



**Question (1)-A**

A couple is planning to finance their 5- years –old daughter’s university education. They established a university funds that earns 10%, compounded annually. What annual deposit must be made from the daughter’s 5<sup>th</sup> birthday (now) to her 16<sup>th</sup> birthday to meet the future university expenses shown in the following table .Assume that today is her 5<sup>th</sup> birthday?

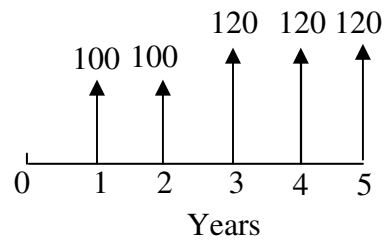
| <b>Birthday</b> | <b>Deposit</b> | <b>Withdrawal</b> |
|-----------------|----------------|-------------------|
| 5-16            | A              |                   |
| 17              |                |                   |
| 18              |                | 25,000            |
| 19              |                | 27,000            |
| 20              |                | 29,000            |
| 21              |                | 31,000            |

**Question (1)-B**

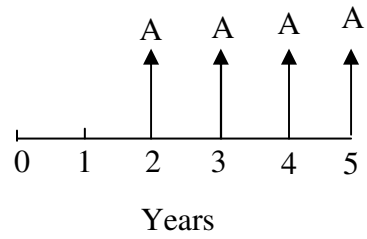
You are about to borrow \$3000 from a bank at interest rate of 12% compounded annually. You are required to make three equal payments in the amount of \$1249.05 per year, with the first repayment occurring at the end of year 1. In each year, show (in a table) the interest payment and principal payment.

**Question (2) -A**

What value of A makes the two annual cash flows equivalent at 10% interest, compounded annually?



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**Question (2)-B**

An investment project costs  $P$ . It is expected to have an annual net cash flow of  $0.125 P$  for 20 years. What is the project's payback period?

**Question (3)-A**

An electric motor is rated at 10 horsepower (HP) and costs \$800. Its full load efficiency is specified to be 85%. A newly designed, high-efficiency motor of the same size has an efficiency of 90%, but costs \$1200. It is estimated that the motors will operate at a rated 10 HP output for 1500 hours a year, and the cost of energy will be \$0.07 per kilowatt-hour. Each motor is expected to have a 15-year life. At the end of 15 years, the first motor will have a salvage value of \$50 and the second motor will have a salvage value of \$100. Consider the MARR to be 8%. (Note: 1HP = 0.7457 kW.)

- (a) Determine which motor should be installed based on the PE criterion.
- (b) In (a), what if the motors operated 2500 hours a year instead of 1500 hours a year? Would the same motor in (a) be the choice?

**Question (3)-B**

You have just received credit card applications from two banks A and B. The interest terms on any unpaid balance are stated as follows:

- (1) bank A: 15% compounded quarterly
- (2) Bank B: 14.8%, compounded daily.

Which of the following statements is incorrect? (Justify your answer)

- (a) The effective annual interest rate for Bank A is 15.865%.
- (b) The nominal interest rate for bank B is 14.8%.
- (c) Bank B's term is better deal because you will pay less interest on your unpaid balance.
- (d) Bank A's term is better deal because you will pay less interest on your unpaid balance.

**Question (4)-A**

You borrowed \$1000 at 8%, compounded annually. The loan was repaid according to the following schedule.

| <b>n</b> | <b>Repayment amount</b> |
|----------|-------------------------|
| <b>1</b> | <b>\$100</b>            |
| <b>2</b> | <b>\$300</b>            |
| <b>3</b> | <b>\$500</b>            |
| <b>4</b> | <b>X</b>                |

Find X, the amount that is required to pay off the loan at the end of year 4.

**Question (4) -B**

The purchase of a car requires a 25,000 loan to be repaid in monthly installments for 4 years at 12% interest, compounded monthly. If the general inflation rate is 6% compounded monthly, find the actual and constant dollar value of the 20<sup>th</sup> payment.

**Question (5)**

The city of Greenville has decided to build a softball complex on land donated by one of the city residents. The city council has already voted to fund the project at a level of \$800,000 (initial capital investment). The city engineer has collected the following financial information for the project.

- Annual upkeep cost: 120,000
- Annual utility cost: 13,000
- Renovation costs: 50,000 every 5 years
- Annual team user fees (revenues): 32,000
- Useful life: Infinite
- Interest rate: 5%

If the city expects 40,000 visitors to the complex each year, what should be the minimum ticket price per person, so that the city can break even? Support your answer with the CFD (Cash Flow Diagram)

### Question (6)

A firm is considering replacing a machine that has been used for making a certain kind of packaging material. The new improved machine will cost \$31,000 installed and will have an estimated economic life of 10 years with salvage value of \$2500. Operating costs are expected to be \$1000 per year throughout its service life. The old machine in use had an original cost of \$25,000 four years ago, and at the time it was purchased, its service life (physical life) was estimated to be 7 years with salvage value of \$5,000. The old machine has a current market value of \$7700. If the firm retains the old machine further, its updated market values and operating costs for the next 4 years will be as follows:

| Year End | Market Value | Operating Cost |
|----------|--------------|----------------|
| 0        | 7700         |                |
| 1        | 4300         | 3200           |
| 2        | 3300         | 3700           |
| 3        | 1100         | 4800           |
| 4        | 0            | 5850           |

The firm's minimum attractive rate of return is 12%

- (a) Working with the updated estimate of market values and operating costs over the next years, determine the remaining economic life of the old machine.
- (b) Determine whether it is economical to make the replacement now.

### Question (7)

A manufacturing company has purchased four assets:

| Item               | Asset Type |            |          |             |
|--------------------|------------|------------|----------|-------------|
|                    | Lathe      | truck      | building | Photocopier |
| Initial cost (\$)  | 45,000     | 25,000     | 800,000  | 40,000      |
| Book life          | 12 yr      | 200,000 km | 50 yr    | 5 yr        |
| CCA class          | 43         | 10         | 1        | 8           |
| Salvage value (\$) | 3,000      | 2,000      | 100,000  | 0           |
| Book depreciation  | DDB        | UP         | SL       | SOYD        |

For book depreciation the units-of –production (UP) method was used for the truck. Usage of the truck was 22,000 kilometers and 25,000 kilometers during the first years, respectively.

- Calculate the book depreciation for each asset in the first 2 years.
- Calculate the capital cost allowance for each asset in the first 2 years.
- If the lathe is to be depreciated over the early portion of its life using DDB and then by switching to SL for the remainder of the asset's life, when should the switch occur?

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| $1/2\%$  |   | Compound Interest Factors               |   |   |   |   |   |   | $1/2\%$  |
|----------|---|---|---|---|---|---|---|---|----------|
| <i>n</i> | Single Payment                          |   | Uniform Payment Series                  |   |   |   | Arithmetic Gradient                     |   | <i>n</i> |
|          | Compound Amount Factor                  | Present Worth Factor                    | Sinking Fund Factor                     | Capital Recovery Factor                 | Compound Amount Factor                  | Present Worth Factor                    | Gradient Uniform Series                 | Gradient Present Worth                  |          |
|          | Find <i>F</i> Given <i>P</i> <i>F/P</i> | Find <i>P</i> Given <i>F</i> <i>P/F</i> | Find <i>A</i> Given <i>F</i> <i>A/F</i> | Find <i>A</i> Given <i>P</i> <i>A/P</i> | Find <i>F</i> Given <i>A</i> <i>F/A</i> | Find <i>P</i> Given <i>A</i> <i>P/A</i> | Find <i>A</i> Given <i>G</i> <i>A/G</i> | Find <i>P</i> Given <i>G</i> <i>P/G</i> |          |
| 1        | 1.005                                   | .9950                                   | 1.0000                                  | 1.0050                                  | 1.000                                   | 0.995                                   | 0                                       | 0                                       | 1        |
| 2        | 1.010                                   | .9901                                   | .4988                                   | .5038                                   | 2.005                                   | 1.985                                   | 0.499                                   | 0.991                                   | 2        |
| 3        | 1.015                                   | .9851                                   | .3317                                   | .3367                                   | 3.015                                   | 2.970                                   | 0.996                                   | 2.959                                   | 3        |
| 4        | 1.020                                   | .9802                                   | .2481                                   | .2531                                   | 4.030                                   | 3.951                                   | 1.494                                   | 5.903                                   | 4        |
| 5        | 1.025                                   | .9754                                   | .1980                                   | .2030                                   | 5.050                                   | 4.926                                   | 1.990                                   | 9.803                                   | 5        |
| 6        | 1.030                                   | .9705                                   | .1646                                   | .1696                                   | 6.076                                   | 5.896                                   | 2.486                                   | 14.660                                  | 6        |
| 7        | 1.036                                   | .9657                                   | .1407                                   | .1457                                   | 7.106                                   | 6.862                                   | 2.980                                   | 20.448                                  | 7        |
| 8        | 1.041                                   | .9609                                   | .1228                                   | .1278                                   | 8.141                                   | 7.823                                   | 3.474                                   | 27.178                                  | 8        |
| 9        | 1.046                                   | .9561                                   | .1089                                   | .1139                                   | 9.182                                   | 8.779                                   | 3.967                                   | 34.825                                  | 9        |
| 10       | 1.051                                   | .9513                                   | .0978                                   | .1028                                   | 10.228                                  | 9.730                                   | 4.459                                   | 43.389                                  | 10       |
| 11       | 1.056                                   | .9466                                   | .0887                                   | .0937                                   | 11.279                                  | 10.677                                  | 4.950                                   | 52.855                                  | 11       |
| 12       | 1.062                                   | .9419                                   | .0811                                   | .0861                                   | 12.336                                  | 11.619                                  | 5.441                                   | 63.218                                  | 12       |
| 13       | 1.067                                   | .9372                                   | .0746                                   | .0796                                   | 13.397                                  | 12.556                                  | 5.931                                   | 74.465                                  | 13       |
| 14       | 1.072                                   | .9326                                   | .0691                                   | .0741                                   | 14.464                                  | 13.489                                  | 6.419                                   | 86.590                                  | 14       |
| 15       | 1.078                                   | .9279                                   | .0644                                   | .0694                                   | 15.537                                  | 14.417                                  | 6.907                                   | 99.574                                  | 15       |
| 16       | 1.083                                   | .9233                                   | .0602                                   | .0652                                   | 16.614                                  | 15.340                                  | 7.394                                   | 113.427                                 | 16       |
| 17       | 1.088                                   | .9187                                   | .0565                                   | .0615                                   | 17.697                                  | 16.259                                  | 7.880                                   | 128.125                                 | 17       |
| 18       | 1.094                                   | .9141                                   | .0532                                   | .0582                                   | 18.786                                  | 17.173                                  | 8.366                                   | 143.668                                 | 18       |
| 19       | 1.099                                   | .9096                                   | .0503                                   | .0553                                   | 19.880                                  | 18.082                                  | 8.850                                   | 160.037                                 | 19       |
| 20       | 1.105                                   | .9051                                   | .0477                                   | .0527                                   | 20.979                                  | 18.987                                  | 9.334                                   | 177.237                                 | 20       |
| 21       | 1.110                                   | .9006                                   | .0453                                   | .0503                                   | 22.084                                  | 19.888                                  | 9.817                                   | 195.245                                 | 21       |
| 22       | 1.116                                   | .8961                                   | .0431                                   | .0481                                   | 23.194                                  | 20.784                                  | 10.300                                  | 214.070                                 | 22       |
| 23       | 1.122                                   | .8916                                   | .0411                                   | .0461                                   | 24.310                                  | 21.676                                  | 10.781                                  | 233.680                                 | 23       |
| 24       | 1.127                                   | .8872                                   | .0393                                   | .0443                                   | 25.432                                  | 22.563                                  | 11.261                                  | 254.088                                 | 24       |
| 25       | 1.133                                   | .8828                                   | .0377                                   | .0427                                   | 26.559                                  | 23.446                                  | 11.741                                  | 275.273                                 | 25       |

| $1\%$    |   | Compound Interest Factors               |   |   |   |   |   |   | $1\%$    |
|----------|---|---|---|---|---|---|---|---|----------|
| <i>n</i> | Single Payment                          |   | Uniform Payment Series                  |   |   |   | Arithmetic Gradient                     |   | <i>n</i> |
|          | Compound Amount Factor                  | Present Worth Factor                    | Sinking Fund Factor                     | Capital Recovery Factor                 | Compound Amount Factor                  | Present Worth Factor                    | Gradient Uniform Series                 | Gradient Present Worth                  |          |
|          | Find <i>F</i> Given <i>P</i> <i>F/P</i> | Find <i>P</i> Given <i>F</i> <i>P/F</i> | Find <i>A</i> Given <i>F</i> <i>A/F</i> | Find <i>A</i> Given <i>P</i> <i>A/P</i> | Find <i>F</i> Given <i>A</i> <i>F/A</i> | Find <i>P</i> Given <i>A</i> <i>P/A</i> | Find <i>A</i> Given <i>G</i> <i>A/G</i> | Find <i>P</i> Given <i>G</i> <i>P/G</i> |          |
| 1        | 1.010                                   | .9901                                   | 1.0000                                  | 1.0100                                  | 1.000                                   | 0.990                                   | 0                                       | 0                                       | 1        |
| 2        | 1.020                                   | .9803                                   | .4975                                   | .5075                                   | 2.010                                   | 1.970                                   | 0.498                                   | 0.980                                   | 2        |
| 3        | 1.030                                   | .9706                                   | .3300                                   | .3400                                   | 3.030                                   | 2.941                                   | 0.993                                   | 2.921                                   | 3        |
| 4        | 1.041                                   | .9610                                   | .2463                                   | .2563                                   | 4.060                                   | 3.902                                   | 1.488                                   | 5.804                                   | 4        |
| 5        | 1.051                                   | .9515                                   | .1960                                   | .2060                                   | 5.101                                   | 4.853                                   | 1.980                                   | 9.610                                   | 5        |
| 6        | 1.062                                   | .9420                                   | .1625                                   | .1725                                   | 6.152                                   | 5.795                                   | 2.471                                   | 14.320                                  | 6        |
| 7        | 1.072                                   | .9327                                   | .1386                                   | .1486                                   | 7.214                                   | 6.728                                   | 2.960                                   | 19.917                                  | 7        |
| 8        | 1.083                                   | .9235                                   | .1207                                   | .1307                                   | 8.286                                   | 7.652                                   | 3.448                                   | 26.381                                  | 8        |
| 9        | 1.094                                   | .9143                                   | .1067                                   | .1167                                   | 9.369                                   | 8.566                                   | 3.934                                   | 33.695                                  | 9        |
| 10       | 1.105                                   | .9053                                   | .0956                                   | .1056                                   | 10.462                                  | 9.471                                   | 4.418                                   | 41.843                                  | 10       |
| 11       | 1.116                                   | .8963                                   | .0865                                   | .0965                                   | 11.567                                  | 10.368                                  | 4.900                                   | 50.806                                  | 11       |
| 12       | 1.127                                   | .8874                                   | .0788                                   | .0888                                   | 12.682                                  | 11.255                                  | 5.381                                   | 60.568                                  | 12       |
| 13       | 1.138                                   | .8787                                   | .0724                                   | .0824                                   | 13.809                                  | 12.134                                  | 5.861                                   | 71.112                                  | 13       |
| 14       | 1.149                                   | .8700                                   | .0669                                   | .0769                                   | 14.947                                  | 13.004                                  | 6.338                                   | 82.422                                  | 14       |
| 15       | 1.161                                   | .8613                                   | .0621                                   | .0721                                   | 16.097                                  | 13.865                                  | 6.814                                   | 94.481                                  | 15       |
| 16       | 1.173                                   | .8528                                   | .0579                                   | .0679                                   | 17.258                                  | 14.718                                  | 7.289                                   | 107.273                                 | 16       |
| 17       | 1.184                                   | .8444                                   | .0543                                   | .0643                                   | 18.430                                  | 15.562                                  | 7.761                                   | 120.783                                 | 17       |
| 18       | 1.196                                   | .8360                                   | .0510                                   | .0610                                   | 19.615                                  | 16.398                                  | 8.232                                   | 134.995                                 | 18       |
| 19       | 1.208                                   | .8277                                   | .0481                                   | .0581                                   | 20.811                                  | 17.226                                  | 8.702                                   | 149.895                                 | 19       |
| 20       | 1.220                                   | .8195                                   | .0454                                   | .0554                                   | 22.019                                  | 18.046                                  | 9.169                                   | 165.465                                 | 20       |
| 21       | 1.232                                   | .8114                                   | .0430                                   | .0530                                   | 23.239                                  | 18.857                                  | 9.635                                   | 181.694                                 | 21       |
| 22       | 1.245                                   | .8034                                   | .0409                                   | .0509                                   | 24.472                                  | 19.660                                  | 10.100                                  | 198.565                                 | 22       |
| 23       | 1.257                                   | .7954                                   | .0389                                   | .0489                                   | 25.716                                  | 20.456                                  | 10.563                                  | 216.065                                 | 23       |
| 24       | 1.270                                   | .7876                                   | .0371                                   | .0471                                   | 26.973                                  | 21.243                                  | 11.024                                  | 234.179                                 | 24       |
| 25       | 1.282                                   | .7798                                   | .0354                                   | .0454                                   | 28.243                                  | 22.023                                  | 11.483                                  | 252.892                                 | 25       |
| 26       | 1.295                                   | .7720                                   | .0339                                   | .0439                                   | 29.526                                  | 22.795                                  | 11.941                                  | 272.195                                 | 26       |
| 27       | 1.308                                   | .7644                                   | .0324                                   | .0424                                   | 30.821                                  | 23.560                                  | 12.397                                  | 292.069                                 | 27       |
| 28       | 1.321                                   | .7568                                   | .0311                                   | .0411                                   | 32.129                                  | 24.316                                  | 12.852                                  | 312.504                                 | 28       |
| 29       | 1.335                                   | .7493                                   | .0299                                   | .0399                                   | 33.450                                  | 25.066                                  | 13.304                                  | 333.486                                 | 29       |
| 30       | 1.348                                   | .7419                                   | .0287                                   | .0387                                   | 34.785                                  | 25.808                                  | 13.756                                  | 355.001                                 | 30       |
| 36       | 1.431                                   | .6989                                   | .0232                                   | .0332                                   | 43.077                                  | 30.107                                  | 16.428                                  | 494.620                                 | 36       |
| 40       | 1.489                                   | .6717                                   | .0205                                   | .0305                                   | 48.886                                  | 32.835                                  | 18.178                                  | 596.854                                 | 40       |
| 48       | 1.612                                   | .6203                                   | .0163                                   | .0263                                   | 61.223                                  | 37.974                                  | 21.598                                  | 820.144                                 | 48       |
| 50       | 1.645                                   | .6080                                   | .0155                                   | .0255                                   | 64.463                                  | 39.196                                  | 22.436                                  | 879.417                                 | 50       |
| 52       | 1.678                                   | .5961                                   | .0148                                   | .0248                                   | 67.769                                  | 40.394                                  | 23.269                                  | 939.916                                 | 52       |

5%

## Compound Interest Factors

5%

| n  | Single Payment         |                      | Uniform Payment Series |                         |                        |                      | Arithmetic Gradient     |                        | n  |
|----|------------------------|----------------------|------------------------|-------------------------|------------------------|----------------------|-------------------------|------------------------|----|
|    | Compound Amount Factor | Present Worth Factor | Sinking Fund Factor    | Capital Recovery Factor | Compound Amount Factor | Present Worth Factor | Gradient Uniform Series | Gradient Present Worth |    |
|    | Find F Given P         | Find P Given F       | Find A Given F         | Find A Given P          | Find F Given A         | Find P Given A       | Find A Given G          | Find P Given G         |    |
|    | F/P                    | P/F                  | A/F                    | A/P                     | F/A                    | P/A                  | A/G                     | P/G                    |    |
| 1  | 1.050                  | .9524                | 1.0000                 | 1.0500                  | 1.000                  | 0.952                | 0                       | 0                      | 1  |
| 2  | 1.102                  | .9070                | .4878                  | .5378                   | 2.050                  | 1.859                | 0.488                   | 0.907                  | 2  |
| 3  | 1.158                  | .8638                | .3172                  | .3672                   | 3.152                  | 2.723                | 0.967                   | 2.635                  | 3  |
| 4  | 1.216                  | .8227                | .2320                  | .2820                   | 4.310                  | 3.546                | 1.439                   | 5.103                  | 4  |
| 5  | 1.276                  | .7835                | .1810                  | .2310                   | 5.526                  | 4.329                | 1.902                   | 8.237                  | 5  |
| 6  | 1.340                  | .7462                | .1470                  | .1970                   | 6.802                  | 5.076                | 2.358                   | 11.968                 | 6  |
| 7  | 1.407                  | .7107                | .1228                  | .1728                   | 8.142                  | 5.786                | 2.805                   | 16.232                 | 7  |
| 8  | 1.477                  | .6768                | .1047                  | .1547                   | 9.549                  | 6.463                | 3.244                   | 20.970                 | 8  |
| 9  | 1.551                  | .6446                | .0907                  | .1407                   | 11.027                 | 7.108                | 3.676                   | 26.127                 | 9  |
| 10 | 1.629                  | .6139                | .0795                  | .1295                   | 12.578                 | 7.722                | 4.099                   | 31.652                 | 10 |
| 11 | 1.710                  | .5847                | .0704                  | .1204                   | 14.207                 | 8.306                | 4.514                   | 37.499                 | 11 |
| 12 | 1.796                  | .5568                | .0628                  | .1128                   | 15.917                 | 8.863                | 4.922                   | 43.624                 | 12 |
| 13 | 1.886                  | .5303                | .0565                  | .1065                   | 17.713                 | 9.394                | 5.321                   | 49.988                 | 13 |
| 14 | 1.980                  | .5051                | .0510                  | .1010                   | 19.599                 | 9.899                | 5.713                   | 56.553                 | 14 |
| 15 | 2.079                  | .4810                | .0463                  | .0963                   | 21.579                 | 10.380               | 6.097                   | 63.288                 | 15 |

6%

## Compound Interest Factors

6%

| n  | Single Payment         |                      | Uniform Payment Series |                         |                        |                      | Arithmetic Gradient     |                        | n  |
|----|------------------------|----------------------|------------------------|-------------------------|------------------------|----------------------|-------------------------|------------------------|----|
|    | Compound Amount Factor | Present Worth Factor | Sinking Fund Factor    | Capital Recovery Factor | Compound Amount Factor | Present Worth Factor | Gradient Uniform Series | Gradient Present Worth |    |
|    | Find F Given P         | Find P Given F       | Find A Given F         | Find A Given P          | Find F Given A         | Find P Given A       | Find A Given G          | Find P Given G         |    |
|    | F/P                    | P/F                  | A/F                    | A/P                     | F/A                    | P/A                  | A/G                     | P/G                    |    |
| 1  | 1.060                  | .9434                | 1.0000                 | 1.0600                  | 1.000                  | 0.943                | 0                       | 0                      | 1  |
| 2  | 1.124                  | .8900                | .4854                  | .5454                   | 2.060                  | 1.833                | 0.485                   | 0.890                  | 2  |
| 3  | 1.191                  | .8396                | .3141                  | .3741                   | 3.184                  | 2.673                | 0.961                   | 2.569                  | 3  |
| 4  | 1.262                  | .7921                | .2286                  | .2886                   | 4.375                  | 3.465                | 1.427                   | 4.945                  | 4  |
| 5  | 1.338                  | .7473                | .1774                  | .2374                   | 5.637                  | 4.212                | 1.884                   | 7.934                  | 5  |
| 6  | 1.419                  | .7050                | .1434                  | .2034                   | 6.975                  | 4.917                | 2.330                   | 11.459                 | 6  |
| 7  | 1.504                  | .6651                | .1191                  | .1791                   | 8.394                  | 5.582                | 2.768                   | 15.450                 | 7  |
| 8  | 1.594                  | .6274                | .1010                  | .1610                   | 9.897                  | 6.210                | 3.195                   | 19.841                 | 8  |
| 9  | 1.689                  | .5919                | .0870                  | .1470                   | 11.491                 | 6.802                | 3.613                   | 24.577                 | 9  |
| 10 | 1.791                  | .5584                | .0759                  | .1359                   | 13.181                 | 7.360                | 4.022                   | 29.602                 | 10 |
| 11 | 1.898                  | .5268                | .0668                  | .1268                   | 14.972                 | 7.887                | 4.421                   | 34.870                 | 11 |
| 12 | 2.012                  | .4970                | .0593                  | .1193                   | 16.870                 | 8.384                | 4.811                   | 40.337                 | 12 |
| 13 | 2.133                  | .4688                | .0530                  | .1130                   | 18.882                 | 8.853                | 5.192                   | 45.963                 | 13 |
| 14 | 2.261                  | .4423                | .0476                  | .1076                   | 21.015                 | 9.295                | 5.564                   | 51.713                 | 14 |
| 15 | 2.397                  | .4173                | .0430                  | .1030                   | 23.276                 | 9.712                | 5.926                   | 57.554                 | 15 |

8%

## Compound Interest Factors

8%

| n  | Single Payment         |                       | Uniform Payment Series |                         |                        |                       | Arithmetic Gradient     |                        | n  |
|----|------------------------|-----------------------|------------------------|-------------------------|------------------------|-----------------------|-------------------------|------------------------|----|
|    | Compound Amount Factor | Present Worth Factor  | Sinking Fund Factor    | Capital Recovery Factor | Compound Amount Factor | Present Worth Factor  | Gradient Uniform Series | Gradient Present Worth |    |
|    | Find F Given P<br>F/P  | Find P Given F<br>P/F | Find A Given F<br>A/F  | Find A Given P<br>A/P   | Find F Given A<br>F/A  | Find P Given A<br>P/A | Find A Given G<br>A/G   | Find P Given G<br>P/G  |    |
| 1  | 1.080                  | .9259                 | 1.0000                 | 1.0800                  | 1.000                  | 0.926                 | 0                       | 0                      | 1  |
| 2  | 1.166                  | .8573                 | .4808                  | .5608                   | 2.080                  | 1.783                 | 0.481                   | 0.857                  | 2  |
| 3  | 1.260                  | .7938                 | .3080                  | .3880                   | 3.246                  | 2.577                 | 0.949                   | 2.445                  | 3  |
| 4  | 1.360                  | .7350                 | .2219                  | .3019                   | 4.506                  | 3.312                 | 1.404                   | 4.650                  | 4  |
| 5  | 1.469                  | .6806                 | .1705                  | .2505                   | 5.867                  | 3.993                 | 1.846                   | 7.372                  | 5  |
| 6  | 1.587                  | .6302                 | .1363                  | .2163                   | 7.336                  | 4.623                 | 2.276                   | 10.523                 | 6  |
| 7  | 1.714                  | .5835                 | .1121                  | .1921                   | 8.923                  | 5.206                 | 2.694                   | 14.024                 | 7  |
| 8  | 1.851                  | .5403                 | .0940                  | .1740                   | 10.637                 | 5.747                 | 3.099                   | 17.806                 | 8  |
| 9  | 1.999                  | .5002                 | .0801                  | .1601                   | 12.488                 | 6.247                 | 3.491                   | 21.808                 | 9  |
| 10 | 2.159                  | .4632                 | .0690                  | .1490                   | 14.487                 | 6.710                 | 3.871                   | 25.977                 | 10 |
| 11 | 2.332                  | .4289                 | .0601                  | .1401                   | 16.645                 | 7.139                 | 4.240                   | 30.266                 | 11 |
| 12 | 2.518                  | .3971                 | .0527                  | .1327                   | 18.977                 | 7.536                 | 4.596                   | 34.634                 | 12 |
| 13 | 2.720                  | .3677                 | .0465                  | .1265                   | 21.495                 | 7.904                 | 4.940                   | 39.046                 | 13 |
| 14 | 2.937                  | .3405                 | .0413                  | .1213                   | 24.215                 | 8.244                 | 5.273                   | 43.472                 | 14 |
| 15 | 3.172                  | .3152                 | .0368                  | .1168                   | 27.152                 | 8.559                 | 5.594                   | 47.886                 | 15 |

10%

## Compound Interest Factors

10%

| n  | Single Payment         |                       | Uniform Payment Series |                         |                        |                       | Arithmetic Gradient     |                        | n  |
|----|------------------------|-----------------------|------------------------|-------------------------|------------------------|-----------------------|-------------------------|------------------------|----|
|    | Compound Amount Factor | Present Worth Factor  | Sinking Fund Factor    | Capital Recovery Factor | Compound Amount Factor | Present Worth Factor  | Gradient Uniform Series | Gradient Present Worth |    |
|    | Find F Given P<br>F/P  | Find P Given F<br>P/F | Find A Given F<br>A/F  | Find A Given P<br>A/P   | Find F Given A<br>F/A  | Find P Given A<br>P/A | Find A Given G<br>A/G   | Find P Given G<br>P/G  |    |
| 1  | 1.100                  | .9091                 | 1.0000                 | 1.1000                  | 1.000                  | 0.909                 | 0                       | 0                      | 1  |
| 2  | 1.210                  | .8264                 | .4762                  | .5762                   | 2.100                  | 1.736                 | 0.476                   | 0.826                  | 2  |
| 3  | 1.331                  | .7513                 | .3021                  | .4021                   | 3.310                  | 2.487                 | 0.937                   | 2.329                  | 3  |
| 4  | 1.464                  | .6830                 | .2155                  | .3155                   | 4.641                  | 3.170                 | 1.381                   | 4.378                  | 4  |
| 5  | 1.611                  | .6209                 | .1638                  | .2638                   | 6.105                  | 3.791                 | 1.810                   | 6.862                  | 5  |
| 6  | 1.772                  | .5645                 | .1296                  | .2296                   | 7.716                  | 4.355                 | 2.224                   | 9.684                  | 6  |
| 7  | 1.949                  | .5132                 | .1054                  | .2054                   | 9.487                  | 4.868                 | 2.622                   | 12.763                 | 7  |
| 8  | 2.144                  | .4665                 | .0874                  | .1874                   | 11.436                 | 5.335                 | 3.004                   | 16.029                 | 8  |
| 9  | 2.358                  | .4241                 | .0736                  | .1736                   | 13.579                 | 5.759                 | 3.372                   | 19.421                 | 9  |
| 10 | 2.594                  | .3855                 | .0627                  | .1627                   | 15.937                 | 6.145                 | 3.725                   | 22.891                 | 10 |
| 11 | 2.853                  | .3505                 | .0540                  | .1540                   | 18.531                 | 6.495                 | 4.064                   | 26.396                 | 11 |
| 12 | 3.138                  | .3186                 | .0468                  | .1468                   | 21.384                 | 6.814                 | 4.388                   | 29.901                 | 12 |
| 13 | 3.452                  | .2897                 | .0408                  | .1408                   | 24.523                 | 7.103                 | 4.699                   | 33.377                 | 13 |
| 14 | 3.797                  | .2633                 | .0357                  | .1357                   | 27.975                 | 7.367                 | 4.996                   | 36.801                 | 14 |
| 15 | 4.177                  | .2394                 | .0315                  | .1315                   | 31.772                 | 7.606                 | 5.279                   | 40.152                 | 15 |

12%

## Compound Interest Factors

12%

| n  | Single Payment         |                       | Uniform Payment Series |                         |                        |                       | Arithmetic Gradient     |                        | n  |
|----|------------------------|-----------------------|------------------------|-------------------------|------------------------|-----------------------|-------------------------|------------------------|----|
|    | Compound Amount Factor | Present Worth Factor  | Sinking Fund Factor    | Capital Recovery Factor | Compound Amount Factor | Present Worth Factor  | Gradient Uniform Series | Gradient Present Worth |    |
|    | Find F Given P<br>F/P  | Find P Given F<br>P/F | Find A Given F<br>A/F  | Find A Given P<br>A/P   | Find F Given A<br>F/A  | Find P Given A<br>P/A | Find A Given G<br>A/G   | Find P Given G<br>P/G  |    |
| 1  | 1.120                  | .8929                 | 1.0000                 | 1.1200                  | 1.000                  | 0.893                 | 0                       | 0                      | 1  |
| 2  | 1.254                  | .7972                 | .4717                  | .5917                   | 2.120                  | 1.690                 | 0.472                   | 0.797                  | 2  |
| 3  | 1.405                  | .7118                 | .2963                  | .4163                   | 3.374                  | 2.402                 | 0.925                   | 2.221                  | 3  |
| 4  | 1.574                  | .6355                 | .2092                  | .3292                   | 4.779                  | 3.037                 | 1.359                   | 4.127                  | 4  |
| 5  | 1.762                  | .5674                 | .1574                  | .2774                   | 6.353                  | 3.605                 | 1.775                   | 6.397                  | 5  |
| 6  | 1.974                  | .5066                 | .1232                  | .2432                   | 8.115                  | 4.111                 | 2.172                   | 8.930                  | 6  |
| 7  | 2.211                  | .4523                 | .0991                  | .2191                   | 10.089                 | 4.564                 | 2.551                   | 11.644                 | 7  |
| 8  | 2.476                  | .4039                 | .0813                  | .2013                   | 12.300                 | 4.968                 | 2.913                   | 14.471                 | 8  |
| 9  | 2.773                  | .3606                 | .0677                  | .1877                   | 14.776                 | 5.328                 | 3.257                   | 17.356                 | 9  |
| 10 | 3.106                  | .3220                 | .0570                  | .1770                   | 17.549                 | 5.650                 | 3.585                   | 20.254                 | 10 |
| 11 | 3.479                  | .2875                 | .0484                  | .1684                   | 20.655                 | 5.938                 | 3.895                   | 23.129                 | 11 |
| 12 | 3.896                  | .2567                 | .0414                  | .1614                   | 24.133                 | 6.194                 | 4.190                   | 25.952                 | 12 |
| 13 | 4.363                  | .2292                 | .0357                  | .1557                   | 28.029                 | 6.424                 | 4.468                   | 28.702                 | 13 |
| 14 | 4.887                  | .2046                 | .0309                  | .1509                   | 32.393                 | 6.628                 | 4.732                   | 31.362                 | 14 |
| 15 | 5.474                  | .1827                 | .0268                  | .1468                   | 37.280                 | 6.811                 | 4.980                   | 33.920                 | 15 |