

Solution for Assignment 1

P 1.4 (10 points)

the sixteen bit number that is the largest is
 1111 1111 1111 1111, and the largest number in decimal
 is $2^{16} - 1 = (65535)_{10}$.

In hexo-decimal the number is $(FFFF)_{16}$

P 1.8

a) $(431)_{10} \rightarrow ()_2$

Handwritten binary conversion steps for (431)₁₀ using repeated division by 2:

$$\begin{array}{r} 431 \div 2 = 215 \text{ r } 1 \\ 215 \div 2 = 107 \text{ r } 1 \\ 107 \div 2 = 53 \text{ r } 1 \\ 53 \div 2 = 26 \text{ r } 1 \\ 26 \div 2 = 13 \text{ r } 0 \\ 13 \div 2 = 6 \text{ r } 1 \\ 6 \div 2 = 3 \text{ r } 0 \\ 3 \div 2 = 1 \text{ r } 1 \\ 1 \div 2 = 0 \text{ r } 1 \end{array}$$

$(431)_{10} \rightarrow (110101111)_2$
 (10 points)

b) $(431)_{10} \rightarrow ()_{16}$

Handwritten hexadecimal conversion steps for (431)₁₀ using repeated division by 16:

$$\begin{array}{r} 431 \div 16 = 26 \text{ r } 15 \\ 26 \div 16 = 1 \text{ r } 10 \\ 1 \div 16 = 0 \text{ r } 1 \end{array}$$

$(431)_{10} \rightarrow (1AF)_{16}$ (10 points)
 (1 A F)₁₆
 (0001 1001 1111)₂

of course method b is faster.

P 1.10

a) $(\underbrace{0001}_1.\underbrace{1001}_9)_2$
 $(1.9)_{16}$

and

$(1.10010)_2 = 1 + 2^{-1} + 2^{-4} = (1.5625)_{10}$
 (5 points)

so $(1.10010)_2 \rightarrow (1.9)_{16}$

$(1.10010)_2 \rightarrow (1.5625)_{10}$ (5 points)

b) $(110.010)_2 \rightarrow (6.4)_{16}$ and $(110.010)_2 = (6.25)_{10}$

the reason why the answer in (b) is 4 times the answer in (a) is because 110.010 is the same as 1.10010 except that it is shifted by two places.

P 1.11

$$\begin{array}{r} 111011 \\ \underline{101} \\ 01001 \\ \underline{101} \\ 001001 \\ \underline{101} \\ 0001000 \\ \underline{101} \\ 00110 \\ \underline{101} \\ 001 \end{array}$$

$111011 \div 101 = 1011.11$

(10 points)

001 we can stop here.

P 1.14

a) $1's \{ 00010000 \} = 11101111$ (5 points)

$2's \{ 00010000 \} = 11110000$

b) $1's \{ 00000000 \} = 11111111$ (5 points)

$2's \{ 00000000 \} = 00000000$

c) $1's \{ 11011010 \} = 00100101$ (5 points)

$2's \{ 11011010 \} = 00100110$

P 1.18

c) $1001 - 110101 = 1001 + 2's \{ 110101 \} = 1001 + 001011$

$$\begin{array}{r} 001001 \\ 001011 \\ \hline 010100 \end{array}$$

no end carry, therefore the answer is $-2's(010100) = -101100$ (5 points)

d) $101000 - 10101 = 101000 - 010101 = 101000 + 2's(010101)$
 $= 101000 + 101011 = \underline{\underline{010011}}$ (5 points)

P 1.23

$$\begin{array}{r} + 791 \\ 658 \\ \hline 1449 \end{array}$$

$$\begin{array}{r} 0111 \\ \hline 0110 \\ \hline 1110 \\ \hline 0110 \\ \hline 10100 \end{array} + \begin{array}{r} 1001 \\ \hline 0101 \\ \hline 1110 \\ \hline 0110 \\ \hline 0100 \end{array} + \begin{array}{r} 0001 \\ \hline 1000 \\ \hline 1001 \end{array}$$

(10 points)

the answer is $(1010001001001)_{BCD}$

P 1.24

decimal Equivalent

6	4	2	1		
0	0	0	0	→	0
0	0	0	1	→	1
0	0	1	0	→	2
0	0	1	1	→	3
0	1	0	0	→	4
0	1	0	1	→	5
0	1	1	0	→	6 or
0	1	1	1	→	7 or
1	0	0	0	→	6 ←
1	0	0	1	→	7 ←
1	0	1	0	→	8
1	0	1	1	→	9
1	1	0	0		don't care
1	1	0	1		don't care
1	1	1	0		don't care
1	1	1	1		don't care

(15 points)