

CLASS: PHY _____

STUDENT #: _____

NAME: _____

Assignment 5: Potential Energy, Linear Momentum, Impulse

Assigned: Oct16 12:00 Due: October 19 14:00

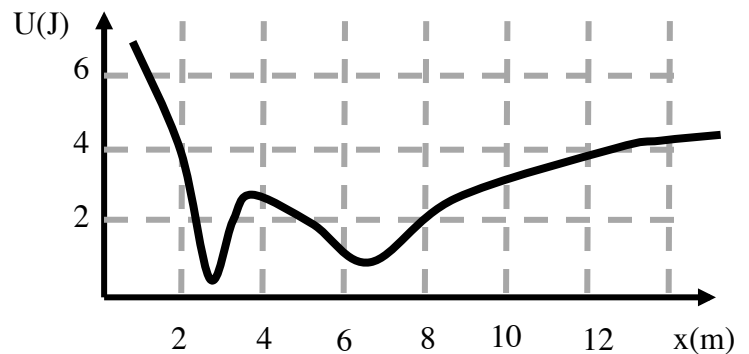
Due to short time given as well as the pain and suffering experienced by students during this week,

a substantial help will be provided on question 3,4 and 5

(These questions will be discussed in class -Thursday and Friday respectively)

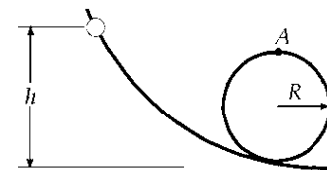
1 At $t=0$ particle is at rest $x=2\text{m}$ After its release it can move under influence of conservative force whose potential energy is shown in the diagram.

- What is the total energy of the particle at $x=8\text{m}$
- What is the position of the right turning point for this particle?
- what is the kinetic energy of the particle at 10m ?



- $E=U+K = E(8\text{m})=\text{const}=E(2\text{m})-4\text{J}$
- $x=12\text{m}$
- $K(10\text{m})=E(10\text{m})-U(10\text{m})=4\text{J}-3\text{J}$

2. A bead slides without friction around a loop-the-loop (Fig. P8.5). The bead is released from a height $h = 3.50R$. (a) What is its speed at point A? (b) How large is the normal force on it if its mass is 5.00 g ?



$$U_i + K_i = U_f + K_f:$$

$$mgh + 0 = mg(2R) + \frac{1}{2}mv^2$$

$$g(3.50R) = 2g(R) + \frac{1}{2}v^2$$

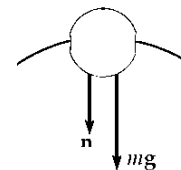
$$v = \sqrt{3.00gR}$$

$$\sum F = m\frac{v^2}{R}: \quad n + mg = m\frac{v^2}{R}$$

$$n = m \left[\frac{v^2}{R} - g \right] = m \left[\frac{3.00gR}{R} - g \right] = 2.00mg$$

$$n = 2.00(5.00 \times 10^{-3} \text{ kg})(9.80 \text{ m/s}^2)$$

$$= \boxed{0.0980 \text{ N downward}}$$



CLASS: PHY _____

STUDENT #: _____

NAME: _____

Assignment 5: cont

3. A tennis player receives a shot with the ball (0.060 0 kg) traveling horizontally at 50.0 m/s and returns the shot with the ball traveling horizontally at 40.0 m/s in the opposite direction. (a) What is the impulse delivered to the ball by the racquet? (b) What work does the racquet do on the ball?

SOLUTION:

Assume the initial direction of the ball in the $-x$ direction.

$$(a) \quad \text{Impulse, } \mathbf{I} = \Delta \mathbf{p} = \mathbf{p}_f - \mathbf{p}_i = (0.060 \text{ 0})(40.0) \hat{\mathbf{i}} - (0.060 \text{ 0})(50.0)(-\hat{\mathbf{i}}) = \boxed{5.40 \hat{\mathbf{i}} \text{ N} \cdot \text{s}}$$

$$(b) \quad \text{Work} = K_f - K_i = \frac{1}{2}(0.060 \text{ 0})[(40.0)^2 - (50.0)^2] = \boxed{-27.0 \text{ J}}$$

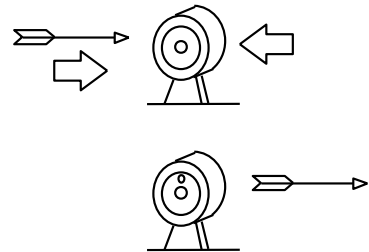
4. An archer shoots an arrow towards a target that is sliding towards her with a speed of 2.50 m/s on a smooth, slippery surface. The 22.5-g arrow is shot with a speed of 35.0 m/s and passes through the 300-g target, which is stopped by the impact. What is the speed of the arrow after passing through the target?

SOLUTION:

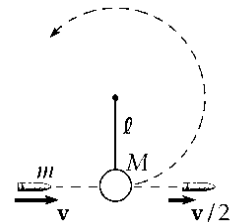
$$(m_1 v_1 + m_2 v_2)_i = (m_1 v_1 + m_2 v_2)_f$$

$$22.5 \text{ g}(35 \text{ m/s}) + 300 \text{ g}(-2.5 \text{ m/s}) = 22.5 \text{ g}v_{1f} + 0$$

$$v_{1f} = \frac{37.5 \text{ g} \cdot \text{m/s}}{22.5 \text{ g}} = \boxed{1.67 \text{ m/s}}$$



5. As shown in Figure P9.24, a bullet of mass m and speed v passes completely through a pendulum bob of mass M . The bullet emerges with a speed of $v/2$. The pendulum bob is suspended by a stiff rod of length ℓ and negligible mass. What is the minimum value of v such that the pendulum bob will barely swing through a complete vertical circle?



Energy is conserved for the bob-Earth system between bottom and top of swing. At the top the stiff rod is in compression and the bob nearly at rest.

$$K_i + U_i = K_f + U_f: \quad \frac{1}{2} M v_b^2 + 0 = 0 + Mg2l$$

$$v_b^2 = g4l \text{ so } v_b = 2\sqrt{gl}$$

Momentum of the bob-bullet system is conserved in the collision:

$$mv = m \frac{v}{2} + M(2\sqrt{gl}) \quad \boxed{v = \frac{4M}{m} \sqrt{gl}}$$