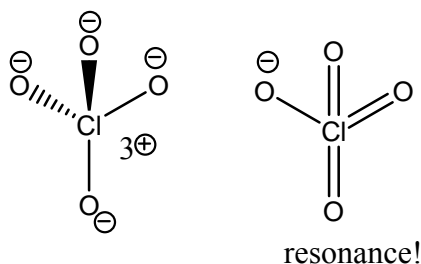
Polarity: _____ yes _____

Hybridization: _____ sp³ _____

(b) ClO₄⁻

3-D Drawing:

LEWIS: $4 \times 6 + 7 + 1 = 32$ electrons



Geometry: _____ Tetrahedral _____

Shape: _____ Tetrahedral _____

Polarity: _____ no _____

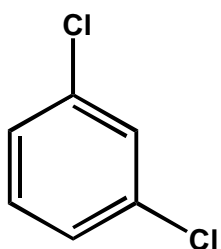
Hybridization: _____ sp³ _____

9. (8 points, 1 point each; *no partial credit*) For the following molecules or ions, indicate highest rotation axis and if there is a plane of reflection.

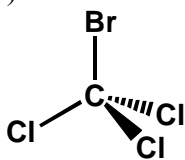
Example: BF_3 C_3, σ_h

(a) N_3^- (a) C_∞, σ_h and/or σ_v

(b) (b) C_2, σ_v



(c) (c) C_3, σ_v

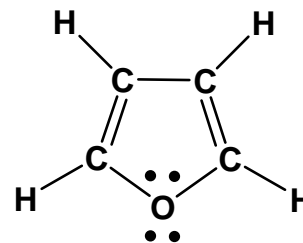


(d) NO_3^- (d) C_3, σ_h and/or σ_v

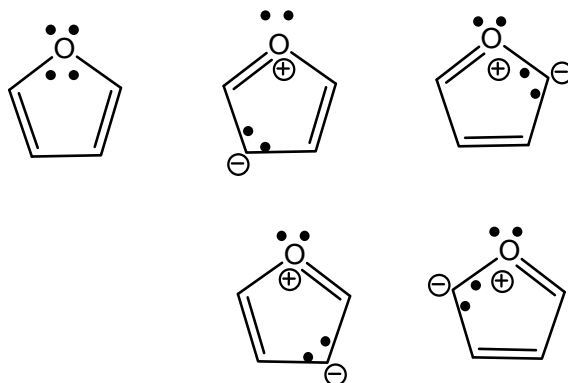
10. The following represents the Lewis structure and geometry of furan:

(1 point) What are the hybridizations of the carbon atoms in this depiction? sp^2

(1 point) Based on this drawing, how many σ -bonds and the π -bonds on the molecule? 9,2

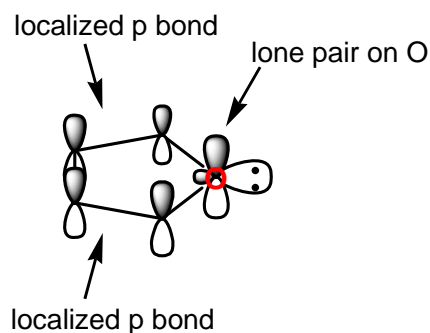


(2 points) Resonance structures for furan can be drawn by using the lone electron pairs on O for bonding with adjacent C. Draw a possible resonance structure with appropriate formal charges.



(2 points) Accounting for the additional resonance structures, what type of orbital must the lone electron pairs on oxygen be occupying? Explain.

If the lone pair is going to overlap with the p-bonding frame of the C atoms, it must be in a p orbital that lines up with these. This would give an sp^2 hybridized O. The remaining lone pair would be in an sp^2 hybrid.



Useful equations, constants, and conversion factors:

$$E = hc/\lambda \quad E = R_H \left(\frac{1}{n_l^2} - \frac{1}{n_h^2} \right) \quad E_{PIB} = \frac{n^2 h^2}{8ma^2} \quad \psi_{PIB} = \sqrt{\frac{2}{a}} \sin\left(\frac{n\pi x}{a}\right)$$

$$\left[-\left(\frac{h^2}{8\pi^2 m}\right) \left(\frac{d^2}{dx^2} + \frac{d^2}{dy^2} + \frac{d^2}{dz^2} \right) + V \right] \Psi = E\Psi \quad \lambda = h/p$$

$\psi(r, \theta, \phi) = R(r)Y(\Theta, \Phi)$ The volume element is $r^2 \sin\Theta d\Theta d\Phi dr$

Angular wave functions: $Y(\Theta, \Phi) = (1/4\pi)^{1/2} y(\Theta, \Phi)$

| orbital | $y(\Theta, \Phi)$ |
|-------------------|--|
| S | 1 |
| Pz | $3\cos\Theta$ |
| px, py | $(2/3)^{1/2} \sin\Theta e^{\pm i\Phi}$ |
| dz^2 | $(5/4)^{1/2} (3\cos 2\Theta - 1)$ |
| Dyz, dxz | $(15/4)^{1/2} \sin\Theta \cos\Theta e^{\pm i\Phi}$ |
| $dx^2 - y^2, dxy$ | $(15/8)^{1/2} \sin 2\Theta e^{\pm 2i\Phi}$ |

$h = \text{Planck's constant} = 6.626 \times 10^{-34} \text{ J s}$

$R_H = 2.179 \times 10^{-18} \text{ J}$

$1 \text{ m} = 10^9 \text{ nm} = 10^{12} \text{ pm}$

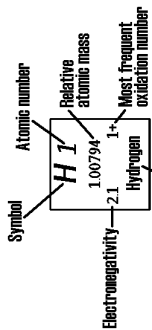
electron mass = $9.11 \times 10^{-31} \text{ kg}$

$c = \text{speed of light} = 2.998 \times 10^8 \text{ m s}^{-1}$

Bohr radius (a_0) = 52.9 pm

$1 \text{ J} = 1 \text{ kg m}^2 \text{ s}^{-2}$

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|-----------------------------------|---------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|--------------------------------------|--------------------------------------|--------------------------------------|-----------------------------------|------------------------------------|-----------------------------------|------------------------------------|-------------------------------|---------------------------------------|------------------------------------|------------------------------------|-------------------------------|-------------------------------|--------------------------------------|--------------------------------|------------------------------------|---------------------------------|--------------------------------------|---------------------------------|---------------------------------|----------------------------------|---------------------------------|-----------------------------------|-------------------------------------|-----|--|------|--|-------|--|
| 1 | | 2 | | 3 | | 4 | | 5 | | 6 | | 7 | | 8 | | 9 | | 10 | | 11 | | 12 | | 13 | | 14 | | 15 | | 16 | | 17 | | 18 | |
| IA | | IIA | | IIIB | | IVB | | VB | | VIB | | VIIB | | VIII | | IB | | IIB | | IIIA | | IIIA | | IIIA | | IVA | | VA | | VIA | | VIIA | | VIIIA | |
| H 1 1.00794 Hydrogen | Li 3 6.941 Lithium | Na 11 22.989768 Sodium | K 19 39.0983 Potassium | Rb 37 85.4678 Rubidium | Cs 55 132.90543 Cesium | Fr 87 223.0197 Francium | Be 4 9.012182 Beryllium | Mg 12 24.3050 Magnesium | Ca 20 40.078 Calcium | Sr 38 87.62 Strontium | Ba 56 137.327 Barium | Ra 88 226.0254 Radium | B 5 10.811 Boron | Al 13 26.981539 Aluminum | Si 14 28.0855 Silicon | Ge 32 72.61 Germanium | Sn 50 118.71 Tin | Pb 82 207.2 Lead | Uuq 114 289 Ununquadium | C 6 12.011 Carbon | N 7 14.00674 Nitrogen | O 8 15.9994 Oxygen | F 9 18.9984032 Fluorine | Ne 10 20.1797 Neon | Ar 18 39.948 Argon | Kr 36 83.80 Krypton | Xe 54 131.29 Xenon | Rn 86 222.0176 Radon | Uuo 118 293 Ununoctium | | | | | | |
| 1 | | 2 | | 3 | | 4 | | 5 | | 6 | | 7 | | 8 | | 9 | | 10 | | 11 | | 12 | | 13 | | 14 | | 15 | | 16 | | 17 | | 18 | |
| IA | | IIA | | IIIB | | IVB | | VB | | VIB | | VIIB | | VIII | | IB | | IIB | | IIIA | | IIIA | | IIIA | | IVA | | VA | | VIA | | VIIA | | VIIIA | |
| H 1 1.00794 Hydrogen | Li 3 6.941 Lithium | Na 11 22.989768 Sodium | K 19 39.0983 Potassium | Rb 37 85.4678 Rubidium | Cs 55 132.90543 Cesium | Fr 87 223.0197 Francium | Be 4 9.012182 Beryllium | Mg 12 24.3050 Magnesium | Ca 20 40.078 Calcium | Sr 38 87.62 Strontium | Ba 56 137.327 Barium | Ra 88 226.0254 Radium | B 5 10.811 Boron | Al 13 26.981539 Aluminum | Si 14 28.0855 Silicon | Ge 32 72.61 Germanium | Sn 50 118.71 Tin | Pb 82 207.2 Lead | Uuq 114 289 Ununquadium | C 6 12.011 Carbon | N 7 14.00674 Nitrogen | O 8 15.9994 Oxygen | F 9 18.9984032 Fluorine | Ne 10 20.1797 Neon | Ar 18 39.948 Argon | Kr 36 83.80 Krypton | Xe 54 131.29 Xenon | Rn 86 222.0176 Radon | Uuo 118 293 Ununoctium | | | | | | |



| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|-----------------------------------|---|-------------------------------------|--|------------------------------------|-------------------------------------|--------------------------------------|--------------------------------------|--------------------------------------|--------------------------------------|----------------------------------|--------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|---|------------------------------------|---------------------------------------|---------------------------------------|---------------------------------------|-------------------------------|---------------------------------------|---|---|--------------------------------------|--|---------------------------------------|---|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|----|--|
| 6 | | 7 | | 8 | | 9 | | 10 | | 11 | | 12 | | 13 | | 14 | | 15 | | 16 | | 17 | | 18 | | 19 | | 20 | | 21 | | 22 | | 23 | | 24 | | 25 | | 26 | | 27 | | 28 | | 29 | | 30 | | 31 | | 32 | | 33 | | 34 | | 35 | | 36 | | 37 | | 38 | | 39 | | 40 | | 41 | | 42 | | 43 | | 44 | | 45 | | 46 | | 47 | | 48 | | 49 | | 50 | | 51 | | 52 | | 53 | | 54 | | 55 | | 56 | | 57 | | 58 | | 59 | | 60 | | 61 | | 62 | | 63 | | 64 | | 65 | | 66 | | 67 | | 68 | | 69 | | 70 | | 71 | |
| Ce 58 140.115 Cerium | Pr 59 140.90765 Praseodymium | Nd 60 144.24 Neodymium | Pm 61 144.9127 Promethium | Sm 62 150.36 Samarium | Eu 63 151.965 Europium | Gd 64 157.25 Gadolinium | Tb 65 168.92534 Terbium | Dy 66 162.50 Dysprosium | Ho 67 164.93032 Holmium | Er 68 167.26 Erbium | Tm 69 168.93421 Thulium | Yb 70 173.04 Ytterbium | Lu 71 174.967 Lutetium | Th 90 232.0381 Thorium | Pa 91 231.03588 Protactinium | U 92 238.0289 Uranium | Np 93 237.0471 Neptunium | Pu 94 244.0642 Plutonium | Am 95 243.0614 Americium | Cm 96 247 Curium | Bk 97 247.0703 Berkelium | Cf 98 251.0796 Californium | Es 99 252.0858 Einsteinium | Fm 100 257.0951 Fermium | Md 101 258.10 Mendelevium | No 102 259.1009 Nobelium | Lr 103 260.1053 Lawrencium | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

Under normal conditions, bold symbols correspond to solid state, italic symbols correspond to liquid state, italic bold symbols correspond to gaseous state and normal correspond to synthetic elements.