

Short answer:

1. The domain of the function:  $f(x) = \frac{\ln(3x+6)}{x-2}$  is:
2. Solve for  $x$  in  $e^{\frac{1}{2}\ln(x^4)} + \ln(x) + \ln(x+2) - \ln(x^2+2x) = 9$
3. If  $\cos(\theta) = \frac{2}{5}$  and  $\frac{3\pi}{2} \leq \theta \leq 2\pi$ , then  $\tan(\theta) =$
4.  $\arccos\left(\frac{1}{\sqrt{2}}\right) =$
5.  $\lim_{x \rightarrow \infty} \frac{\sqrt{x^2-4}}{2x+1} =$
6.  $\lim_{x \rightarrow 3} \frac{x^3-4x^2+9}{2x-6} =$
7.  $\lim_{x \rightarrow 0} \frac{1-\cos(2x)}{\sin(3x)} =$
8.  $\frac{d}{dx} 3^{x^2+1} =$
9.  $\lim_{x \rightarrow 1^+} (x-1)\ln(x-1) =$
10. The absolute minimum value of  $f(x) = x^3 - 6x + 1$  on  $[-1, 3]$  is
11. The general antiderivative of  $f(x) = 4e^{2x} + \sqrt{x} - \sin(x)$  is
12.  $\frac{d}{dx} \int_0^{x^2} e^t \sin(t) dt =$
13.  $\int_0^{\frac{\pi}{4}} \frac{1}{1+x^2} dx =$
14. The inverse of  $f(x) = (x-1)^3 + 4$  is
15.  $\int 3x - x^3 + e^{4x} + 3\sin(x) =$

Long Answer:

1. A) Determine the values of  $c$  and  $k$  that make the following function continuous. (Justify all reasoning)

$$f(x) = \begin{cases} 3x+k & x < 0 \\ x^2-1 & 0 \leq x \leq 2 \\ \sqrt{cx+3} & x > 2 \end{cases}$$

- B) Find the following limit  $\lim_{x \rightarrow 0} \left(1 + \frac{3}{x}\right)^{2x}$
- C) Find the following limit  $\lim_{x \rightarrow \infty} \sqrt{2x+1} - \sqrt{2x+7}$
2. A) Find the derivatives of the following three functions:

$$f(x) = \ln(x) (\sin(x)), \quad g(x) = \frac{2x+1}{x^2-1}, \quad h(x) = \log_3(2e^{3x^2} + 1)$$

- B) Find the equation of the tangent line of  $e^y - x^2y = 2x$  at  $(1,0)$
- C) Determine the linearization of  $g(x) = \sqrt[3]{x}$  at  $x = 27$  and use this equation to approximate the value of  $\sqrt[3]{26}$
- D) Using logarithmic differentiation, find the derivative of:  $f(x) = \frac{e^{2x}(x^3-1)^3}{x^5(1-3x)^6}$

3. A) Consider a function  $f(x) = 12\sqrt[3]{x^2}e^{\frac{1}{6}x}$  which has the derivative given as:

$$f'(x) = 2x^{-\frac{1}{3}}e^{\frac{1}{6}x}(4+x)$$

- i) Determine the intervals which  $f$  is increasing and decreasing.
- ii) Find all critical points and classify the points as local max, local min or neither.

- B) Consider a function  $g(x) = \frac{(x^2-1)}{2x^2-8}$  that has the following properties:

$$D = (-\infty, -2) \cup (-2, 2) \cup (2, \infty)$$

Intercepts:  $(0, 0.125)$ ,  $(-1, 0)$ , and  $(1, 0)$

Critical points  $x = 0$

$g$  is increasing on  $(-\infty, -2)$  and  $(-2, 0)$ ; decreasing on  $(0, 2)$  and  $(2, \infty)$

$f$  is concave up  $(-\infty, -2)$  and  $(2, \infty)$ ; concave down on  $(-2, 2)$

Vertical asymptotes:  $x=2$  and  $x=-2$ ; horizontal asymptotes:  $y = 0.5$

Provide a sketch of the function.

4. A) Given  $f(x) = x^2 - 1$  and  $g(x) = 2x + 7$ , determine the points of intersection of the two functions.
- B) Determine the contained area between the two curves.
- C) Let  $H(x)$  be the antiderivative of  $f(x)$ , determine the function  $H(x)$  given that the point  $(-3, 1)$  lies on the graph of  $H(x)$ .