

## Assignment 1

1.

a).  $n = 1000$   $P_1 = 26.2\%$   $P_2 = 39.62\% - 10\% = 29.62\%$

S1:  $H_0: P_1 = P_2$

$H_a: P_1 < P_2$  (Left Tail Test)

S2:  $n_1 = 1000 * 26.2\% = 262$   $n_2 = 1000 * 29.62\% = 296.2$

$$SE(\hat{p}_1 - \hat{p}_2) = \sqrt{\hat{p}_1 \hat{q}_1 / n_1 + \hat{p}_2 \hat{q}_2 / n_2}$$

$$= \sqrt{0.262 * 0.738 / 262 + 0.2962 * 0.7038 / 296.2} = 0.038$$

$$Z_{\text{calc}} = Z_{\text{Test}} = (\hat{p}_1 - \hat{p}_2) / SE(\hat{p}_1 - \hat{p}_2) = (0.262 - 0.2962) / 0.038 = -0.9$$

S3: Level of Significance,  $LS = 0.01$ , so  $CI = 1 - LS = 99\%$ , then

$$Z_{\text{crit}} = Z_{\alpha} = 2.33$$

S4: Reach an appropriate conclusion, since  $\{|Z_{\text{calc}}| = 0.9\} < \{Z_{\text{crit}} = 2.33\} \rightarrow$  Do Not Reject  $H_0$

So, there is insufficient evidence to show that the Conservative vote has dropped by more than 10% from their share of the popular vote in 2011.

b).  $ME = +/- 1\%$   $99\% CI = 2.576$   $\hat{p} = 0.262$   $\hat{q} = 1 - \hat{p} = 0.738$

$$n = (Z^* / ME)^2 \hat{p} \hat{q}$$

$$= 2.576^2 * 0.262 * 0.738 / (0.01)^2 = 12831$$

c).

$$p = 0.3962 \quad n = 17 \quad \hat{p} = 2/17 = 0.1176$$

$$n\hat{p} = 17 * 0.1176 = 1.9992 < 10$$

$$n\hat{q} = 17 * 0.8824 = 15.0008 > 10$$

S1:  $H_0: \hat{p} = p$

$H_a: \hat{p} < p$  (Left Tail Test)

Since  $n\hat{p} < 10$ , the normal Hypothesis Test cannot be used, we should use the Binomial Distribution

$$P\text{-Value} = 1 - P(0) - P(1) - P(2)$$

$$= 1 - [17! / 0!(17-0)! * 0.3692^0 * 0.6038^{17}] - [17! / 1!(17-1)! * 0.3692^1 * 0.6038^{16}] - [17! / 2!(17-2)! * 0.3692^2 * 0.6038^{15}] = 0.9867$$

$$LS = \alpha = 0.01$$

Reach an appropriate conclusion, since  $[P\text{-Value} = 0.9867] > [\alpha = 0.01] \rightarrow$  Do Not Reject  $H_0$

So, this is insufficient evidence to indicate that the level of support for the Conservatives among U of O students is lower than the 39.62% share of the popular vote in 2011.

2.

**Descriptive Statistics: BMI<sub>male</sub>, BMI<sub>female</sub>**

Variable	N	N*	Mean	SE Mean	StDev	Minimum	Q1	Median	Q3
BMI <sub>male</sub>	50	0	26.300	0.531	3.754	21.400	23.750	25.400	28.325
BMI <sub>female</sub>	40	0	24.812	0.855	5.409	17.900	21.300	23.150	27.000

Variable	Maximum
BMI <sub>male</sub>	38.800
BMI <sub>female</sub>	43.100

According to the data;

Female: n=40 SD=5.409

S1.  $H_0: \mu = (\mu_0 = 26)$

$H_a: \mu < (\mu_0 = 26)$  (Left Tail Test)

S2.  $T_{\text{calc}} = (\bar{x} - \mu_0) / SE(\bar{x})$

$SE(\bar{x}) = S / \sqrt{n} = 5.409 / \sqrt{40} = 0.855$

$T_{\text{calc}} = (24.812 - 26) / 0.855 = -1.389$

S3. Level of Significance, LS=0.05, so CI=1-LS=95%, then

$T_{\text{calc}} = T_{\alpha}(n-1) = T_{0.05}(39) = 0.520$

S4. Reach an appropriate conclusion, since  $\{|T_{\text{calc}}| = 1.389\} > \{T_{\text{crit}} = 0.520\} \rightarrow$  Do Not Reject  $H_0$

So, it is insufficient evidence to show that the average female BMI (in the population) is less than 26.

3.

**Descriptive Statistics: BMI<sub>male</sub>, BMI<sub>female</sub>**

Variable	N	N*	Mean	SE Mean	StDev	Minimum	Q1	Median	Q3
BMI <sub>male</sub>	25	25	28.988	0.701	3.507	25.500	26.400	28.300	30.000
BMI <sub>female</sub>	11	28	32.12	1.45	4.81	26.40	28.80	30.80	34.50

Variable	Maximum
BMI <sub>male</sub>	38.800
BMI <sub>female</sub>	43.10

Male:  $\bar{x}_1 = 25$  Female:  $\bar{x}_2 = 11$   $n_1 = 50$   $n_2 = 40$

a).

S1.  $H_0: \hat{p}_1 - \hat{p}_2 = \Delta_0$

$H_A: \hat{p}_1 - \hat{p}_2 \neq \Delta_0$  (Two Tail Test)

S2.  $Z_{\text{calc}} = (\hat{p}_1 - \hat{p}_2) / SE(\hat{p}_1 - \hat{p}_2)$

$p\text{-bar} = (x_1 + x_2) / (n_1 + n_2) = (25 + 11) / (50 + 40) = 0.4$

$q\text{-bar} = 1 - 0.4 = 0.6$

$SE(\hat{p}_1 - \hat{p}_2) = \sqrt{p\text{-bar} * q\text{-bar} * (1/n_1 + 1/n_2)} = \sqrt{0.4 * 0.6 * (1/50 + 1/40)} = 0.1039$

$Z_{\text{calc}} = (25/50 - 11/40) / 0.1039 = 2.1655$

S3. For two tail test, level of Significance,  $LS = 0.05$ , so  $CI = 1 - LS = 95\%$ , then

$Z_{\text{crit}} = 1.960$

S4. Reach an appropriate conclusion, since  $\{Z_{\text{calc}} = 2.165\} > \{Z_{\text{crit}} = 1.960\} \rightarrow \text{Reject } H_0$

So, it is sufficient evidence to show that the proportion of overweight females in the population.

b).  $P\text{-val} = (Z > Z_{\text{calc}} = 2.165) * 2 = (1 - 0.984806) * 2 = 0.0304$

c).  $CI: (25/50 - 11/40) + 1.96(0.1039) = 0.428644$

$(25/50 - 11/40) - 1.96(0.1039) = 0.021356$

$CI: 0.021356 \sim 0.428644$

d). From question b, since  $\{p\text{-Val} = 0.0304\} < \{\alpha = 0.05\} \rightarrow \text{Reject } H_0$

From question c,  $\hat{p}_1 - \hat{p}_2 = 25/50 - 11/40 = 0.225$ , since CI is from 0.021356 to 0.428644, 0.225 is in the range of CI, so it is  $\text{Reject } H_0$ .

Therefore, the results from b and c are all reject  $H_0$ , they are as same as the conclusion in a.

4.

a).

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MTB > desc c1
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**Descriptive Statistics: Liab07**

Variable	N	N*	Mean	SE Mean	StDev	Minimum	Q1	Median	Q3
Liab07	479	0	39.33	7.57	165.73	0.12	2.18	6.17	17.67

Variable	Maximum
Liab07	2074.03

b)

One-Sample T: C2, C3, C4, C5, C6, C7, C8, C9, ...

Variable	N	Mean	StDev	SE Mean	95% CI
C2	50	36.1	80.6	11.4	( 13.2, 59.0)
C3	50	26.52	44.63	6.31	(13.83, 39.20)
C4	50	31.7	101.5	14.4	( 2.8, 60.5)
C5	50	41.7	221.0	31.3	(-21.1, 104.5)
C6	50	16.79	31.46	4.45	( 7.85, 25.73)
C7	50	33.9	132.9	18.8	(-3.9, 71.7)
C8	50	85.9	324.1	45.8	(-6.2, 178.1)
C9	50	48.6	203.3	28.8	(-9.2, 106.4)
C10	50	24.93	69.40	9.81	( 5.21, 44.66)
C11	50	40.8	157.6	22.3	(-4.0, 85.6)
C12	50	58.6	157.4	22.3	( 13.8, 103.3)
C13	50	24.51	49.11	6.94	(10.55, 38.46)
C14	50	26.3	76.6	10.8	( 4.5, 48.0)
C15	50	58.8	231.4	32.7	(-7.0, 124.5)
C16	50	31.18	51.43	7.27	(16.56, 45.79)
C17	50	28.9	133.2	18.8	(-9.0, 66.7)
C18	50	70.6	325.9	46.1	(-22.0, 163.2)
C19	50	33.4	100.7	14.2	( 4.8, 62.0)
C20	50	13.93	27.29	3.86	( 6.17, 21.68)
C21	50	43.5	221.1	31.3	(-19.3, 106.3)

c)

### Data Display

C2							
	27.233	30.179	6.085	0.755	30.170	57.214	4.351
	11.344	1.485	7.863	2.959	0.925	0.174	5.150
	3.710	1.073	7.826	13.257	3.164	527.814	24.215
	29.388	161.521	0.769	18.930	2.182	1.407	2.498
	12.934	31.777	1.978	21.716	0.767	10.717	134.557
	121.219	57.010	54.017	18.604	27.759	4.853	9.574
	17.124	131.244	47.812	0.401	90.482	1.373	10.013
	14.938						

95%CI=1.96

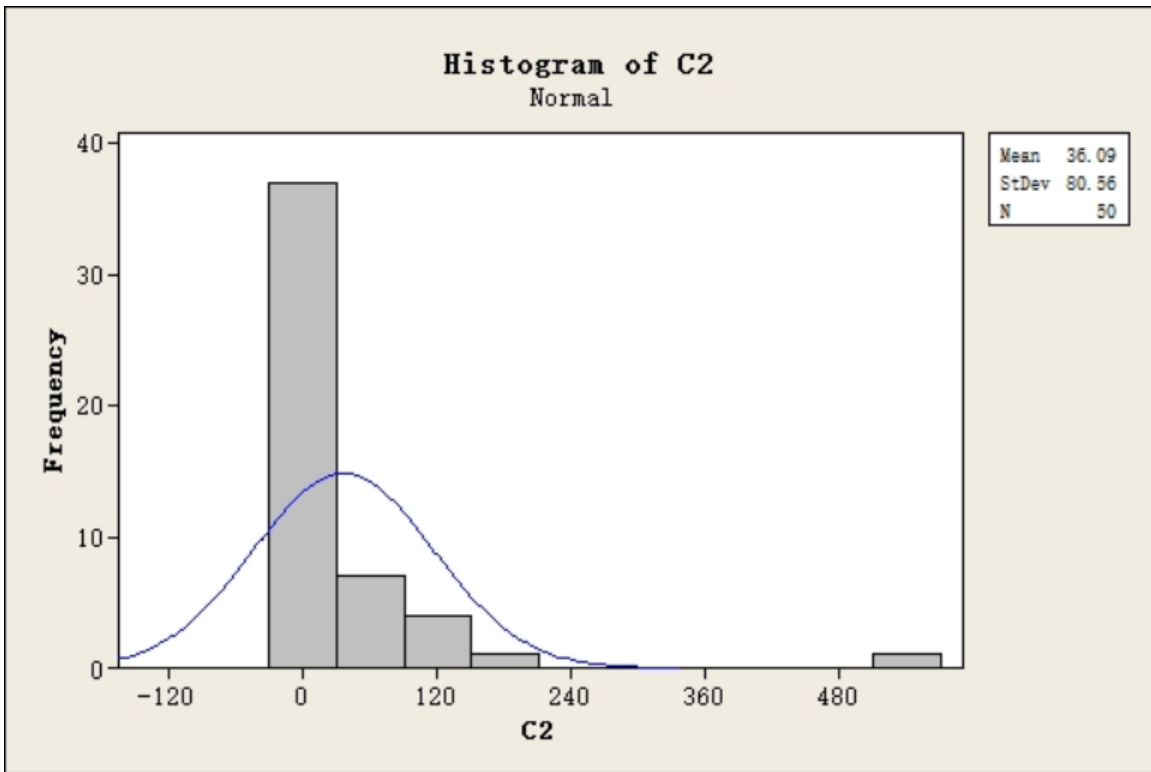
SE( $\bar{x}$ )=S/sqrt(n)=80.6/sqrt(50)=11.399

CI: 36.1+1.96\*11.399=58.442

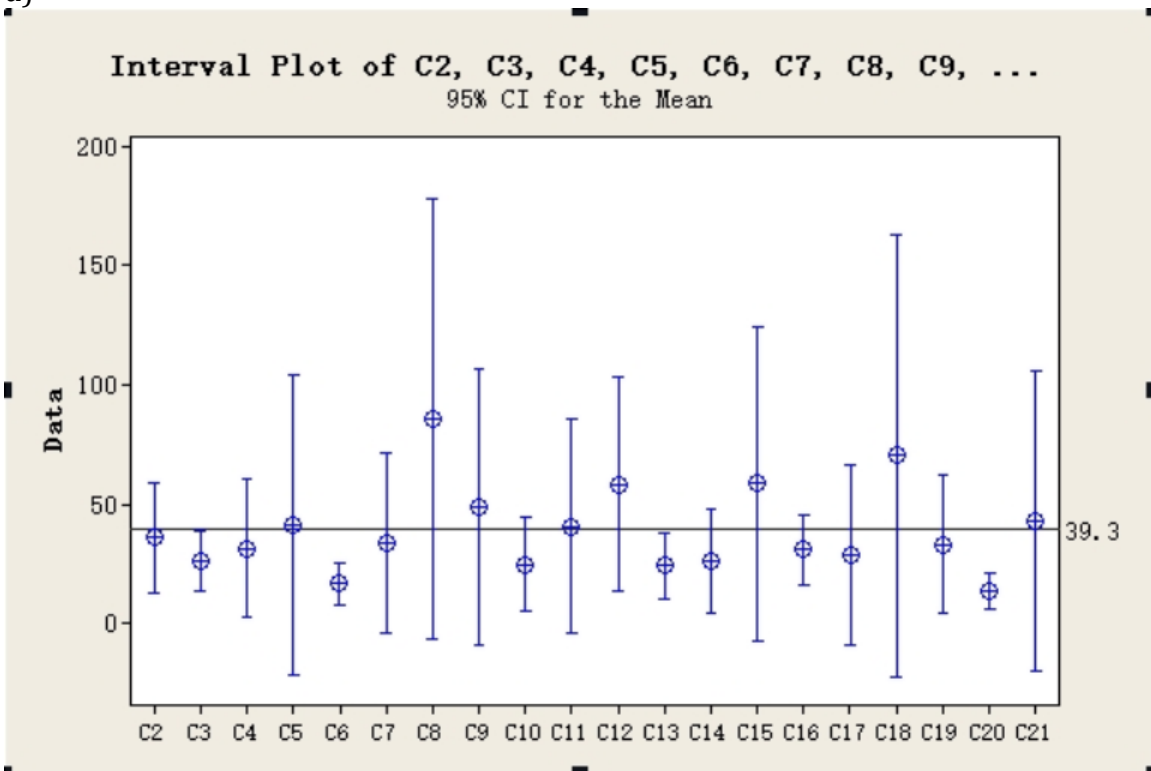
CI: 36.1-1.96\*11.399=13.758

CI:(13.758,58.442)

So, CI95% is (13.758, 58.442)



d)



According to the graph above, C6, C13, C20 do not reach the mean line. Therefore, there are only 17 out of 20 intervals that contain the true value of the population mean from part a.

e). From the question, the samples that we use to calculate are 50 that mean the sample size is 50. It is not large enough to get the accurate results. There are some errors will appear when we count the data. From question d we only get 17, so it is not necessarily equal to the "expected value" to 19.

#### Personal Ethics Statement

##### Individual Assignment:

By signing this Statement, I am attesting to the fact that I have reviewed the entirety of my attached work and that I have applied all the appropriate rules of quotation and referencing in use at the Telfer School of Management at the University of Ottawa, as well as adhered to the fraud policies outlined in the Academic Regulations in the University's Undergraduate Studies Calendar. I further attest that I have knowledge of and have respected the "Beware of Plagiarism" brochure found on the Telfer School of Management web site.

Xi Liu

Signature

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Last Name (print), First Name (print)

January 31, 2014

Date

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