



Carleton University

Department of Civil and Environmental Engineering

CIVE 3204 Introduction to Structural Design (Fall 2014)

Solution for Assignment #5 [out of 100]

Question 1: [50 marks]

a) Base shear for the earthquake effect in the N-S direction

base shear $V = [S(T_a)M_v I_E W]/(R_d R_o)$

Earthquake Importance Factor I_E : for normal facility, $I_E = 1.0$

Ductility-related force modification factor R_d : (Table 4.1.8.9)

For concrete structures with moderately ductile moment resisting frame $R_d = 2.5$

Overstrength-related force modification factor R_o : (Table 4.1.8.9)

For concrete structures with moderately ductile moment resisting frame $R_o = 1.4$

Fundamental lateral period T_a :

For Concrete moment frame, $T_a = 0.075 (h_n)^{0.75} = 0.075 (25.2)^{0.75} = 0.844$ s

$h_n = 6 * 4.2 = 25.2$ m

Gravity load W :

$$\begin{aligned} W &= \Sigma W_i + 25\% \text{ snow load on roof} \\ &= 5 * 950 * 9.81 + 600 * 9.81 + 0.25 * 2200 \\ &= 53034 \text{ kN} \end{aligned}$$

Design spectral response acceleration $S(T)$:

For Ottawa (Table C-2):

$$S_a(0.2) = 0.64$$

$$S_a(0.5) = 0.31$$

$$S_a(1.0) = 0.14$$

$$S_a(2.0) = 0.046$$

Site class:

Top 10m: $N_{60} = 20$

From 10 to 40m: $N_{60} = 50$

Average $N_{60} = \frac{30}{\frac{10}{20} + \frac{20}{50}} = 33.3$ $15 \leq \text{Average } N_{60} \leq 50$

→ The building is located in site class D.

Modifying spectral response acceleration, $S_a(T)$ for site class D (Table 4.1.8.4 B and C):

$S_a(0.2) = 0.64$ → $F_a = 1.2 + [(1.1 - 1.2) / (0.75 - 0.50)] * (0.64 - 0.50) = 1.144$

$S_a(1.0) = 0.14$ → $F_v = 1.4 + [(1.3 - 1.4) / (0.20 - 0.10)] * (0.14 - 0.10) = 1.36$

Construct $S(T)$:

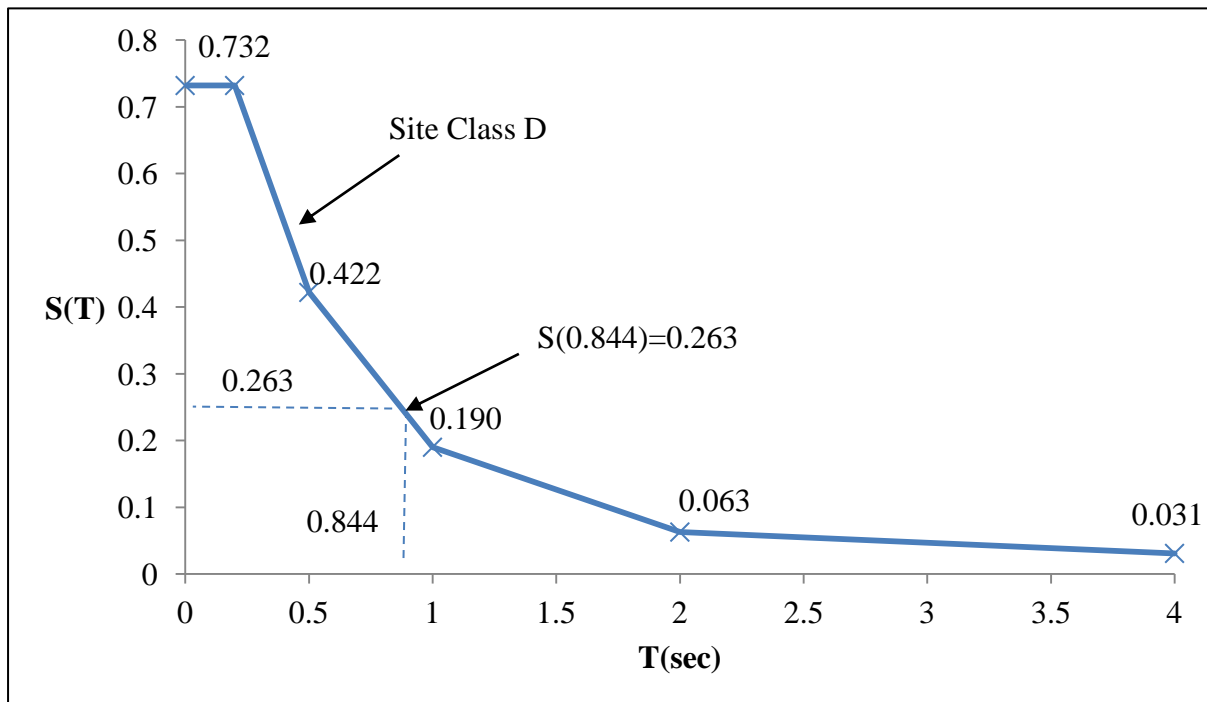
$T \leq 0.2$ s → $S(T) = F_a S_a(0.2) = 1.144 * 0.64 = 0.73216$

$T = 0.5$ s → $S(T) = \min[F_v S_a(0.5), F_a S_a(0.2)] = \min[1.36 * 0.31, 1.144 * 0.64]$
 $= 0.4216$

$T = 1$ s → $S(T) = F_v S_a(1) = 1.36 * 0.14 = 0.1904$

$T = 2$ s → $S(T) = F_v S_a(2) = 1.36 * 0.046 = 0.06256$

$T \geq 4$ s → $S(T) = F_v S_a(2) / 2 = 1.36 * 0.046 / 2 = 0.03128$



$T_a = 0.844$ s → $S(0.844) = 0.4216 + [(0.1904 - 0.4216) / (1 - 0.5)] * (0.844 - 0.5) = 0.263$

Higher mode effect factor M_v : (use Table 4.1.8.11)

$$[S_a(0.2)/S_a(2.0) = 0.64/0.046 = 13.9 \geq 8] \text{ and } [\text{moment-resisting frame}] \rightarrow \\ [T_a = 0.844] \leq 1.0 \rightarrow M_v(T_a) = 1.0$$

Base shear V :

$$V = [S(T_a)M_v I_E W]/(R_d R_o) = (0.263 * 1.0 * 1.0 * 53034)/(2.5 * 1.4) = 3985 \text{ kN} \\ \mathbf{V = 3.99 \text{ MN}}$$

For moment-resisting frame,

$$V_{\min} = [S(2)M_v I_E W]/(R_d R_o) = (0.06256 * 1.0 * 1.0 * 53034)/(2.5 * 1.4) = 948 \text{ kN}$$

For SFRS with $R_d \geq 1.5$,

$$V_{\max} = (2/3)[S(0.2) I_E W]/(R_d R_o) = (2/3) (0.73216 * 1.0 * 53034)/(2.5 * 1.4) = 7.4 \text{ MN}$$

$$[V_{\min} = 948 \text{ kN}] \leq [V = 3.99 \text{ MN}] \leq [V_{\max} = 7.4 \text{ MN}] \rightarrow$$

$$\mathbf{V = 3.99 \text{ MN}}$$

b) Lateral force applied at each storey

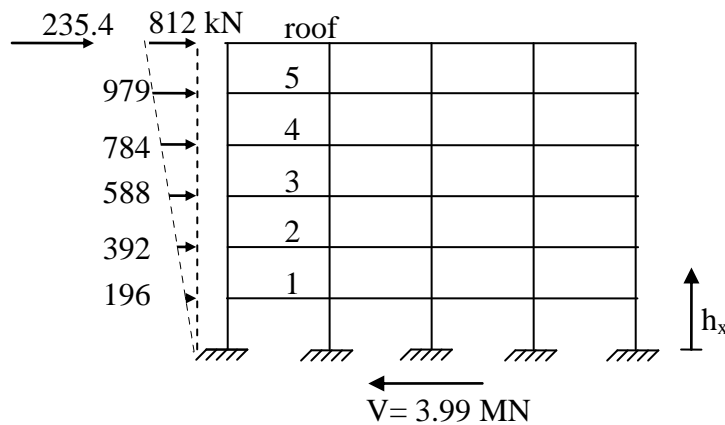
$$T = 0.844 \text{ s} > 0.7 \text{ s} \quad \rightarrow \quad F_t = 0.07 T_a V = 0.07 * 0.844 * 3985 = 235.4 \text{ kN}$$

$$F_t \leq 0.25 V \quad \text{O.K.}$$

$$F_x = (V - F_t) \frac{W_x h_x}{\sum_{i=1}^n W_i h_i} = (3985 - 235.4) * \left[\frac{W_x h_x}{\sum_{i=1}^n W_i h_i} \right] = 3749.6 * \left[\frac{W_x h_x}{\sum_{i=1}^n W_i h_i} \right]$$

$$= 3749.6 * \left[\frac{W_x h_x}{749316} \right] \quad (\text{see table below})$$

Level	h_x	W_x	$W_x h_x$	F_x	F_t	F_x
	(m)	(kN)	(kN.m)	(kN)	(kN)	(kN)
	25.2	6436	162187	811.6	235.4	1047.0
5	21	9320	195710	979.3	0	979.3
4	16.8	9320	156568	783.5	0	783.5
3	12.6	9320	117426	587.6	0	587.6
2	8.4	9320	78283.8	391.7	0	391.7
1	4.2	9320	39141.9	195.9	0	195.9
	$\Sigma =$	53034	749316	3749.6	235.4	3985.0



Lateral Earthquake force distribution along the height

Question 2: [50 marks]

External Pressure: $P = I_w q C_e C_g C_p$

Internal Pressure: $P_i = I_w q C_e C_{gi} C_{pi}$

Reference wind pressure q: In Ottawa, the 1/50 years wind pressure, $q = 0.41 \text{ kPa}$

Importance factor I_w : Assume normal importance structure, $I_w = 1.0$

Exposure factor C_e :

For structures exposed to rough terrain: $C_e = 0.7 \times \left(\frac{h}{12}\right)^{0.3} \geq 0.7$

Where,

h = reference height above grade (m)

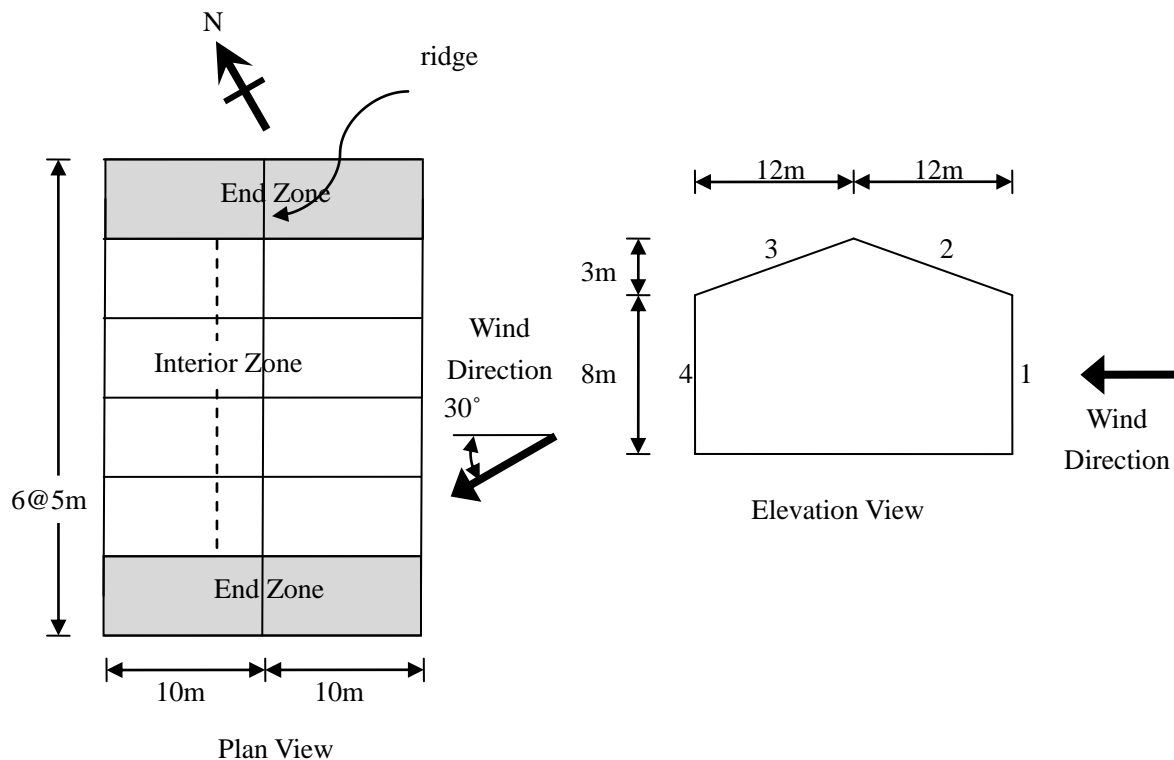
D_s = shorter plan dimension = 24 m

H = mean height of the roof from the ground level = $8 + 3/2 = 9.5 \text{ m}$

Since $H = 9.5 \text{ m} < 20 \text{ m}$, and $H/D_s = 9.5/24 \leq 1.0$, the building should be considered as low-rise.

$h = \max(\text{mean height of the roof, } 6^{\text{m}}) = 9.5 \text{ m}$

$C_e = 0.7 \times \left(\frac{9.5}{12}\right)^{0.3} < 0.7 \rightarrow C_e = 0.7$



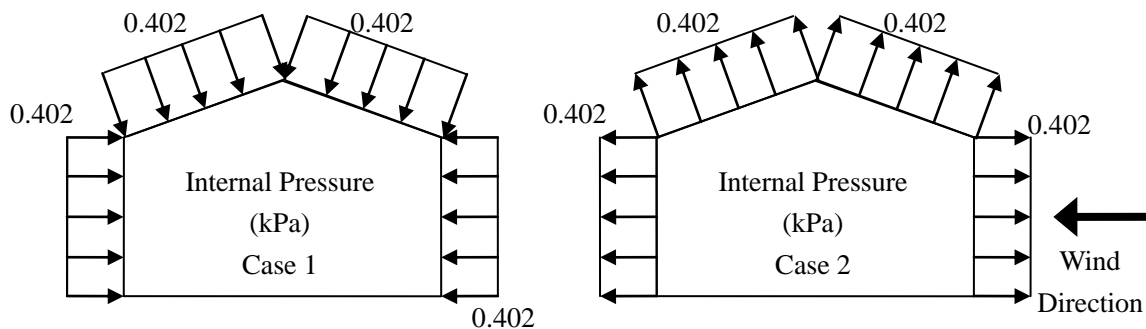
Internal Pressure:

Internal Gust Effect Factor C_{gi} : use default value, $C_{gi} = 2.0$

Internal pressure coefficient C_{pi} : For industrial buildings with shipping doors, it is considered as category 3; $C_{pi} = -0.7$ to 0.7

surface 1: Case 1: $P_i = I_w q C_e C_{gi} C_{pi} = 1 * 0.41 * 0.7 * 2.0 * (0.7) = 0.402 \text{ kPa}$
 Case 2: $P_i = I_w q C_e C_{gi} C_{pi} = 1 * 0.41 * 0.7 * 2.0 * (-0.7) = -0.402 \text{ kPa}$

Following figures show internal pressure on all surfaces.



a) **Net wind pressure profile for the interior zone**

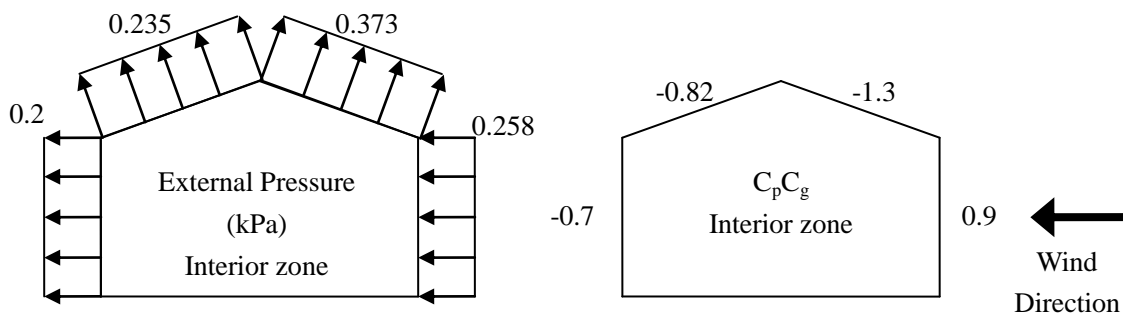
External Pressure:

External peak composite pressure-gust coefficient $C_p C_g$:

Wind blows generally perpendicular to the ridge → use load case A in Figure I-7

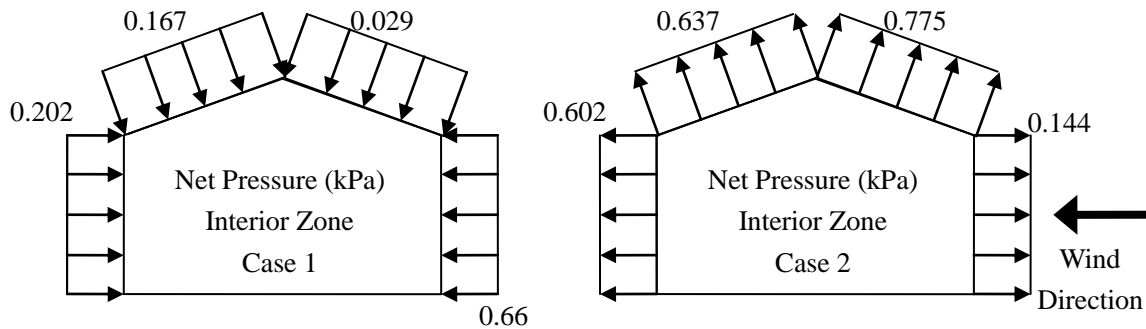
$\alpha = \text{roof slope} = \tan^{-1}(3/12) = 14.0^\circ$
 $\alpha = 5^\circ \rightarrow \text{surface 1: } C_p C_g = 0.75$
 $\alpha = 20^\circ \rightarrow \text{surface 1: } C_p C_g = 1.0$
 $\alpha = 14.0^\circ \rightarrow \text{surface 1: } C_p C_g = 0.75 + [(1 - 0.75) / (20 - 5)](14.0 - 5) = 0.9$
 surface 1: $P = I_w q C_e C_g C_p = 1 * 0.41 * 0.7 * 0.9 = 0.258 \text{ kPa}$

Following figures show $C_p C_g$ values and external pressure on all interior surfaces.



Net Pressure:

To get the net pressure acting on each surface, external and internal pressure should be combined for cases 1 and 2, separately. Following figures show the net pressure profile for the interior zone for cases 1 and 2.



b) Net wind pressure profile for the End zone

External Pressure:

External peak composite pressure-gust coefficient $C_p C_g$:

Wind blows generally perpendicular to the ridge \rightarrow use load case A in Figure I-7

$\alpha = \text{roof slope} = \tan^{-1}(3/12) = 14^\circ$

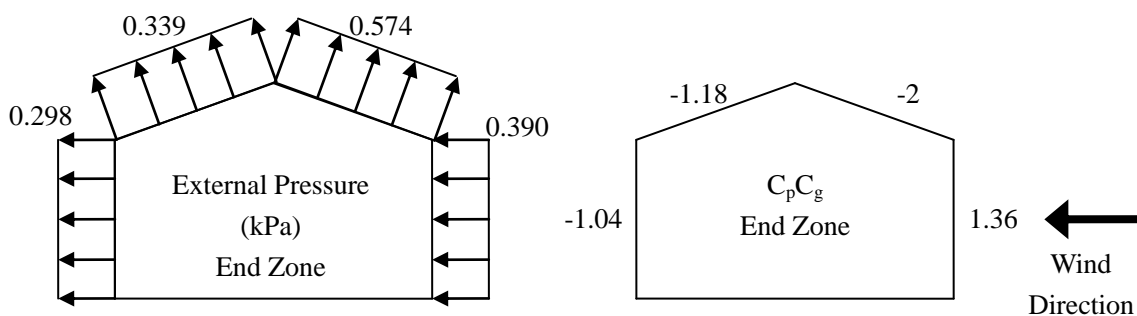
$\alpha = 5^\circ \rightarrow \text{surface 1E: } C_p C_g = 1.15$

$\alpha = 20^\circ \rightarrow \text{surface 1E: } C_p C_g = 1.5$

$\alpha = 16.7^\circ \rightarrow \text{surface 1E: } C_p C_g = 1.15 + [(1.5 - 1.15)/(20 - 5)](14 - 5) = 1.36$

surface 1E: $P = I_w q C_e C_g C_p = 1 * 0.41 * 0.7 * 1.36 = 0.39 \text{ kPa}$

Following figures show $C_p C_g$ values and external pressure on all surfaces at end zones.



Net Pressure:

To get the net pressure acting on each surface, external and internal pressure should be combined for cases 1 and 2, separately. Following figures show the net pressure profile for end zones for cases 1 and 2.

