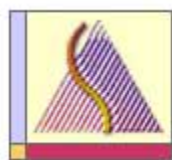




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Principles of Physics  
PHY1322



Department of  
Physics

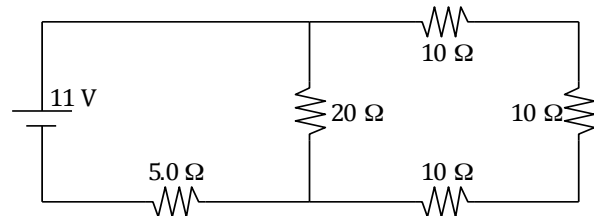
Instructor: Dr. Andrzej Czajkowski  
Final Exam  
April 21, 2015  
Closed book exam  
Duration: 3 hrs  
Return only the scantron sheets

**ELECTRICITY**

- 1E.** Three resistors are connected in parallel. Their resistances  $16\Omega$ ,  $24\Omega$ , and  $48\Omega$ . What is their equivalent resistance in  $\Omega$ ?  
 a) 8                      b) 36                      c) 54                      d) 62                      e) 88
- 2E.** Two charges  $+Q$  and  $+4Q$  are separated by a distance  $r$ . At what distance from the greater charge, would a third test charge experience no net electrical force? /It has to be placed between the two charges/  
 a)  $\frac{3}{2}r$                       b)  $\frac{r}{4}$                       c)  $\frac{r}{2}$                       d)  $\frac{2}{3}r$                       e) impossible to answer
- 3E.** Two charges of  $15\text{ pC}$  and  $-40\text{ pC}$  are inside a cube with sides that are of  $0.40\text{-m}$  length. Determine the net electric flux (in  $\text{Nm}^2/\text{C}$ ) through the whole surface of the cube.  
 a. +2.8                      b. -1.1                      c. +1.1                      d. -2.8                      e. -0.47
- 4E.** Find the electric Field  $E$  at Point  $(1,1,1)$  when the electric potential is given by the function  $V(x,y,z) = 10 + yzx + x^2 + y^2 - 2z^2$   
 a)  $E(1,1,1) = (0,0,0)$                       b)  $E(1,1,1) = (-3,-3,3)$                       c)  $E(1,1,1) = (-4,-4,4)$   
 d)  $E(1,1,1) = (4,4,-4)$                       e) None of the above
- 5 M.** A hemispherical surface (half of a spherical surface) of radius  $R$  is located in a uniform electric field of magnitude  $E$  that is parallel to the axis of the hemisphere. What is the magnitude of the electric flux through the hemisphere surface?  
 a.  $\pi R^2 E$                       b.  $4\pi R^2 E/3$                       c.  $2\pi R^2 E/3$                       d.  $\pi R^2 E/2$                       e.  $\pi R^2 E/3$

6M. What is the magnitude (in V) of the potential difference across the  $20\Omega$  resistor?

- a) 3.2  
 b) 7.8  
 c) 11  
 d) 5.0  
 e) 8.6

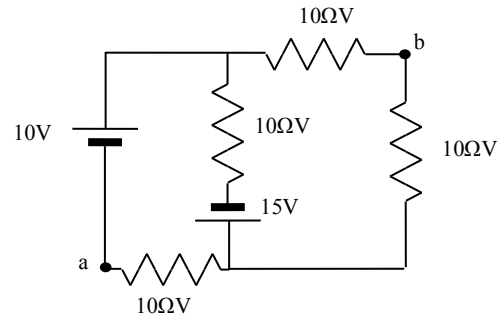


- 7D** As thin spherical metal shell of radius  $R=1\text{m}$  is charged to density of  $+1\text{C}/\text{m}^2$ . A small disk of the radius  $r=5\text{cm}$  ( and the charge that was on it) is then removed from the sphere by means of laser ablation. This process leaves the rest of the sphere unperturbed with its charge density intact. What is the magnitude of the electric field (in  $\text{N}/\text{C}$ ) at the center of the sphere?  
 a)  $70.5 \times 10^6$                       b)  $70.6 \times 10^6$                       c)  $90.5 \times 10^6$                       d)  $90.7 \times 10^6$                       e) none of the above

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**8D.** Determine the potential difference  $V_a - V_b$  shown in the circuit below.

- a.  $-5.0 \text{ V}$
- b.  $+5.0 \text{ V}$
- c.  $-10 \text{ V}$
- d.  $+10 \text{ V}$
- e.  $0 \text{ V}$



**VIBRATIONS AND MECHANICAL WAVES**

**9E.** The amplitude of a system moving with simple harmonic motion is doubled. The total energy will then be

- a) 4 times larger
- b) 3 times larger
- c) 2 times larger
- d) the same
- e) half as much

as before

**10E.** A piano string of density  $0.0050 \text{ kg/m}$  is under a tension of  $1350 \text{ N}$ . Find the velocity ( in m/s) with which a wave travels on the string.

- a) 260
- b) 520
- c) 1040
- d) 2080
- e) 4160

**11E.** Principle of operation of a music synthesizer is based on

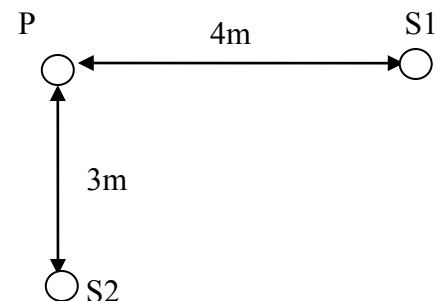
- a) resonance principle
- b) Fourier theorem
- c) logarithmic scale
- d) interference
- e) none of the above

**12E.** By what factor will an intensity change when the corresponding sound level increases by 6 dB?

- a) 3
- b) 0.5
- c) 2
- d) 4
- e) 0.3

**13M.** An observer stands 3 m from speaker A and 4 m from speaker B. Both speakers, oscillating in phase, produce  $170 \text{ Hz}$  waves. The speed of sound in air is  $340 \text{ m/s}$ . What is the phase difference (in radians) between the waves from A and B at the observer's location, point P?

- a) 0
- b)  $\frac{\pi}{2}$
- c)  $\pi$
- d)  $2\pi$
- e)  $4\pi$



**PHY 1322**  
**Dr. Andrzej Czajkowski**

**April 20145**  
**Final Exam: 3 hrs**

**Page 4 of 15**

**OPTICS**

- 14E** An object 50-cm high is placed 1 m in front of a converging lens whose focal length is 1.5 m. Determine the image height (in cm).  
a) 77                      b) 150                      c) 52                      d) 17                      e) 83
- 15E** If a bi-convex lens was made out of very thin clear plastic filled with air, and was then placed underwater where  $n = 1.33$  and where the lens would have an effective index of refraction  $n = 1$ , the lens would act in the same way  
a. as a concave mirror in air.  
b. as a bi-concave lens in air.  
c. as a bi-convex lens in air.  
d. as a flat refracting surface between water and air as seen from the water side.  
e. as the glasses worn by a farsighted person.
- 16E.** The inhabitants of a planet in another galaxy have their eyes at the exact center of their 4.0-m long bodies. How long must a plane mirror be for such a creature to be able to see all of its body in the mirror?  
a) 1.0 m                      b) 2.0 m                      c) 2.5 m                      d) 4.0 m  
e) it depends how far from the mirror is the alien.
- 17E.** Light reflected off a plate-glass window ( $n = 1.5$ ) is found to be completely polarized at angle-of-incidence  $q$ . Find  $q$ .  
a. 56.3°                      b. 5.7°                      c. 21.2°                      d. 18.6°                      e. 33.7°
- 18E** Ideally, how close together in km could 2 objects on the moon's surface be if they can just be resolved by the human eye?  $D$  (Earth-moon) = 385,000 km,  $\lambda$  (visible) =  $5.00 \times 10^{-7}$  m, and  $d$ (pupil) = 0.00700 m. Assume eye fluid has an average  $n = 1.33$ .  
a) 170                      b) 335                      c) 33.5                      d) 25.2                      e) 42.0
- 19M** Parallel beam of light (wavelength= 514nm in the air,  $n=1$ ) enters the medium of refractive index of 1.532. at angle of incidence of  $60^\circ$  to the normal. What is the angle of refraction  $r$  and the wavelength of the light inside the new medium  $\lambda(n)$  ?  
a)  $r = 0.7\text{rad}$ ;  $\lambda(n) = 400\text{nm}$                       b)  $r = 0.6\text{rad}$ ;  $\lambda(n) = 336\text{ nm}$   
c)  $r = 0.6\text{rad}$ ;  $\lambda(n) = 514\text{nm}$                       d)  $r = 0\text{ rad}$ ;  $\lambda(n) = 787\text{nm}$   
e) none of the above
- 20E.** Monochromatic light ( $\lambda = 500\text{ nm}$ ) is incident on a soap bubble ( $n = 1.40$ ). How thick is the bubble (in nm) if destructive interference occurs in the reflected light?  
a. 102                      b. 179                      c. 54                      d. 1                      e. 89
- 21M** Two parallel glass plates of index of refraction  $n$  are separated by oil film of thickness  $d$  and refractive index  $n = n_{\text{glass}}$ . Light has wavelength  $\lambda$  in the air, it is normally incident on the plates. What is the condition for the intensity increase in the reflection at some integer  $m$ .  
a)  $2d = m\lambda$                       b)  $2d = mn\lambda$                       c)  $2dn = m\lambda$                       d)  $2d = (m + \frac{1}{2})\lambda$                       e)  $2dn = (m + \frac{1}{2})\lambda$
- 22M** Light of a wavelength 548nm illuminates two slits separated by 0.25 mm. At what angle would one find the phase difference between the waves from two slits to be 2 radians?  
a) 0.04°                      b) 0.04 rad                      c) 0.02 rad                      d) 0.02°                      e) none of these results

ELEMENTARY PARTICLES AND ASTROPHYSICS

- 23E Which of the groups of particles below are truly elementary according to Standard Model:
- a) leptons, quarks, mesons
  - b) quarks, protons and gauge bosons
  - c) leptons quarks and gauge bosons
  - d) leptons hadrons and bosons
  - e) all of the particles listed in above choices are truly elementary according to Standard Model
- 24E Main Sequence Star
- a) is a star that no longer produces radiation
  - b) is star that produces radiation predominantly via H->He synthesis
  - c) is a star that produces radiation via cooling and shrinking
  - d) is a type of neutron star
  - e) none of the above
- 25E Relic radiation
- A) is almost perfectly non-isotropic and its temperature is close to 3K
  - B) is almost perfectly isotropic and its temperature depends strongly on the direction of observation
  - c) is almost perfectly isotropic and its temperature is close to 3K
  - d) has not yet been confirmed experimentally
  - e) is a radiation emitted by large black holes
- 26M Which of the pairs of particles below consists of two different Majorana particles /Majorana particle is its own antiparticle. This is dual question – I am asking whether both particles in the pair are Majorana particles – and not if one of them is the another's antiparticle.
- a) electron and proton
  - b) photon and Z boson
  - c) W+ boson and W- boson
  - d) up quark and muonic neutrino
  - e) none of the above pairs are two different Majorana particles

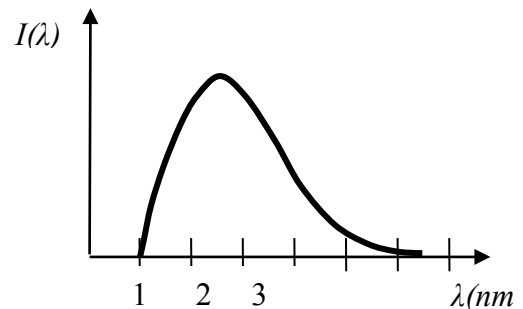
QUANTUM PHYSICS

27E The cutoff wavelength for photoelectric emission of a particular substance is 500 nm. What is the work function in eV?  
a) 4.2                      b)  $4.0 \times 10^{-19}$       c)  $4.0 \times 10^{-10}$       d)  $2.5 \times 10^{-19}$       e) 2.5

28E In Compton scattering from stationary electrons the largest change in wavelength occurs when the photon is scattered through: the angle of  
A) 0deg                      b) 45deg                      c) 90deg                      d) 180deg                      e) 270deg

29M. The X ray intensity distribution function for X ray lamp is given on the figure. Based on this profile one could say that the X-ray lamp was operating under the following potential difference:

- a) 2960V
- b) 980V
- c) 1240V
- d) not enough information to answer
- e) none of the above



30D. A metal of work function 5eV is illuminated with the light emitted by a black body. The cut off frequency of the metal corresponds to the frequency at which certain blackbody emission has maximum. Find the temperature of the black body.  
a) 10.4K                      b) 104K                      c) 1166K                      d) 11 660K                      e) none of the above

31D. The electron on the first Bohr's orbit has de Broglie's wavelength of  
a) 0.66nm                      b) 0.33nm                      c).053nm                      d) 0.021nm                      e)none of the above

NUCLEAR PHYSICS:

32(E) Liquid drop model  
a) predicts correctly the magic numbers  
b) predicts correctly the values of magnetic moments of proton and neutron  
c) explains correctly the mechanism for the light nuclei fusion  
d) explains correctly what happens when heavy nucleus is bombarded by thermal neutrons  
e) is an old model no longer useful – it has been replaced by the shell model

33 (M) 44 g of petrified wood was found in a petrified forest. A sample showed a  $^{14}\text{C}$  activity of 100 decays/minute. How long has the tree been dead (in years)? (The half-life of carbon-14 is 5730 years and freshly cut wood contains  $6.5 \times 10^{10}$  atoms of  $^{14}\text{C}$  per gram.)  
a) 12 300  
b) 15 600  
c) 8 500  
d) 4 700  
e) 2 400

Rotational motion About a Fixed Axis

---

Angular speed  $\omega = d\theta/dt$

Angular acceleration  $\alpha = d\omega/dt$

Net torque  $\sum \tau = I\alpha$

$$\text{If } \alpha = \text{const.} \left\{ \begin{array}{l} \omega_f = \omega_i + \alpha t \\ \theta_f = \theta_i + \omega_i t + \frac{1}{2} \alpha t^2 \\ \omega_f^2 = \omega_i^2 + 2\alpha(\theta_f - \theta_i) \end{array} \right.$$

Work  $W = \int_{\theta_i}^{\theta_f} \tau \, d\theta$

Rotational kinetic energy  $K_R = \frac{1}{2} I\omega^2$

Power  $P = \tau \omega$

Angular momentum  $L = I\omega$

Net torque  $\sum \tau = dL/dt$

Circular Hoop

$$I_{CM} = MR^2$$

Hollow cylinder

$$I_{CM} = \frac{1}{2} M(R_1^2 + R_2^2)$$

where  $R_1$ : inner radius,  $R_2$ : outer radius

Solid cylinder or disc

$$I_{CM} = \frac{1}{2} MR^2$$

Thin Rectangle

$$I_{CM} = \frac{1}{12} M(a^2 + b^2)$$

Long thin rod with rotational axis through center

$$I_{CM} = \frac{1}{12} ML^2$$

Long thin rod with rotational axis through edge

$$I_{CM} = \frac{1}{3} ML^2$$

Solid sphere

$$I_{CM} = \frac{2}{5} MR^2$$

Thin spherical shell

$$I_{CM} = \frac{2}{3} MR^2$$

Mechanics

---

$$v_x = \frac{dx}{dt} \quad \vec{v} = \frac{d\vec{r}}{dt}$$

$$a_x = \frac{dv_x}{dt} \quad \vec{a} = \frac{d\vec{v}}{dt}$$

$$\vec{r}_f = \vec{r}_o + \vec{v}_o t + \frac{1}{2} \vec{a} t^2$$

---

$$a_t = \frac{dv}{dt}$$

$$a_c = \frac{v^2}{r}$$

$$\vec{F} = m \vec{a}$$

$$\vec{F}_o = -b \vec{v}$$

$$f = \mu N$$

$$R = \frac{1}{2} D \rho A v^2$$

$$F_B = \rho_l V \cdot g$$

$$\vec{F} = -k \vec{x}$$

---

$$W = \int \vec{F} \cdot d\vec{s}$$

$$k = \frac{mv^2}{2}$$

$$U_g = mgh$$

$$U_e = \frac{1}{2} kx^2$$

$$\vec{P} = m \vec{v}$$

$$\vec{F} = \frac{d\vec{p}}{dt}$$

$$\vec{r}_{CM} = \frac{\sum m_i \vec{r}_i}{M}$$

$$r_{CM} = \frac{\int r dm}{M}$$

---

$$V = \frac{4}{3} \pi r^3$$

$$A = 4\pi r^2$$

$$A = \pi r^2$$

$$C = 2\pi r$$

SUMMARY OF ELECTRICITY

Coulomb's Law:  $\vec{F} = \frac{k_e q_1 q_2}{r^2} \hat{r}$

$\vec{F} = \iint \frac{k_e dq_1 dq_2}{r^2} \hat{r}$

Electric Field  $\vec{E} = \frac{k_e q}{r^2} \hat{r}$

$\vec{E} = \int \frac{k_e dq}{r^2} \hat{r}$        $\vec{F} = q\vec{E}$

Flux

$\Phi = \int \vec{E} \cdot d\vec{A}$

Gauss Law

$\Phi_{tot} = \oint \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0}$

Electric Potential Energy U

$U = -q \int \vec{E} \cdot d\vec{r} = -qV$

Electric Potential V:

$V = -\int \vec{E} \cdot d\vec{r}$

$\vec{E} = -grad V$        $\vec{E} = E_x \hat{i} + E_y \hat{j} + E_z \hat{k}$        $E_x = -\frac{\partial V}{\partial x}; E_y = -\frac{\partial V}{\partial y}; E_z = -\frac{\partial V}{\partial z}$

Capacitance C

$C = \frac{q}{V}$        $C_{par} = \sum C_i$        $\frac{1}{C_{ser}} = \sum \frac{1}{C_i}$

Various Capacitor's Capacitances

Spherical:  $C = 4\pi\epsilon_0 \frac{ab}{b-a}$       Cylindrical:  $C = 2\pi\epsilon_0 \frac{l}{\ln(b/a)}$       Parallel plate:  $C = \frac{\epsilon_0 A}{d}$

Isolated sphere:  $C = 4\pi\epsilon_0 R$       Capacitor with dielectric:  $C_{diel} = \epsilon C_{air}$

Current:  $I = \frac{dQ}{dt}$       Resistance:  $R = \rho \frac{L}{A}$       Ohm's Law:  $V = RI$

$R_{ser} = \sum R_i$        $\frac{1}{R_{par}} = \sum \frac{1}{R_i}$

Power dissipated on resistor  $P = VI = RI^2 = \frac{V^2}{R}$

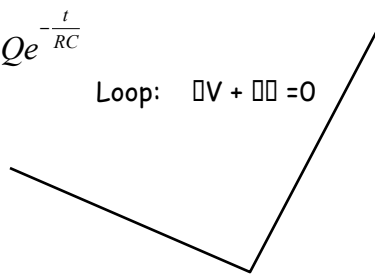
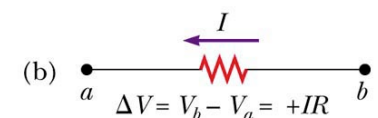
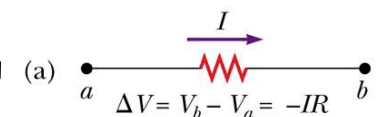
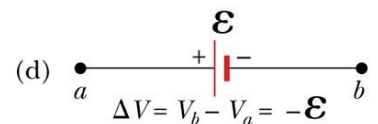
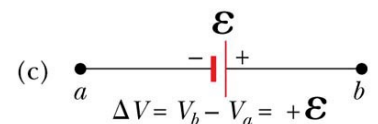
RC circuits: charging the capacitor:  $Q(t) = Q(1 - e^{-\frac{t}{RC}})$

RC circuits: discharging the capacitor:  $Q(t) = Qe^{-\frac{t}{RC}}$

Kirchhoff's Rules      Junction:  $\sum I_{in} = \sum I_{out}$

Loop:  $\sum V + \sum \epsilon = 0$

Suggested sign convention for circuit analysis:



SUMMARY OF E-FIELD AND V FOR MOST IMPORTANT CHARGE DISTRIBUTIONS

Charge distribution	Distance	E field	V potential
Point charge	$r$	$k_e \frac{q}{r^2} \hat{r}$	$k_e \frac{q}{r}$
Many point charges	$r_i$ $1 < i < N$	$\sum k_e \frac{q}{r_i^2} \hat{r}_i$	$\sum k_e \frac{q}{r_i}$
Insulating Charged Sphere	$r \geq R$	$k_e \frac{q}{r^2}$	$k_e \frac{q}{r}$
	$r < R$	$k_e \frac{q}{R^3} r$	$\frac{k_e q}{2R} (3 - \frac{r^2}{R^2}); V(r_0) = V(R)$
Conducting Charged Sphere	$r \geq R$	$k_e \frac{q}{r^2}$	$k_e \frac{q}{r}$
	$r < R$	0	$k_e \frac{q}{R}$
Charged Infinite thin line of charge	$r$	$2k_e \frac{\lambda}{r}$	$2\lambda k_e \ln \frac{r_0}{r}; V(r_0) = 0$
Infinite Charged insulating Cylinder	$r \geq R$	$2k_e \frac{\lambda}{r}$	$2\lambda k_e \ln \frac{R}{r}; V(R) = 0$
	$r < R$	$2\pi k_e \rho r = \frac{2k_e \lambda}{R^2} r$	$\pi k_e \rho (R^2 - r^2) = k_e \frac{\lambda}{R^2} (R^2 - r^2); V(R) = 0$
Infinite Charged Conducting Cylinder	$r \geq R$	$2k_e \frac{\lambda}{r}$	$2\lambda k_e \ln \frac{R}{r}; V(R) = 0$
	$r < R$	0	0
Infinite plane	$y$	$\frac{\sigma}{2\epsilon_0} = 2\sigma\pi k_e$	$Ey$

### Finite continuous charge distributions:

Charge Distribution	Distance	E field	V potential
Finite Charged rod	$y$	$2k_e\lambda\left(\frac{1}{y\sqrt{l^2+y^2}}\right)$	$2k_e\lambda\ln\left(\frac{\sqrt{l^2+y^2}+l}{y}\right)$
	$x$	$\frac{k_e q}{x(l+x)}$	$k_e\lambda\ln\left(\frac{x+l}{x}\right)$
Charged Ring	$y$	$\frac{k_e q y}{(\sqrt{R^2+y^2})^3}$	$k_e \frac{q}{\sqrt{R^2+y^2}}$
Charged Disk	$y$	$2\pi k_e \sigma_e \left(1 - \frac{y}{\sqrt{R^2+y^2}}\right)$	$2\pi k_e \sigma_e (\sqrt{R^2+y^2} - y)$

### OPTICS

General Interference:  $\frac{\delta}{\lambda} = \frac{\varphi}{2\pi}$

Double slit:  $\delta = d \sin \theta = m\lambda$  (max)       $\delta = d \sin \theta = (m + \frac{1}{2})\lambda$  (min)

Single slit:  $a \sin \theta = m\lambda$  (min)      Rayleigh criterion:  $\theta_c = \frac{1.22\lambda}{a}$

$$I = I_{\max} \cos^2\left(\frac{\pi d \sin \theta}{\lambda}\right) \approx I_{\max} \cos^2\left(\frac{\pi d}{\lambda L} y\right) \quad I = I_{\max} \cos^2\left(\frac{\pi d \sin \theta}{\lambda}\right) \left[\frac{\sin(\pi a \sin \theta / \lambda)}{\pi a \sin \theta / \lambda}\right]^2$$

$$R = \frac{\lambda}{\lambda_2 - \lambda_1} = \frac{\lambda}{\Delta\lambda} \quad R = Nm$$

Polarization:  $I = I_{\max} \cos^2 \theta$        $\tan \theta_B = \frac{n_2}{n_1}$

$n_1 \sin \theta_1 = n_2 \sin \theta_2$        $v(n) = \frac{c}{n}$        $v = f\lambda$

$\frac{1}{f} = \frac{1}{p} + \frac{1}{q}$        $\frac{1}{f} = \left(\frac{n_2 - n_1}{n_1}\right) \left(\frac{1}{R_1} - \frac{1}{R_2}\right)$

SIGN CONVENTIONS

**Table 36.2**

Sign Conventions for Refracting Surfaces		
Quantity	Positive When	Negative When
Object location ( $p$ )	Object is in front of surface (real object)	Object is in back of surface (virtual object)
Image location ( $q$ )	Image is in back of surface (real image)	Image is in front of surface (virtual image)
Image height ( $h'$ )	Image is upright	Image is inverted
Radius ( $R$ )	Center of curvature is in back of surface	Center of curvature is in front of surface

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**Table 36.3**

Sign Conventions for Thin Lenses		
Quantity	Positive When	Negative When
Object location ( $p$ )	Object is in front of lens (real object)	Object is in back of lens (virtual object)
Image location ( $q$ )	Image is in back of lens (real image)	Image is in front of lens (virtual image)
Image height ( $h'$ )	Image is upright	Image is inverted
$R_1$ and $R_2$	Center of curvature is in back of lens	Center of curvature is in front of lens
Focal length ( $f$ )	Converging lens	Diverging lens

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**Table 36.1**

Sign Conventions for Mirrors		
Quantity	Positive When	Negative When
Object location ( $p$ )	Object is in front of mirror (real object)	Object is in back of mirror (virtual object)
Image location ( $q$ )	Image is in front of mirror (real image)	Image is in back of mirror (virtual image)
Image height ( $h'$ )	Image is upright	Image is inverted
Focal length ( $f$ ) and radius ( $R$ )	Mirror is concave	Mirror is convex
Magnification ( $M$ )	Image is upright	Image is inverted

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MODERN PHYSICS AND NUCLEAR PHYSICS

$$\lambda_{\max} T = 2.898 \times 10^{-3} \text{ m}\cdot\text{K} \quad P = \sigma A e T^4 \quad \sigma = 5.67 \times 10^{-8} \frac{\text{W}}{\text{m}^2 \cdot \text{K}^4}$$

$$E = hf \quad K_{\max} = hf - \Phi_o \quad \lambda = \frac{h}{p}$$

$$\Delta\lambda = \lambda' - \lambda_0 = \frac{h}{m_e c} (1 - \cos\theta)$$

Kinetic energy of charge  $q$  accelerated in the potential difference  $U$ :  $K = qU$

Kinetic energy of particles moving with speed  $v < 0.1c$ :  $K = \frac{1}{2} mv^2$

Kinetic energy of particles moving with speed  $v > 0.1c$ :  $K = E - m_o c^2 = (\gamma - 1)m_o c^2$

$$\gamma = \frac{1}{\sqrt{1 - v^2/c^2}} \quad \text{and} \quad E^2 = (pc)^2 + (m_o c^2)^2$$

$$N = N(0)e^{-\lambda t}$$

$$R({}_Z^A X) = 1.2 \text{ fm} \cdot \sqrt[3]{A}$$

OSCILLATIONS AND WAVE MECHANICS

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Angular frequencies of various oscillating systems

$$\omega^2 = \frac{k}{m} \quad \text{mass } m \text{ on the spring } k$$

$$\omega^2 = \frac{g}{L} \quad \text{simple pendulum}$$

$$\omega^2 = \frac{mgd}{I} \quad \text{physical pendulum}$$

$$\omega^2 = \frac{K}{I} \quad \text{torsional pendulum}$$

$$v_{\text{sound}} = 340 \text{ m/s} \quad v = \sqrt{\frac{F}{\mu}} \quad v = \sqrt{\frac{S}{\rho}} \quad v = \sqrt{\frac{B + \frac{S}{3}}{\rho}}$$

$$P = \frac{1}{2} \mu \omega^2 A^2 v$$

$$f' = \left[ \frac{v \pm v_o}{v \pm v_s} \right] f$$

$$\beta = 10 \log \left[ \frac{I}{I_o} \right]$$

$$I_o = 10^{-12} \text{ W/m}^2 \quad I = \left[ \frac{P}{A} \right]$$

$$v = f\lambda$$

$$\frac{\partial^2 y}{\partial x^2} = \frac{1}{v^2} \frac{\partial^2 y}{\partial t^2}$$

### Mathematical Constants

Symbol	Value
$\pi$	3.14159...
$e$	2.71828...

### Physical Constants

#### Useful Data

$M_e$	Mass of the earth	$5.98 \times 10^{24}$ kg	
$R_e$	Radius of the earth	$6.37 \times 10^6$ m	
$g$	Free-fall acceleration on earth	$9.80$ m/s <sup>2</sup>	
$G$	Gravitational constant	$6.67 \times 10^{-11}$ N m <sup>2</sup> /kg <sup>2</sup>	
$k_B$	Boltzmann's constant	$1.38 \times 10^{-23}$ J/K	
$R$	Gas constant	$8.31$ J/mol K	
$N_A$	Avogadro's number	$6.02 \times 10^{23}$ particles/mol	
$T_0$	Absolute zero	$-273^\circ\text{C}$	
$\sigma$	Stefan-Boltzmann constant	$5.67 \times 10^{-8}$ W/m <sup>2</sup> K <sup>4</sup>	
$p_{\text{atm}}$	Standard atmosphere	$101,300$ Pa	
$v_{\text{sound}}$	Speed of sound in air at 20°C	$343$ m/s	
$m_p$	Mass of the proton (and the neutron)	$1.67 \times 10^{-27}$ kg	
$m_e$	Mass of the electron	$9.11 \times 10^{-31}$ kg	
$K$	Coulomb's law constant ( $1/4\pi\epsilon_0$ )	$8.99 \times 10^9$ N m <sup>2</sup> /C <sup>2</sup>	
$\epsilon_0$	Permittivity constant	$8.85 \times 10^{-12}$ C <sup>2</sup> /N m <sup>2</sup>	
$\mu_0$	Permeability constant	$1.26 \times 10^{-6}$ T m/A	
$e$	Fundamental unit of charge	$1.60 \times 10^{-19}$ C	
$c$	Speed of light in vacuum	$3.00 \times 10^8$ m/s	
$h$	Planck's constant	$6.63 \times 10^{-34}$ J s	$4.14 \times 10^{-15}$ eV s
$\hbar$	Planck's constant	$1.05 \times 10^{-34}$ J s	$6.58 \times 10^{-16}$ eV s
$a_B$	Bohr radius	$5.29 \times 10^{-11}$ m	

#### Common Prefixes

Prefix	Meaning
femto-	$10^{-15}$
pico-	$10^{-12}$
nano-	$10^{-9}$
micro-	$10^{-6}$
milli-	$10^{-3}$
centi-	$10^{-2}$
kilo-	$10^3$
mega-	$10^6$
giga-	$10^9$
terra-	$10^{12}$

#### Conversion Factors

##### Length

1 in = 2.54 cm
1 mi = 1.609 km
1 m = 39.37 in
1 km = 0.621 mi

##### Velocity

1 mph = 0.447 m/s
1 m/s = 2.24 mph = 3.28 ft/s

##### Mass and energy

1 u = $1.661 \times 10^{-27}$ kg
1 cal = 4.19 J
1 eV = $1.60 \times 10^{-19}$ J

##### Time

1 day = 86,400 s
1 year = $3.16 \times 10^7$ s

##### Pressure

1 atm = 101.3 kPa = 760 mm of Hg
1 atm = 14.7 lb/in <sup>2</sup>

##### Rotation

1 rad = $180^\circ/\pi = 57.3^\circ$
1 rev = $360^\circ = 2\pi$ rad
1 rev/s = 60 rpm