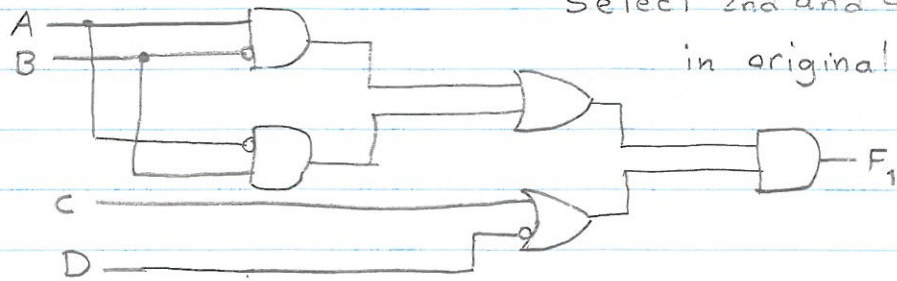
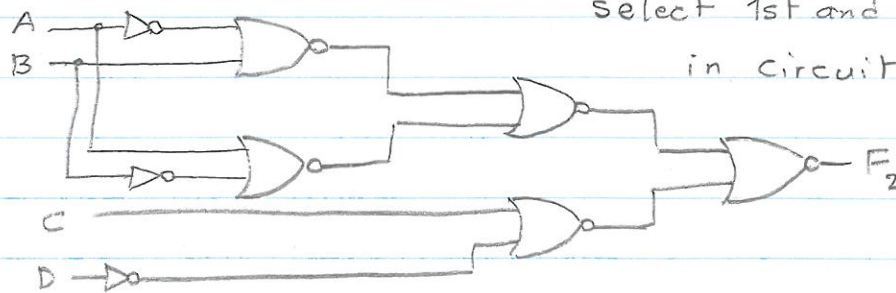


1. AND-OR



Select 2nd and 4th layer
in original circuit

NOR



Select 1st and 3rd layer
in circuit above

check

$$\begin{aligned}
 F_1 &= (A\bar{B} + B\bar{A})(C + \bar{D}) \\
 &= \overline{(\overline{A\bar{B} + B\bar{A}})} + \overline{(C + \bar{D})} \\
 &= \overline{[(\bar{A} + B) + (\bar{B} + A)]} + (C + \bar{D}) = F_2
 \end{aligned}$$

$$\begin{aligned}
 2. (a) (110101.101)_2 &= 2^5 + 2^4 + 2^2 + 2^0 + 2^{-1} + 2^{-3} \\
 &= 32 + 16 + 4 + 2 + \frac{1}{2} + \frac{1}{8} \\
 &= 54.625
 \end{aligned}$$

$$(b) (1101110.1101)_2 = (001101110.110100)_2 = (156.64)_8$$

$$(c) \quad \quad \quad = (01101110.1101)_2 = (6E.D)_{16}$$

$$(d) (785.96)_{10} = (1100010001.111)_2$$

3. (a) $A+B$

$$\begin{array}{r} \textcircled{1} \quad \textcircled{1} \\ 01100101 \\ + 11010110 \\ \hline \textcircled{1}00111011 \end{array}$$

no overflow

(b) $B-A$

$$\begin{array}{r} \textcircled{1}\textcircled{1}\textcircled{1}\textcircled{1} \\ 11010110 \\ = B+(-A) + 10011011 \leftarrow A's\ 2's\ complement\ -A \\ \hline \textcircled{1}01110001 \end{array}$$

↑ sign of result \neq sign of operands
 \therefore overflow (i.e. 8-bit answer isn't valid)

(c) $A \times 101$ since 101 is negative, we take its 2's complement, which is 011.

$= 11010001$

Decimal version

$$\begin{array}{r} 101 \\ \times -3 \\ \hline -303 \end{array}$$

$$\begin{array}{r} 01100101 \\ \times \quad \quad \quad 11 \\ \hline 01100101 \\ 01100101 \\ \hline 10010111 \end{array} \xrightarrow[2's\ comp.]{2's} 11010001$$

Since we know the result of multiplication is negative, we take 2's complement of the product

Note: when multiplying two binary numbers of m and n bits, $m+n$ bits are needed to accommodate the result.

(d) $A + 0111101$ ← 7-bits

$= A + 00111101$ ← sign extended to 8-bits

$= 10100010$ with overflow
 (for 8-bit answer)

$$\begin{array}{r} \textcircled{1}\textcircled{1}\textcircled{1}\textcircled{1}\textcircled{1} \\ 01100101 \\ + 00111101 \\ \hline 10100010 \end{array}$$

overflow ↑

$$4. F = \bar{a}\bar{b} + d\bar{c}b + dc + \bar{a}cd + \bar{a}\bar{b}\bar{c}d$$

$$= \bar{a}\bar{b} + dc + bd$$

check by Algebra

ab \ cd		d			
		00	01	11	10
a	00			1	
	01		1	1	
	11		1	1	
	10	1	1	1	1

$$F = \bar{a}\bar{b} + b\bar{c}d + cd + \bar{a}cd + \bar{a}\bar{b}\bar{c}d$$

$$= \bar{a}\bar{b}(1 + \bar{c}d) + cd(1 + \bar{a}) + b\bar{c}d$$

$$= \bar{a}\bar{b} + cd + b\bar{c}d$$

$$= \bar{a}\bar{b} + d(c + b\bar{c})$$

$$= \bar{a}\bar{b} + d(c + b)(c + \bar{c}) = \bar{a}\bar{b} + cd + bd \quad \checkmark$$

5.

$$F = \bar{c}\bar{d} + \bar{b}\bar{d} + a\bar{d}$$

ab \ cd		d			
		00	01	11	10
a	00	1		d	d
	01		d		1
	11	1			d
	10	d	d	d	1