

Non-programmable calculators are permitted. This test is closed book.

Supply your answers on this sheet, but TA's have extra paper if you need it.

**PLEASE PRINT**

\_\_\_\_\_

First name

\_\_\_\_\_

Last name

\_\_\_\_\_

Student number

**Please show your work where appropriate!**

1. [5] Determine  $\int -3x^{-1} - \frac{4}{5\sqrt[5]{x}} + (x+1)^2 - e^x \, dx$

2. [4] Determine  $\int 2(2x+1)^3 \, dx$ . There are 2 ways to do this; pick one.

3. [4] Determine  $\int \frac{e^{\sqrt{x}} + 1}{2\sqrt{x}} \, dx$  (HINT: separate the integrand first, then integrate)

4. Let  $F(x) = \int x^{-1} - 2\sqrt[3]{x^2} + x^4 - 2\sqrt[5]{x^4} + 1 \, dx$ .

- [5] Determine the most general antiderivative  $F(x)$ .
- [2] Determine the constant of integration if  $F(-1) = 3$

5. [4] Determine the area under the curve  $y = \sqrt[4]{x^3}$  between the values  $x = 1$  and  $x = 16$ . The curve lies above the  $x$  axis.

6. **Profit maximization:** you are given the following information about a firm: the wage rate ( $w$ ) is 200, the rental rate ( $r$ ) is 12.5, the price ( $p$ ) is 240 and production output is given by the model  $Q = 2.5 K^{0.25} L^{0.5}$ . Use *any method* to determine:

a. [4] The values of $K$ and $L$ that maximize profits.	b. [1] The resulting production output $Q$ .	c. [1] The profit $\Pi$ .
---	--	---------------------------

7. [5] Determine the area of the region enclosed between the curves  $y = x^2$  and  $y = 3x + 4$ . It is known that the 2 curves meet at the points  $(-1, 1)$  and  $(4, 16)$ .