

let  $p_z = p_0$  (pressure at 0 depth)

let  $h = y_2 - y_1$  (height of water above depth  $h$ )

This gives  $p = p_0 + \rho gh$

What is pressure at 100m below sea?

$$p = p_{\text{atm}} + (1.03 \frac{\text{g}}{\text{cm}^3}) (9.8 \text{ m/s}^2) (100\text{m})$$

$$p = 1.013 \times 10^5 \text{ Pa} + 1.010 \times 10^6 \text{ Pa}$$

1 atm

$\approx 10 \text{ atm}$

gauge pressure

→ pressure above

atmospheric pressure

absolute pressure

→ total pressure

# Pascal's Law

2-2

$$p = \frac{F_1}{A_1} = \frac{F_2}{A_2}$$

$$F_2 = \frac{A_2}{A_1} F_1$$

force has been multiplied by ratio of areas.

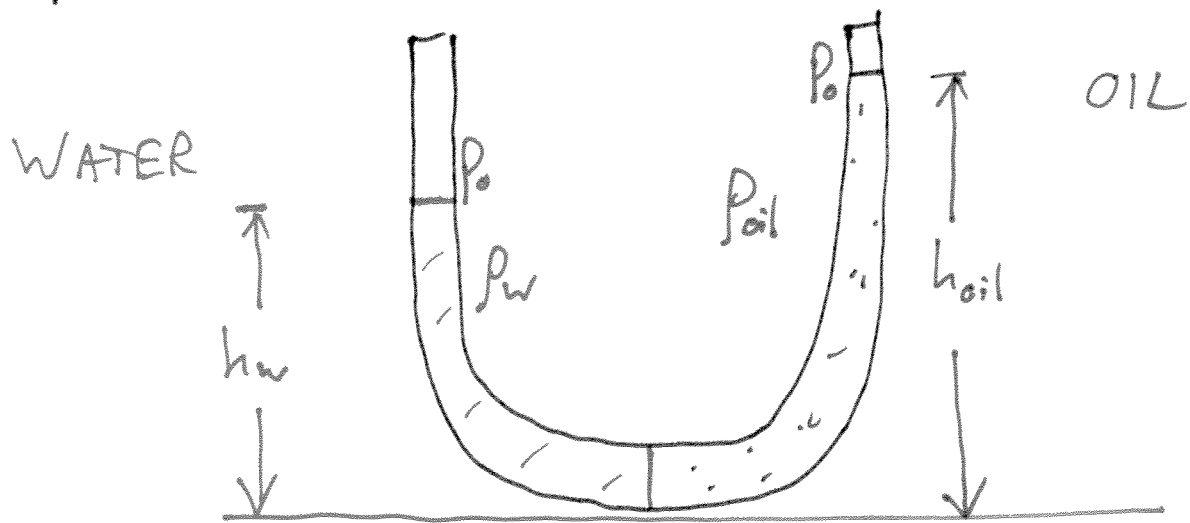
Principle behind  
hydraulics.

Figure 12.8 a)  $p = p_{atm} + \rho gh$

b)  $p_{atm} = \rho gh$

# Example 12.4

2-3



What is more dense?

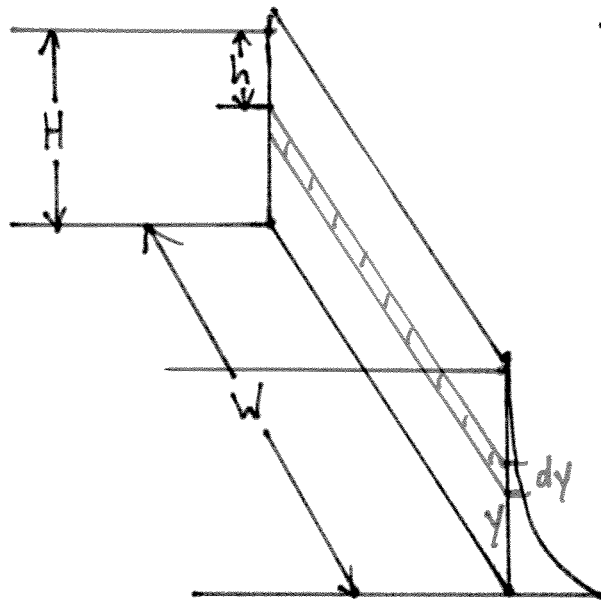
$$\underline{\rho_{oil} < \rho_{water}}$$

Express  $h_{oil}$  in terms of all other variables.

$$p = P_0 + \rho_w h_w g \quad \rho_w h_w g$$

$$p = P_0 + \rho_{oil} h_{oil} g$$

$$h_{oil} = \frac{\rho_{water} h_{water}}{\rho_{oil}}$$



Water is filled to a height  $H$  behind a dam with width  $w$ . Determine the force exerted by the water on the dam.

- pressure varies with depth, cannot calculate force simply by multiplying by area

variation } integrate  
total force }

pressure due to water only at depth  $h$

$$P = \rho g h = \rho g (H - y)$$

$$dF = p dA = \rho g (H - y) w dy \quad (dA = w dy)$$

$$F = \int p dA = \int_0^H \rho g (H - y) w dy$$

$$= \frac{1}{2} \rho g w H^2$$

## 12.5 Bernoulli's Equation

2-5

When an incompressible fluid flows along a flow tube with varying cross section, its speed must change, and so an element of fluid must have an acceleration

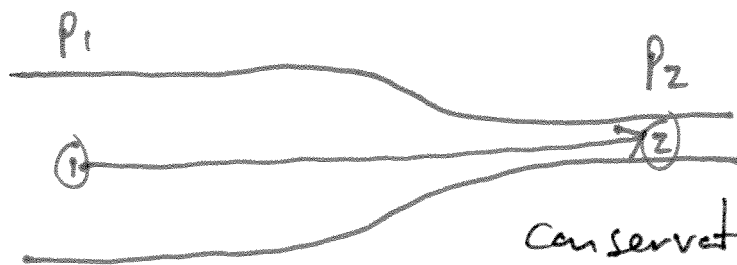
↳ This comes from change in pressure  
derivation p. 385 - 386

for everywhere along flow

$$p + \rho g y + \frac{1}{2} \rho v^2 = \text{constant}$$

so for any 2 points along flow

$$p_1 + \cancel{\rho g y_1} + \frac{1}{2} \rho v_1^2 = p_2 + \cancel{\rho g y_2} + \frac{1}{2} \rho v_2^2$$



conservation of volume, flow velocity must be greater at (2)

$$v_1 A_1 = v_2 A_2$$

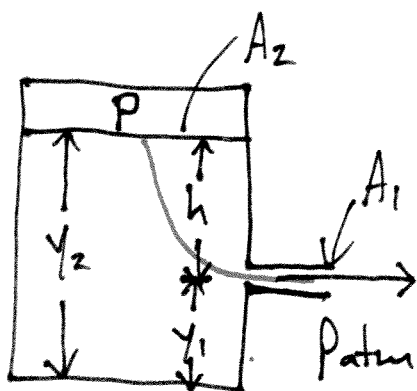
$$- p_2 < p_1$$

Solve for  $v_2$ 

$$P_1 + \frac{1}{2} \rho \left( \frac{A_2}{A_1} \right)^2 v_2^2 = P_2 + \frac{1}{2} \rho v_2^2$$

$$v_2 = A_1 \sqrt{\frac{2(P_1 - P_2)}{\rho(A_1^2 - A_2^2)}}$$

FIRE EXTINGUISHER (pressurized tank)

What is  $v_1$ ?

$$\rho + \rho g y_2 + \frac{1}{2} \rho v_2^2 = P_{atm} + \rho g y_1 + \frac{1}{2} \rho v_1^2$$

assume  $A_2 \gg A_1$ 

$$v_1 A_1 = v_2 A_2$$

$$v_2 = \frac{A_1 v_1}{A_2}$$

$$v_2 = 0$$

$$v_1 = \sqrt{\frac{2(P - P_0) + 2gh}{\rho}}$$

$$y_2 - y_1 = h$$

Open up top of container

2-7

$$p_{atm} + \rho g y_2 = p_{atm} + \rho g y_1 + \frac{1}{2} \rho v_1^2$$

$$g(y_2 - y_1) = \frac{1}{2} v_1^2$$

$$v_1 = \sqrt{2gh}$$

Torricelli's Law

speed of object  
falling freely  
a distance of  $h$