

**Assignment** *AnsKey*  
Students need to write detailed answers

1. (2 marks) a. Discuss the law of demand. Graph the following demand- supply equations:

$$Q_d = 100 - 0.5P$$
$$Q_s = P$$

- b. Calculate the equilibrium price and quantity. Find the excess demand, if the price is set at \$50.
- c. Suppose the government imposes a tax (\$2/unit) on the seller. Determine the new equilibrium price and quantity.
- d. Calculate the amount of tax revenue, and show it on a diagram.

2. (2 marks) Assume the market demand for wheat is as follows:

$$Q_d = 45 - 2p + 0.3Y + 1p_b$$

where Y refers to income and  $p_b$  refers to the price of barley.

- i. Assuming that wheat and barley both sell for \$1, and income is \$20, calculate the price elasticity, cross-price elasticity, and income elasticity of demand for wheat.
- ii. If income goes up by 50%, what will be the percentage change in quantity demand of wheat?

3. (2 marks) Using suitable diagrams and appropriate assumptions, explain why two indifference curves cannot intersect.

4. (2 marks) a. For each of the following utility functions, calculate the MRS and explain whether it is diminishing or not:

$$U = 16q_1q_2^3 \dots\dots\dots i$$

$$U = \alpha \ln q_1 + (1 - \alpha) \ln q_2 \dots\dots\dots ii$$

$$U = 10q_1 + 5q_2 \dots\dots\dots iii$$

$$U = \min(q_1, q_2) \dots\dots\dots iv$$

5. (2 marks) Suppose Jason's utility function is as follows:  $U = q_1^{0.8} q_2^{0.2}$

- i. and his income,  $Y = \$100$ , and prices are  $P_1 = \$20$  and  $P_2 = \$10$ ; calculate the utility maximizing quantities of  $q_1$  and  $q_2$ , and the resulting utility. Show it on a diagram.
- ii. if his new income,  $Y_1 = \$150$ , and prices are the same. Calculate the new level of utility and show it on a diagram.

① a. Law of Demand (see ch.2) assumptions

$Q_d = 100 - 0.5P$  ——— ①

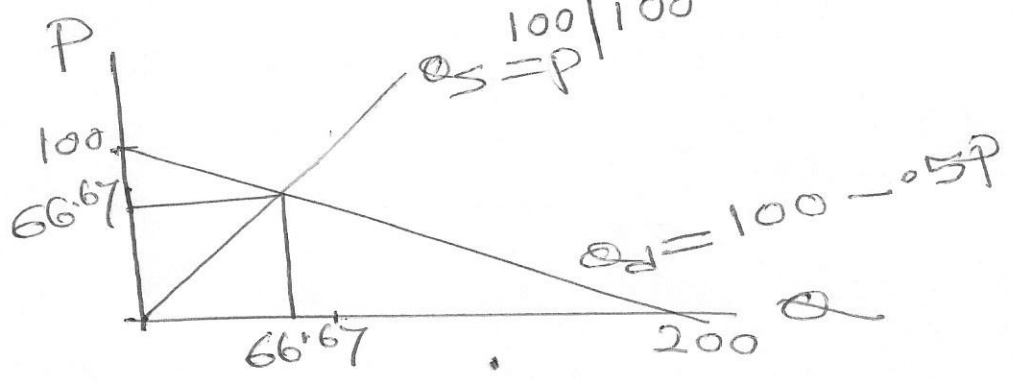
$Q_s = P$  ————— ②

From ①

| $Q_d$ | $P$ |
|-------|-----|
| 100   | 0   |
| 0     | 200 |

From ②

| $Q_s$ | $P$ |
|-------|-----|
| 0     | 0   |
| 100   | 100 |



② b. At equilibrium,

$Q_s = Q_d$

$P = 100 - 0.5P$

$1.5P = 100$

$P = \frac{100(10)}{15} = \frac{200}{3} = 66.67$  \$

$Q = \frac{200}{3} = 66.67$  units

① c. To assess impacts of tax, use inverse supply-demand functions:

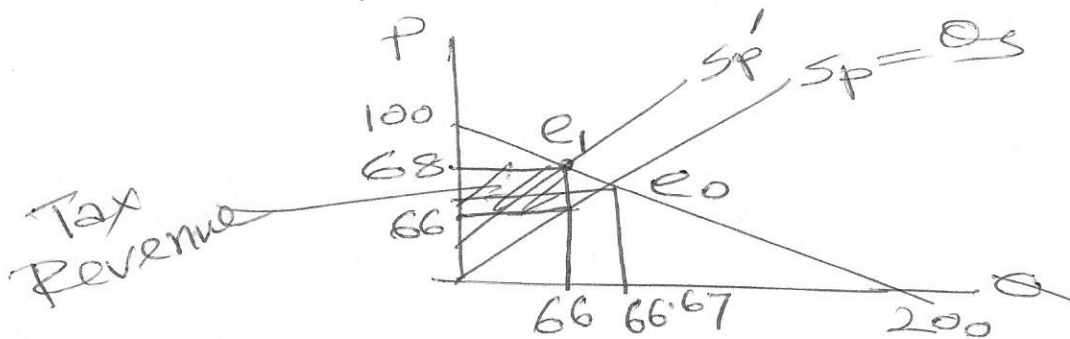
$$P = Q_s$$

$$S_p = Q_s$$

$$S'_p = S_p + 2 = 2 + Q_s$$

$$P_D = 100 - Q_D$$

$$D_p = 200 - 2Q_D$$



With tax, at equilibrium

$$S'_p = D_p$$

$$Q_s + 2 = 200 - 2Q_d$$

$$3Q = 198$$

$$Q = 66 \text{ units}$$

Price paid by the consumer =

$$S'_p = 2 + 66 = \$68$$

Price received by the producer = \$66

④ → Tax revenue =  $2(66) = \$132$   
shaded area on the graph.

2

$$Q_d = 45 - 2P + .3Y + 1P_b$$

1

solve for:

$$Q = 45 - 2(1) + .3(20) + 1(1)$$

$$= 50 \text{ units}$$

$$\epsilon_{Q,P} = \frac{dQ}{dP} \cdot \frac{P}{Q} = -2 \frac{1}{50} = -0.04$$

$$\epsilon_{Q,P_b} = \frac{dQ}{dP_b} \cdot \frac{P_b}{Q} = 1 \frac{1}{50} = 0.02$$

$$\epsilon_{Q,Y} = \frac{dQ}{dY} \cdot \frac{Y}{Q} = .3 \frac{20}{50} = 0.12$$

~~1~~

11

$$\epsilon_{Q,Y} = 0.12 = \frac{\% \Delta Q}{\% \Delta Y}$$

$$\therefore \% \Delta Q = 0.12 \% \Delta Y$$

$$= 0.12(50)$$

$$= 6\%$$

\therefore A 50% increase in income will raise demand for wheat by 6%.

③ See ch. 3

Prove that an intersection violates the transitivity and non-satiation assumptions.

④

$$MRS = - \frac{U_1}{U_2} = - \frac{\partial U / \partial q_1}{\partial U / \partial q_2}$$

①  $U = 16q_1 q_2^3$

$$\frac{\partial U}{\partial q_1} = 16 q_2^3$$

$$\frac{\partial U}{\partial q_2} = 48 q_1 q_2^2$$

$$\therefore MRS = - \frac{16 q_2^3}{48 q_1 q_2^2} = - \frac{1}{3} \frac{q_2}{q_1}$$

As  $q_1$  goes up,  $\frac{q_2}{q_1}$  would drop.  $\therefore$  the MRS is diminishing

②  $U = \alpha \ln q_1 + (1-\alpha) \ln q_2$

$$MRS = - \frac{\frac{\alpha}{q_1}}{\frac{(1-\alpha)}{q_2}} = - \frac{\alpha}{(1-\alpha)} \cdot \frac{q_2}{q_1}$$

$\therefore$  MRS is diminishing same as ①.

III

$$U = 10q_1 + 5q_2$$

$$MRS = - \frac{10}{5} = -2$$

if  $q_1$  goes up MRS stays the same (-2)

∴ MRS is constant (not diminishing)

IV

$$U = \min(q_1, q_2)$$

$$MRS = - \frac{0}{0} = -0$$

$\frac{\partial U}{\partial q_1} = 0$  if  $q_1$  goes up keeping  $q_2$  constant  $U$  does not change.

∴ MRS is constant (not diminishing).

5  
i

At equilibrium

$$MRS = MRT$$

$$U = q_1^{.8} q_2^{.2}$$

$$MRS = - \frac{.8 q_1^{-.2} q_2^{.2}}{.2 q_1^{.8} q_2^{-.8}} = - \frac{4 q_2}{q_1}$$

$$MRT = - \frac{P_1}{P_2} = - \frac{20}{20}$$

or  
Maximize

$$L = q_1^{.8} q_2^{.2} + \lambda [100 - 20q_1 - 20q_2]$$

US FAC

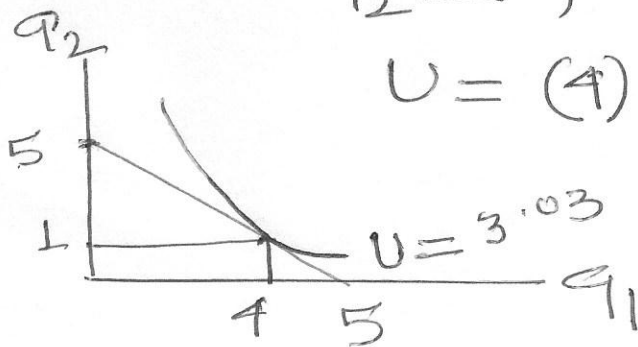
$$\frac{4 q_2}{q_1} = \frac{20}{20} \quad q_1 = 4 q_2$$

$$20 q_1 + 20 q_2 = 100$$

$$80 q_2 + 20 q_2 = 100$$

$$q_2 = 1, \quad q_1 = 4$$

$$U = (4)^{.8} (1)^{.2} = (3.03) \cdot 1 = 3.03$$



5  
11

P8/8

$$Y = 150$$

$$20q_1 + 20q_2 = 150$$

$$\therefore q_1 = 4q_2 \quad \left. \begin{array}{l} 80q_2 + 20q_2 = 150 \\ q_2 = 1.5 \text{ units} \end{array} \right\}$$

$$q_2 = 1.5 \text{ units}$$

$$q_1 = 4(1.5) = 6 \text{ units}$$

$$U = (6)^{.8} (1.5)^{.2}$$

$$= (4.19)(2.25)$$

$$= 9.43$$

