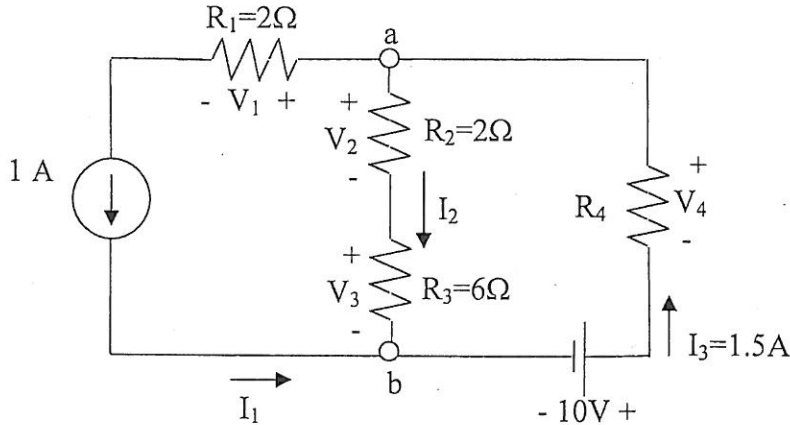


Instructions: Answer all 3 questions. Each question is equally weighted.
Answer on the exam questionnaire. Use the back of pages for rough work.

Q1	Q2	Q3	Total

AUTHORIZED MEMORANDA: CALCULATOR, OPEN NOTES, TEXT (Foundations of Electric Circuits). NO COMMUNICATING DEVICES!

Question 1:



- Apply KCL to find I_2 .
- Apply Ohm's law to find V_{ab} .
- Calculate the power supplied by the 1A source.
- Find the value of R_4 .

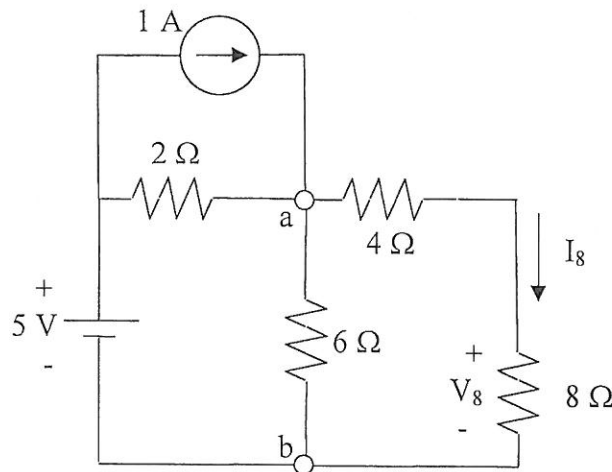
a) At node b) $I_1 + I_2 - I_3 = 0$ ①
 $1A + I_2 - 1.5A = 0$ ① $I_2 = 0.5A$

b) $V_{ab} = V_2 + V_3 = I_2 (R_2 + R_3)$ ①
 $= 0.5A \times (2\Omega + 6\Omega)$ ① $V_{ab} = 4V$

c) KVL: $V_{source} + V_1 - V_{ab} = 0$ ①
 $V_{source} = 4V - 1A \times 2\Omega = 2V$ ①
 Power = $V \times I = 2V \times 1A$ ① $P_{source} = 2W$

d) KVL: $10V + V_4 - V_{ab} = 0$ ①
 $V_4 = 4V - 10V = -6V$ ①
 then $R_4 = \frac{V_4}{I_3} = \frac{-6V}{1.5A}$ ① $R_4 = 4\Omega$

Question 2:



- For the 1A source only (voltage source = 0V), use current division to find I_8 .
- For the 5V source only (current source = 0A), use voltage division to find V_8 .
- With **both** sources in the circuit, find the total current through the $8\ \Omega$ resistor.
- With **both** sources in the circuit, find the power delivered to the $8\ \Omega$ resistor.

$$a) \quad I_8 = 1A \times \frac{R_{eq}}{(4+8)\Omega} = 1A \times \frac{2\Omega // 6\Omega // 12\Omega}{12\Omega} = \underline{0.111A}$$

$$b) \quad V_8 = V_{ab} \times \frac{8\Omega}{(8+4)\Omega} = 5V \times \left(\frac{6\Omega // 12\Omega}{2 + 6\Omega // 12\Omega} \right) \left(\frac{8\Omega}{12\Omega} \right)$$

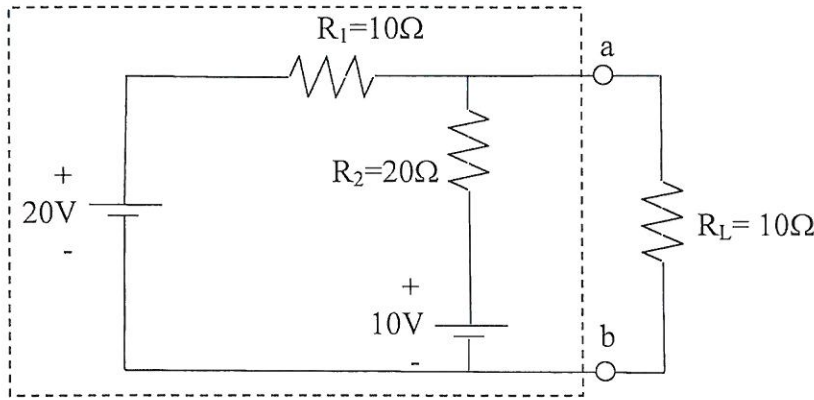
$$V_8 = 5V \times \frac{4}{6} \times \frac{8}{12} = \frac{20}{9} V = \underline{2.222V}$$

$$c) \quad \text{For the 5V source} \quad I_8 = \frac{V_8}{R} = \frac{2.222V}{8\Omega} = 0.278A$$

$$I_{8\text{total}} = 0.111A + 0.278A = \underline{0.389A}$$

$$d) \quad P = I^2 R = (0.389A)^2 \times 8\Omega = \underline{1.21W}$$

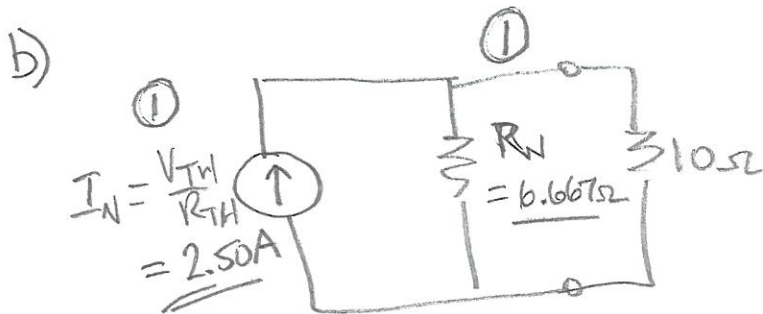
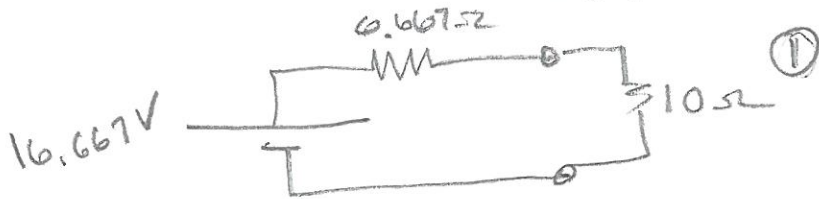
Question 3: R_L is a load resistor.



- Evaluate V_{th} and R_{th} , and draw the Thevenin equivalent for the circuit driving the load resistor R_L .
- Convert the circuit to a Norton equivalent circuit.
- Find the power delivered to the load resistor R_L .
- What value of R_L would result in maximum power dissipated in the load? Calculate the power for this new value of R_L .

a) $V_{oc} = 20V \times \frac{20}{20+10} + 10V \left(1 - \frac{20}{20+10}\right)$
 $V_{th} = 16.667V$

$R_{th} = R_{eq} |_{source=0} = 10\Omega // 20\Omega = 6.667\Omega$



d) maximum power
 $R_L = R_{th} = 6.667\Omega$

Then
 $P_L = \frac{(16.667V \times \frac{1}{2})^2}{6.667}$
 $P_L = 10.417W$

c) $P = \frac{V^2}{R} = \frac{(16.667V \times \frac{10\Omega}{16.667\Omega})^2}{10\Omega}$
 $P_L = 10W$