

Surname (last name): _____

Given name (first name): _____

Student number: _____

Lab Section: (circle one) 1 2 3 4 5 6 7 8

Lab Day: (circle one) Tues. Wed. Thurs. Fri.

Lab TA: _____

Course: (circle one) 1301 1311B

Chemistry 1311B/1301

Test 2

November 1, 2006

***Please keep your work covered and keep your eyes on your own paper!
Cheating or any appearance of cheating will result in an F in the course and
possible expulsion from the University.***

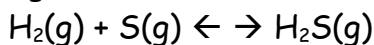
There are 5 questions in this exam. A periodic table and formula sheet are provided at the end. You may rip these two pages off of the exam and use them to cover your work during the exam.

Any scratch work should be on the back of the exam pages and should be handed in with your exam.

Please show all work to receive partial credit.

You have 80 minutes to complete the exam.

1. At 1130 °C, for the reaction given below,



the equilibrium concentrations are:

$$[\text{H}_2\text{S}] = 4.8 \times 10^{-2} \text{ M}; [\text{H}_2] = 1.5 \times 10^{-5} \text{ M}; [\text{S}] = 1.37 \times 10^{-5} \text{ M}$$

Given the molar enthalpies of formation:

$$\text{H}_2\text{S}(\text{g}) \Delta G_f^\circ = -33.0 \text{ kJ mole}^{-1};$$

$$\text{H}_2(\text{g}) \Delta G_f^\circ = 0.0 \text{ kJ mole}^{-1};$$

$$\text{S}(\text{g}) \Delta G_f^\circ = 238.3 \text{ kJ mole}^{-1}$$

$$\text{S}_8(\text{g}) \Delta G_f^\circ = 49.63 \text{ kJ mole}^{-1};$$

$$\text{S}_8(\text{s}) \Delta G_f^\circ = 0.0 \text{ kJ mole}^{-1}$$

a) (3 points) Determine the equilibrium constant (**that you would use to calculate ΔG°**) for the reaction at 1130 °C.

$$K_c = [\text{H}_2\text{S}] / ([\text{S}] [\text{H}_2]) = 4.8 \times 10^{-2} / (1.5 \times 10^{-5} \times 1.37 \times 10^{-5}) = 2.34 \times 10^8$$

$$K_p = K_c / (RT) = 2.34 \times 10^8 / (0.08206 \times (1130 + 273)) = 2.0 \times 10^6$$

b) (3 points) Determine the equilibrium constant for the reaction at 298 K.

$$\Delta G^\circ(\text{at } 298\text{K}) = -33 - (238.3 + 0) = -271.3 \text{ kJ mol}^{-1}$$

$$= -RT \ln K$$

$$\ln K = -(-271.3 \times 10^3) / (8.314 \times 298) = 109.5$$

$$K = 3.6 \times 10^{47}$$

c) (3 points) Determine the enthalpy, ΔH_f° , of the reaction.

$$\ln\left(\frac{k_2}{k_1}\right) = \frac{\Delta H}{R} \left(\frac{1}{T_1} - \frac{1}{T_2}\right)$$

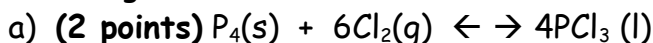
$$\ln\left(\frac{3.6 \times 10^{47}}{2 \times 10^6}\right) = \frac{\Delta H}{8.414} \left(\frac{1}{1403} - \frac{1}{298}\right)$$

$$\Delta H_f^\circ = -299 \text{ kJ mol}^{-1}$$

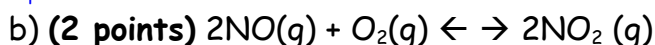
d) (1 point) Is the reaction endothermic or exothermic?

exothermic

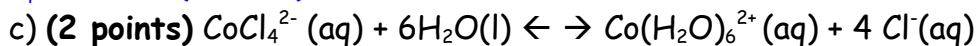
2. Write the equilibrium expression for K you would use to calculate ΔG° for the following reactions:



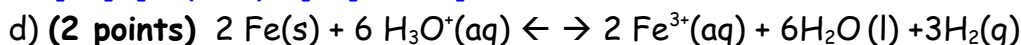
$$K_p = P_{\text{Cl}_2}^{-6}$$



$$K_p = P_{\text{NO}_2}^2 / (P_{\text{NO}}^2 P_{\text{O}_2})$$



$$K_c = [\text{Cl}^-]^4 [\text{Co}(\text{H}_2\text{O})_6^{2+}] / [\text{CoCl}_4^{2-}]$$



$$K_{\text{eq}} = P_{\text{H}_2}^3 [\text{Fe}^{3+}]^2 / [\text{H}_3\text{O}^+]^6$$

3. An 0.10 M solution of acetic acid was found to be 1.3 % ionized.

a) (1 point) Write the chemical equation illustrating acid ionization for acetic acid in water:



b) (4 points) What are the equilibrium concentrations of all species in the above reaction?

$$\% \text{ ionization} = [\text{H}_3\text{O}^+] / [\text{initial acid concentration}]$$

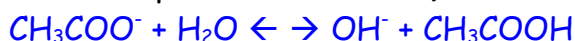
$$[\text{H}_3\text{O}^+] = (1.3/100)0.1 = 0.0013 \text{ M} = [\text{CH}_3\text{COO}^-]$$

$$[\text{CH}_3\text{COOH}] = 0.1 - 0.0013 = 0.0987 \text{ M}$$

c) (3 points) Write the equilibrium expression, K_a for the reaction in part a and determine the acid dissociation (equilibrium constant) K_a for a 0.10 M acetic acid solution.

$$K_a = [\text{CH}_3\text{COO}^-][\text{H}_3\text{O}^+] / [\text{CH}_3\text{COOH}] = 0.0013 \cdot 0.0013 / 0.0987 = 1.7 \times 10^{-5}$$

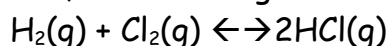
d) (1 point) Write the chemical reaction that corresponds to the ionization of the conjugate base of acetic acid, (acetic acid = CH_3COOH) (ie. the reaction for which K_b is the equilibrium constant)



e) (1 point) What is the base dissociation constant K_b for the acetate anion in aqueous solution?

$$K_b = K_w / K_a = 10^{-14} / 1.7 \times 10^{-5} = 5.9 \times 10^{-10}$$

4. (8 points) A mixture of 0.94 g of H_2 and 3.59 moles of HCl is heated to 2800°C . Calculate the mole fraction of H_2 , Cl_2 and HCl given that $K_p = 193$ at 2800°C for:



$$\text{Moles of H}_2 = 0.94/2 = 0.47 \text{ moles}$$

	H_2	Cl_2	2HCl
I	.47 moles	0 moles	3.59 moles
C	+x	+x	-2x
E	0.47+x	x	3.59 -2x

In terms of pressure

E	$(0.47 + x)P_T/n_T$	$(x)P_T/n_T$	$(3.59 - 2x)P_T/n_T$
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$$\begin{aligned} K_p = 193 &= [(3.59 - 2x)P_T/n_T]^2 / [(0.47 + x)P_T/n_T \cdot (x)P_T/n_T] \\ &= [(3.59 - 2x)]^2 / [(0.47 + x) \cdot (x)] \\ &= (12.88 - 14.36x + 4x^2) / (0.47x + x^2) \end{aligned}$$

$$0 = 189x^2 + 105x - 12.88$$

$x = 0.102$ or -0.661 (this root is not meaningful)

moles $H_2 = .47 + .1 = 0.57$; moles $Cl_2 = 0.1$; moles $HCl = 3.59 - 2(.1) = 3.39$

total moles = $0.57 + 0.1 + 3.39 = 4.06$

$X_{H_2} = 0.140$; $X_{Cl_2} = 0.025$; $X_{HCl} = 0.835$

b) If the partial pressure of Cl_2 , at equilibrium, is 0.102 atm, what is the total pressure of the gas mixture at equilibrium?

$P_{Cl_2} = P_T X_{Cl_2}$; $0.102 \text{ atm} = P_T (0.025)$

$P_T = 4 \text{ atm}$

4. The following equilibrium constants were obtained at 1123K :

$2CO(g) \rightleftharpoons C(s) + CO_2(g)$ $K_p = 7.7 \times 10^{-15}$ rxn 1

$CO(g) + Cl_2(g) \rightleftharpoons COCl_2(g)$ $K_p = 6.0 \times 10^{-3}$ rxn 2

a) (4 points) Calculate K_c at 1123 K for

$C(s) + CO_2(g) + 2Cl_2(g) \rightleftharpoons 2COCl_2(g)$ rxn 3

Rxn 3 = $2 \times \text{rxn 2} + (-\text{rxn 1})$

$K_3 = (K_2)^2 / K_1 = (6 \times 10^{-3})^2 / (7.7 \times 10^{-15}) = 4.7 \times 10^{-9} = K_p$

$K_p = K_c(RT)^{2-3} = K_c/RT$; $K_c = K_p(RT) = 4.7 \times 10^{-9} \times 0.08206 \times 1123 = 4.3 \times 10^{-11}$

b) (1 point) Is this reaction spontaneous under standard conditions at 1123 K ? Explain.

Since K_p is very much larger than 1, the reaction is product favoured, so under standard conditions it will be spontaneous (also if $K > 1$, $\Delta G^\circ < 0$)

c) (3 point) Do you expect ΔH° and ΔS° to be positive or negative? Explain.

ΔS° will be negative because you are going from 3 moles of gas (and one mole of solid) down to 2 moles of gas.

ΔH° must be -ve because ΔG° is negative at 1123 , and $-T\Delta S^\circ$ is positive.

d) (2 points) Under what temperature conditions will the reaction be product favoured? Explain briefly

Under low T conditions. If T gets too large then the positive $(-T\Delta S^\circ)$ will "swamp" the negative ΔH° and ΔG° will become positive.

e) (3 points) You have a non equilibrium mixture at 1123K of 0.2 moles of $COCl_2$, 1×10^{-4} moles of Cl_2 and 1.0×10^{-4} moles of CO_2 (total pressure 1 atm). Determine Q and based on this value predict if the reaction will be spontaneous in the forward direction.

$C(s) + CO_2(g) + 2Cl_2(g) \rightleftharpoons 2COCl_2(g)$

$K = P_{COCl_2}^2 / (P_{Cl_2}^2 * P_{CO_2}) = X_{COCl_2}^2 P_{total} / (X_{Cl_2}^2 * (P_T)^2 * X_{CO_2} * P_T)$

$$= [n_{\text{COCl}_2}^2 / (n_{\text{Cl}_2}^2 * n_{\text{CO}_2})] * (n_{\text{total}}/P_{\text{total}}) \quad (n = \text{number of moles})$$

$$= .2^2(0.2002)/[(1 \times 10^{-4})^3 * 1 \text{ atm}] = 8.0 \times 10^9$$

$$K_p = 4.7 \times 10^9$$

Since $Q > K$, you have too much products, so the reaction is not spontaneous in the forward direction.

f) (4 points) Determine ΔG for the reaction under the conditions described in part e above. Is your answer reasonable?

$$\Delta G = \Delta G^\circ + RT \ln Q = -RT \ln K + RT \ln Q$$

$$= -(8.314 * 1123) \ln 4.7 \times 10^9 + (8.314 * 1123) \ln 8.0 \times 10^9 = 4.98 \text{ kJ}$$

Since $\Delta G > 0$, rxn is not spontaneous and yes it makes sense because in e) above we said it shouldn't be spontaneous.

Bonus: You have 3 M standard solutions of HCl and benzoic acid, $\text{C}_6\text{H}_5\text{COOH}$ collecting dust on a shelf in the laboratory. You are required to make up 100 ml solutions of pH = 2 from each of the HCl and benzoic acid. Given the K_a of benzoic acid = 6.5×10^{-5} , how many more ml of the benzoic acid (than HCl) 3M standard will you use?

To make a pH 2 solution from HCl

$$\text{pH} = 2; [\text{H}_3\text{O}^+] = 10^{-2} \text{ M}$$

To make 100ml of 10^{-2} M from your 3M stock:

$$100 * 10^{-2} = x * 3\text{M}; x = 0.33 \text{ ml (you need 0.33 ml of 3M HCl)}$$

To make a pH 2 solution from benzoic acid:



$$\text{At Equilibrium:} \quad x \quad \quad \quad 10^{-2} \quad 10^{-2}$$

$$K_a = 6.5 \times 10^{-5} = (10^{-2})^2 / x$$

$$x = 1.54 \text{ M}$$

$$\text{So initial concentration of } \text{C}_6\text{H}_5\text{COOH} = 1.54 \text{ M} + 0.01 \text{ M} = 1.55 \text{ M}$$

$$1.55 (100) = 3 (x)$$

$$x = 51.67 \text{ ml (you need 51.67 ml of 3M benzoic acid)}$$

$$\Delta V = 51.67 - 0.33 = 51.33 \text{ ml You need 51.33 ml more benzoic acid than HCl}$$

EQUATIONS SHEET

$$\Delta H^\circ_{\text{rxn}} = \sum n\Delta H^\circ_f (\text{products}) - \sum m\Delta H^\circ_f (\text{reactants})$$

$$\Delta G^\circ_{\text{rxn}} = \sum n\Delta G^\circ_f (\text{products}) - \sum m\Delta G^\circ_f (\text{reactants})$$

$$\Delta S^\circ_{\text{rxn}} = \sum nS^\circ (\text{products}) - \sum mS^\circ (\text{reactants})$$

$$PV = nRT$$

$$\Delta G = \Delta H - T\Delta S$$

$$\Delta G^\circ = -RT\ln K$$

$$v_{\text{rms}} = (3RT/MM)^{1/2}$$

$$\Delta E = q + w$$

$$\Delta G = \Delta G^\circ + RT\ln Q$$

$$\ln\left(\frac{k_2}{k_1}\right) = \frac{\Delta H}{R}\left(\frac{1}{T_1} - \frac{1}{T_2}\right)$$

$$q = ms\Delta T$$

$$q = C\Delta T$$

$$w = -P\Delta V$$

$$[A] = -kt + [A]_0$$

$$t_{1/2} = 0.693/k$$

$$\ln\left(\frac{k_2}{k_1}\right) = \frac{E_a}{R}\left(\frac{1}{T_1} - \frac{1}{T_2}\right)$$

$$1/[A] = kt + 1/[A]_0$$

$$\ln[A] = -kt + \ln[A]_0$$

$$P_A = X_A P_A^\circ$$

$$P_A = X_A P_{\text{Total}}$$

$$P_{\text{total}} = P_1 + P_2 + \dots$$

$$K_P = K_C(RT)^{\Delta n}$$

$$\text{pH} = -\log[\text{H}_3\text{O}^+]$$

$$\text{pOH} = -\log[\text{OH}^-]$$

$$\text{pH} + \text{pOH} = 14$$

$$K_w = K_a \times K_b$$

$$\text{pH} = \text{pK}_a + \log \frac{[\text{conjugate base}]}{[\text{acid}]}$$

Constants:

Avogadro's Number (N_A)

$$6.02 \times 10^{23}$$

Faraday's constant (F)

$$96,500 \text{ C/mol e}^-$$

Universal Gas Constant (R)

$$8.314 \text{ J mol}^{-1} \text{ K}^{-1}$$

$$8.314 \text{ kg m}^2 \text{ mol}^{-1} \text{ K}^{-1} \text{ s}^{-2}$$

$$0.08206 \text{ L atm mol}^{-1} \text{ K}^{-1}$$

Planck's constant (h)

$$6.626 \times 10^{-34} \text{ J s}$$

Rydberg Constant (R_H)

$$2.18 \times 10^{-18} \text{ J}$$

Speed of light (c)

$$3.00 \times 10^8 \text{ m/s}$$

Conversion Factors :

$$1 \text{ A} = 1 \text{ C s}^{-1}$$

$$1 \text{ C} = 1 \text{ J V}^{-1} \text{ mol}^{-1}$$

$$1 \text{ nm} = 10^{-9} \text{ m}$$

$$1 \text{ atm} = 760 \text{ torr}$$

$$= 760 \text{ mmHg}$$

$$= 101.3 \text{ kPa}$$

