

# Assignment 3 MEC 830

①


Covers:

{ Tachometer, Absolute encoder,  
MZMS sensors }  
⇒ from chapter 3 sensors.

Chapter 5 Signal processing 5.1 ~ 5.3

Chapter 6. Wheeled mobile robot

## Problem #1

Design an absolute optical encoder with a resolution of  $22.5^\circ$  using straight binary code, please show the schematic drawing of the encoder disk with transparent and opaque areas indicated.  [Lecture 16, 17, 18. Page 13].

problem #2

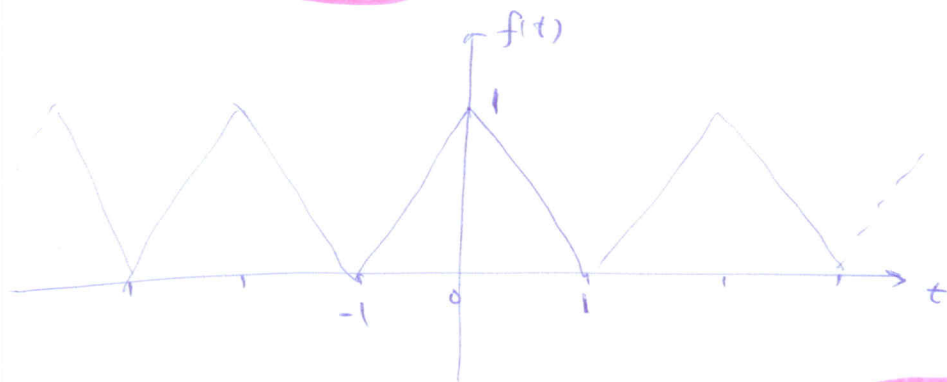
What is the fundamental <sup>②</sup>  
difference between incremental ~~and~~ and  
absolute encoders? ~~what~~ Which  
kind encoder we are using with  
the Lego system?

problem #3

Use your own words with drawings  
(if necessary) to explain how a  
rotation tachometer works.

Problem #4

periodic signal is shown in the fig.



$$f(t) = \begin{cases} 1+t & -1 \leq t \leq 0 \\ 1-t & 0 < t \leq 1 \end{cases} \text{ for one period.}$$

1) find Fourier Series of f(t)

2) Plot Amplitude Spectrum.

3) plot power spectrum.

4) Take the first 11 terms of the ~~Fourier~~ -

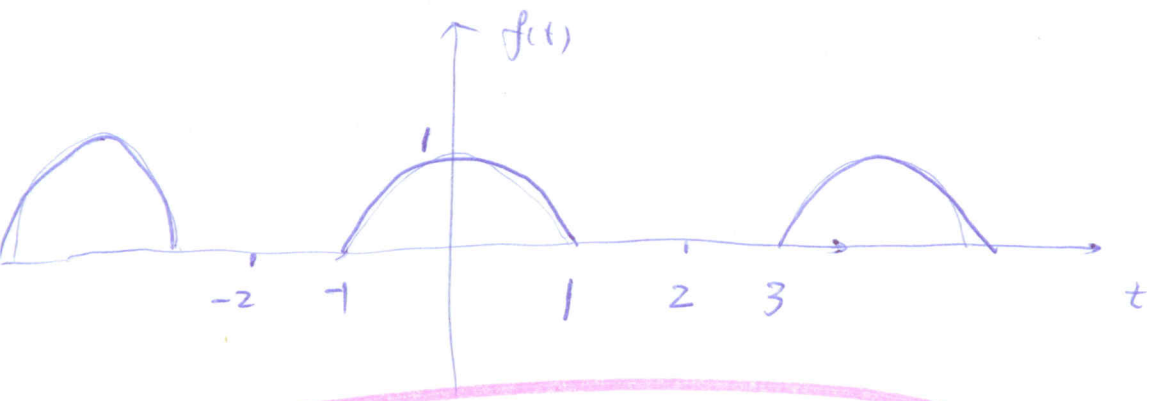
Fourier Series, use ~~any~~ software such as maple, Matlab -- to plot the signal in the range of [-1, 1]

Problem #5

for the periodic wave,

one period

can be expressed as



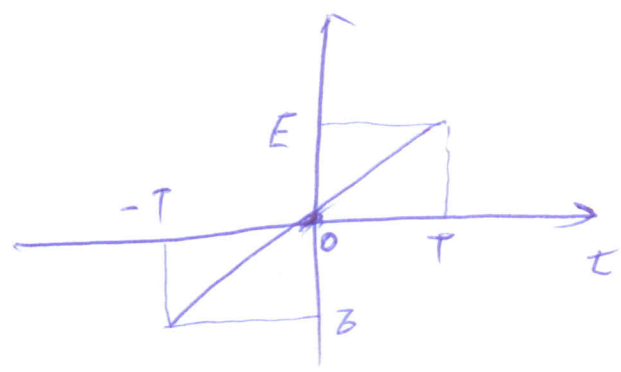
$$f(t) = \begin{cases} \cos \frac{\pi}{2} t & [-1, 1] \\ 0 & [-2, -1] \text{ \& } [1, 2] \end{cases}$$

1) find Fourier Series

plot  
2) Power spectrum

Problem # 6

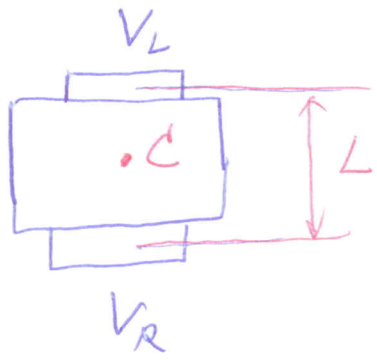
① Find Fourier transform of the pulse shown in the Fig.



② if  $Z=1$ ,  $T=1$ , plot Amplitude spectrum.

③ if  $Z=1$ ,  $T=1$ , plot Energy spectrum.

Problem #7



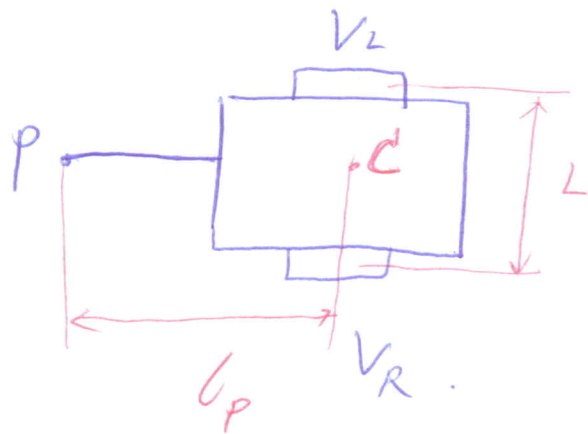
Differential drive wheeled Robot. With ~~parameter~~  
~~\$L\$~~ \$L\$ as the distance between the center of two wheels.

1) Derive ~~the~~ the condition, under which the trajectory of 'C' will be a circle.  
 [Hint: a condition means ~~how~~ how to set \$V\_R, V\_L\$. ]

2) Relation of \$R\$ (radius of trajectory of C) to \$V\_R, V\_L, L\$.

37) What is the maximum and minimum radius  $\rightarrow$  ~~the point "C" trajectory~~ the robot can achieve if the pen is located at "C" point.

Problem #8



for a differential drive robot, carrying a pen with a distance of  $l_p$  from C,

17) ~~Derive~~ Derive the condition, under which the robot can plot a circle.

2) Relation of  $R$  to  $L_P, L, V_R, V_L$ .

8)

3) Maximum & minimum  $R$ .

$R$  is the radius of the circle plotted by the robot

Problem #7, Q #8 can be finished with help of software such as Maple, Matlab, ...